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Mark Scheme (Results)

January 2015

Pearson Edexcel International A Level in Core Mathematics 34 (WMA02/01)

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Mathematics C34

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WMA02

General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 125.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M)
 marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper or ag- answer given
- _ or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

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- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q)$$
, where $|pq| = |c|$, leading to $x = ...$
 $(ax^2 + bx + c) = (mx + p)(nx + q)$, where $|pq| = |c|$ and $|mn| = |a|$, leading to $x = ...$

2. Formula

Attempt to use correct formula (with values for a, b and c).

3. Completing the square

Solving
$$x^2 + bx + c = 0$$
: $(x \pm \frac{b}{2})^2 \pm q \pm c$, $q \ne 0$, leading to $x = \dots$

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. $(x^n \rightarrow x^{n-1})$

2. Integration

Power of at least one term increased by 1. $(x^n \rightarrow x^{n+1})$

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

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Question Number	Scheme	Marks
1	y = 7 at point P	B1
	$y = \frac{3x - 2}{(x - 2)^2} \Rightarrow \frac{dy}{dx} = \frac{(x - 2)^2 \times 3 - (3x - 2) \times 2(x - 2)}{(x - 2)^4}$	M1A1
	Sub $x = 3$ into $\frac{dy}{dx} = (-11)$	M1
	$\frac{1}{11} = \frac{y - 7}{x - 3} \Rightarrow x - 11y + 74 = 0$ cso	M1A1 cso
		(6 marks)

- For seeing y = 7 when x = 3. This may be awarded if embedded within an equation. **B**1
- Application of Quotient rule. If the rule is quoted it must be correct. M1

It may be implied by their u = 3x - 2, u' = ..., $v = (x - 2)^2$, v' = ... followed by their $\frac{vu' - uv'}{v^2}$

If the rule is neither stated nor implied only accept expressions of the form

$$\frac{(x-2)^2 \times A - (3x-2) \times B(x-2)}{\left((x-2)^2\right)^2} A, B > 0 \text{ condoning missing brackets}$$

Alternatively applies the Product rule to $(3x-2)(x-2)^{-2}$ If the rule is quoted it must be correct.

It may be implied by their u or v = 3x - 2, u', v or $u = (x - 2)^{-2}$, v' followed by their vu' + uv'

If the rule is neither stated nor implied only accept expressions of the form $A(x-2)^{-2} \pm B(3x-2)(x-2)^{-3}$

If they use partial fractions expect to see
$$y = \frac{3x-2}{(x-2)^2} \Rightarrow y = \frac{P}{(x-2)} + \frac{Q}{(x-2)^2} (P=3, Q=4) \Rightarrow \frac{dy}{dx} = \pm \frac{R}{(x-2)^2} \pm \frac{S}{(x-2)^3}$$

You may also see implicit differentiation etc where the scheme is easily applied.

A1 A correct (unsimplified) form of the derivative.

Accept from the quotient rule versions equivalent to $\frac{dy}{dx} = \frac{(x-2)^2 \times 3 - (3x-2) \times 2(x-2)}{\left((x-2)^2\right)^2}$

Accept from the product rule versions equivalent to $\frac{dy}{dx} = 3(x-2)^{-2} - 2(3x-2)(x-2)^{-3}$

Accept from partial fractions $\frac{dy}{dx} = -3(x-2)^{-2} - 8(x-2)^{-3}$

or $(x-2)^2 \frac{dy}{dx} + y \times 2(x-2) = 3$ from implicit differentiation

FYI: Correct simplified expressions are $\frac{dy}{dx} = \frac{-3x^2 + 4x + 4}{(x-2)^4}$ or $\frac{-3x - 2}{(x-2)^3}$

- Sub x = 3 into what they believe is their derivative to find a numerical value of $\frac{dy}{dx}$. M1
- Uses x = 3 and their numerical value of y with their numerical $\frac{dx}{dy}$ at x = 3 to form an equation of M1a normal. If the form y = mx + c is used then it must be a full method reaching a value for c.
- **A**1 Correct solution only Accept $\pm A(x-11y+74) = 0$ where $A \in \mathbb{N}$. from correct working. Watch for correct answers coming from incorrect versions of $\frac{dy}{dx}$ with eg. $(x-2)^2$ on the denominator

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Past Paper (Mark Scheme)

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Question Number	Scheme	Marks
2	$2\cos 2\theta = 5 - 13\sin\theta \Rightarrow 4\sin^2\theta - 13\sin\theta + 3 = 0$	M1A1
	$\Rightarrow (4\sin\theta - 1)(\sin\theta - 3) = 0$	
	$\sin \theta = \frac{1}{4}$	M1
	$\theta = \text{awrt } 0.253, 2.889 (3\text{dp})$	A1,A1 cso
		(5 marks)

Uses $\cos 2\theta = 1 - 2\sin^2 \theta$ to get a quadratic equation in just $\sin \theta$. M1

If candidate uses $\cos 2\theta = \cos^2 \theta - \sin^2 \theta$ or $2\cos^2 \theta - 1$ they must use $\cos^2 \theta = 1 - \sin^2 \theta$ to form a quadratic equation in just $\sin \theta$ before scoring the M.

- $\pm (4\sin^2\theta 13\sin\theta + 3) = 0$. The = 0 may be implied by subsequent working **A**1
- Solves their 3TQ in $\sin \theta$ with usual rules by factorisation, formula or completing the square. They M1must proceed as far as $\sin \theta = ...$ Accept an answer from a calculator. You may have to pick up a calculator to check their values.
- **A**1 Either of $\theta = \text{awrt } 0.25, 2.89 \text{ (2dp)}$ in radians or either of $\theta = \text{awrt } 14.5, 165.5 \text{ (1dp)}$ in degrees Accept either of awrt 0.08π , 0.92π
- **A**1 Correct solution with only two solutions $\theta = \text{awrt } 0.253, 2.889 \text{ (3dp)}$ within the given range.

Accept equivalents such as awrt 0.0804π , 0.9196π

Ignore any extra answers outside the range.

Note that incorrect factorisation $(4 \sin \theta - 1)(\sin \theta + 3) = 0$ would lead to correct answers. As this mark is cso, it would be withheld in such circumstances.

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Past Paper (Mark Scheme)

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WMA02

Question Number	Scheme		Marks	
3(a)	ν ↑	V shape just in Quad 1and correct position	B1	
	8	Meets/cuts y axis at $(0,8)$	B1	
	0 4 x	Meets x axis at $(4,0)$	B1	
				(3)
(b)	x = 1		B1	
	$x + 5 = -(8 - 2x) \Rightarrow x = 13$		M1A1	(3)
(c)	fg(5) = f(2) = -1		M1A1	
				(2)
(d)	$f'(x) = 2x - 3 \Rightarrow \min \text{ at } x = \frac{3}{2} \Rightarrow \min = -\frac{5}{4}$		M1A1	
	Maximum value = 5		B1	
	$-\frac{5}{4}$,, f(x),, 5		A1	
				(4)
			(12 marks)	

Past Paper (Mark Scheme)

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(a)

B1 Accept a V shape **just in quadrant one** with the left hand end meeting the y - axis, the minimum point on the x - axis and the right hand section being at least as high as the left hand section.



Look for either or shape just in quadrant one. Don't accept a curved base.

- **B**1 The graph meets or cuts the y axis at (0, 8) only. Allow just 8 and condone (8,0) written on the correct axis. There needs to be a graph for this to be awarded
- The graph meets the x axis at (4, 0) only. Allow 4 and condone (0,4) written on the correct axis B1 There needs to be a graph for this to be awarded.

(b)

- For stating that x = 1B1
- For an attempt at the 'second' solution. M1

Accept $x + 5 = -(8 - 2x) \Rightarrow x = \dots$ or $-(x + 5) = 8 - 2x \Rightarrow x = \dots$ or equivalent

Do NOT condone invisible brackets in this case

Accept $(x+5)^2 = (8-2x)^2 \implies x = ...$

x=13 and no other solutions (apart from x=1). Accept this for both marks as long as no **A**1 incorrect working is seen. Eg $x+5=-8-2x \Rightarrow x=13$ is M0 A0

(c)

M1Scored for a full method to find fg(5).

Accept x = 5 being substituted into |8 - 2x| and the result being substituted into $x^2 - 3x + 1$

Accept an attempt to substitute x = 5 into $(|8-2x|)^2 - 3|8-2x| + 1$

Accept for an attempt at f(2) but not f(-2)

-1 only. Accept this for both marks as long as no incorrect working is seen. A1

(d)

An acceptable method of finding a turning point. A full method using calculus or a full method by M1completion of the square is acceptable. The y value must be attempted.

Using calculus look for $f'(x) = ax + b = 0 \Rightarrow x = ..$ followed by an attempt to find y.

Using completing the square look for $\left(x \pm \frac{3}{2}\right)^2 \pm \left(\frac{3}{2}\right)^2 + 1$ followed by a statement that $y = \pm \left(\frac{3}{2}\right)^2 + 1$

- For achieving the minimum value of $y = -\frac{5}{4}$. Award for y > -1.25 following the M mark **A**1
- **B**1 For achieving the maximum value of y = 5.

This may be scored from an inequality. Accept ..., f, 5 and even ..., f < 5

CSO Allow [-1.25, 5] and y...-1.25- **and** y, 5**A**1

Do not allow y...-1.25- or y, 5 or [-1.25, 5) or $-\frac{5}{4}, f(x) < 5$

Special case: Allow the answer from a graphical calculator as long as it is given with the evidence of a correct sketch. Allow from a table as long as the value at 1.5 is calculated. Score 4/4 Just the (correct) answer, no working, special case award 1,1,0,0

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WMA02

Past Paper (Mark Scheme)

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Question Number	Scheme	Marks
4	$x = 2\sin\theta \Rightarrow \frac{\mathrm{d}x}{\mathrm{d}\theta} = 2\cos\theta$	B1
	$\int \frac{1}{(4-x^2)^{\frac{3}{2}}} dx = \int \frac{1}{(4-4\sin^2\theta)^{\frac{3}{2}}} 2\cos\theta(d\theta)$	M1
	$= \int \frac{1}{4} \sec^2 \theta(d\theta) OR \int \frac{1}{4} \times \frac{1}{\cos^2 \theta} (d\theta)$	M1
	$=\frac{1}{4}\tan\theta$	dM1A1
	Uses limits 0 and $\frac{\pi}{3}$ in their integrated expression	
	$= \left[\frac{1}{4} \tan \theta\right]_0^{\frac{\pi}{3}} = \frac{\sqrt{3}}{4}$	M1A1
		(7 marks)

- B1 States either $\frac{dx}{d\theta} = 2\cos\theta$ or $dx = 2\cos\theta d\theta$. Condone $x' = 2\cos\theta$
- M1 Attempt to produce integral in just θ by substituting $x = 2\sin\theta$ and using $dx = \pm A\cos\theta$ ($d\theta$) You may condone a missing $d\theta$
- M1 Uses $1-\sin^2\theta = \cos^2\theta$ and simplifies integral to $\int C \sec^2\theta (d\theta)$ or $\int \frac{C}{\cos^2\theta} (d\theta)$

Again you may condone a missing $d\theta$

- dM1 Dependent upon previous M1 for $\int \sec^2 \theta \rightarrow \tan \theta$
- A1 $\frac{1}{4} \tan \theta (+c)$. No requirement for the +c
- Changes limits in x to limits in θ of 0 and $\frac{\pi}{3}$, then subtracts their integrated expression either way around. The subtraction of 0 can be implied if f(0) = 0. If the candidate changes the limits to 0 and 60 (degrees) it scores M0, A0. Alternatively they could attempt to change their integrated expression in θ back to a function in x and use the original limits. Such a method would require

seeing either
$$\cos \theta = \sqrt{1 - \frac{x^2}{4}}$$
 or $\tan \theta = \sqrt{\frac{x}{2}} \sqrt{1 - \frac{x^2}{4}}$

A1
$$\frac{\sqrt{3}}{4}$$

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Mathematics C34 WMA02

Question Number	Scheme	Marks
5 (a)	$\frac{1}{\sqrt{1-2x}} = (1-2x)^{-\frac{1}{2}} = 1 + \left(-\frac{1}{2}\right)(-2x) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{1}{2}-1\right)}{2!}(-2x)^2$ $= 1 + x + \frac{3}{2}x^2 + \dots$	M1A1
	$\frac{2+3x}{\sqrt{1-2x}} = (2+3x)(1+x+\frac{3}{2}x^2+\dots$ $= 2+5x+6x^2$	M1 A1*
(b)	Sub $x = \frac{1}{20}$ into both sides of $\frac{2+3x}{\sqrt{1-2x}} = 2+5x+6x^2$ $\frac{43\sqrt{10}}{60} = \frac{453}{200} \qquad \text{oe } \frac{43}{20} = \frac{453}{200} \times \frac{3}{\sqrt{10}}$	M1 dM1
	$\sqrt{10} = \frac{1359}{430} \qquad \text{Accept } \frac{4300}{1359}$	A1 (3) (7 marks)

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WMA02

(a)

M1 Uses the correct form of the binomial expansion with $n = \pm \frac{1}{2}$ and 'x' = $\pm 2x$ to achieve

 $1 + \left(\pm \frac{1}{2}\right) \left(\pm 2x\right) + \frac{\left(\pm \frac{1}{2}\right) \left(\pm \frac{1}{2} - 1\right)}{2} \left(\pm 2x\right)^2 \dots \text{ You may condone missing/invisible brackets.}$

Candidates cannot just write down the answer $1+x+\frac{3}{2}x^2+.$

There must be an intermediate line showing some working for at least the x^2 term.

A1 Correct (unsimplified expression) $1 + \left(-\frac{1}{2}\right)\left(-2x\right) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)}{2}\left(-2x\right)^2$

Condone poor notation such as $-2x^2$ for $(-2x)^2$ if it is subsequently corrected.

Evidence of this could be $1 + -0.5 \times -2x + \frac{-0.5 \times -1.5}{2} \times -2x^2 = 1 + x + \frac{3}{2}x^2 + \dots$

M1 An attempt to multiply their 'quadratic' binomial expansion by (2 + 3x).

Look for at least 4 terms. If they have simplified their binomial expansion to $1+x+\frac{3}{2}x^2+.$

then it is possible to write out the final answer of $2 + 5x + 6x^2$ from $(2 + 3x)(1 + x + \frac{3}{2}x^2)$

This is acceptable for the final M1A1only if the quadratic expansion $1 + x + \frac{3}{2}x^2$ has been simplified from an intermediate line.

A1* $2+5x+6x^2$ Correct solution only. This is a given answer and all aspects must be correct including bracketing.

(b)

M1 Sub $x = \frac{1}{20}$ into **both sides** of the given expression. Condone missing brackets.

Accept for this any equivalent to $\frac{2+3\times0.05}{\sqrt{1-2\times0.05}} = 2.265$

dM1 For an attempt to simplify **both** sides of the expression resulting in an expression involving $\sqrt{10}$ Look for an equation of the from $\frac{a\sqrt{10}}{b} = \frac{c}{d}$ or equivalent where a, b, c and d are integers

Sight of $\frac{43\sqrt{10}}{60}$, on the left hand side and $\frac{453}{200}$ on the right hand side an example of correct work.

An alternative would be $\frac{43}{20} = \frac{453}{200} \times \frac{3}{\sqrt{10}}$ Accept mixed numbers for fractions such as $\frac{453}{200}$

A1 Accept $\sqrt{10} = \frac{1359}{430} = 3\frac{69}{430}$ or by using the rationalised form $\sqrt{10} = \frac{4300}{1359} = 3\frac{223}{1359}$

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Past Paper (Mark Scheme)

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Question Number	Scheme	Marks
6(i)	$x = \tan^2 4y \Rightarrow \frac{dx}{dy} = 8\tan 4y \sec^2 4y$ oe	M1A1
	$\frac{dy}{dx} = \frac{1}{8\tan 4y \sec^2 4y}, = \frac{1}{8\tan 4y(1+\tan^2 4y)} = \frac{1}{8\sqrt{x}(1+x)} = \frac{1}{8(x^{0.5} + x^{1.5})}$	M1,M1A1
	$\mathrm{d}V$, and $\mathrm{d}V$, a	(5)
(ii)	$\frac{\mathrm{d}V}{\mathrm{d}t} = 2, V = x^3 \Rightarrow \frac{\mathrm{d}V}{\mathrm{d}x} = 3x^2$	B1,B1
	Uses $\frac{\mathrm{d}V}{\mathrm{d}t} = \frac{\mathrm{d}V}{\mathrm{d}x} \times \frac{\mathrm{d}x}{\mathrm{d}t}$	M1
	$\frac{dx}{dt}\Big _{x=4} = \frac{2}{3x^2} = \frac{1}{24} (\text{cm s}^{-1})$	M1A1
		(5) (10 marks)

(i)

M1 Differentiates $\tan^2 4y$ to get an expression equivalent to the form $C\tan 4y \sec^2 4y$ You may see $\tan 4y \times A \sec^2 4y + \tan 4y \times B \sec^2 4y$ from the product rule or versions appearing from $\sqrt{x} = \tan 4y \Rightarrow Ax^{-0.5} \times ... = B\sec^2 4y$ or $Ax^{-0.5} = B\sec^2 4y \times ... \quad x = \frac{\sin^2 4y}{\cos^2 4y} \Rightarrow \frac{dx}{dy} = \frac{\cos^2 4y \times A \sin 4y \cos 4y - \sin^2 4y \times B \cos 4y \sin 4y}{\left(\cos^2 4y\right)^2}$

from the quotient rule

- A1 Any fully correct answer, or equivalent, including the left hand side. $\frac{dx}{dy} = 2\tan 4y \times 4\sec^2 4y$ Also accept the equivalent by implicit differentiation $1 = 8\tan 4y\sec^2 4y\frac{dy}{dx}$
- M1 Uses $\frac{dy}{dx} = 1 / \frac{dx}{dy}$ Follow through on their $\frac{dx}{dy}$.

 Condone issues with reciprocating the '8' but not the trigonometrical terms.

Condone issues with reciprocating the '8' but not the trigonometrical term. If implicit differentiation is used it is scored for writing $\frac{dy}{dx}$ as the subject.

- Uses $\sec^2 4y = 1 + \tan^2 4y$ where $x = \tan^2 4y$ to get their expression for $\frac{dy}{dx}$ or $\frac{dx}{dy}$ in terms of just x. If they use other functions it is for using $\sin^2 4y = \frac{x}{1+x}$ and $\cos^2 4y = \frac{1}{1+x}$ where $x = \tan^2 4y$ to get their expression for $\frac{dy}{dx}$ or $\frac{dx}{dy}$ in terms of just x.
- A1 Correct answer and solution. Accept $\frac{1}{8(x^{0.5} + x^{1.5})}, \frac{1}{8(x^{\frac{1}{2}} + x^{\frac{3}{2}})}$ or A = 8, p = 0.5 and q = 1.5

Candidates do not have to explicitly state the values of A, p and q. Remember to isw after the sight of an acceptable answer.

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Alt (i) using
$$y = \frac{1}{4} \arctan\left(\sqrt{x}\right) \Rightarrow \frac{dy}{dx} = \frac{1}{4} \left(\frac{1}{1 + \left(\sqrt{x}\right)^2}\right) \times \frac{1}{2} x^{-\frac{1}{2}}$$

M1 Changes the subject of the formula to get $y = D\arctan(\sqrt{x})$ and proceeds to $\frac{dy}{dx} = \left(\frac{1}{1 + (\sqrt{x})^2}\right) \times ...$

A1 Achieves
$$y = \frac{1}{4}\arctan(\sqrt{x})$$
 and proceeds to $\frac{dy}{dx} = \left(\frac{1}{1+(\sqrt{x})^2}\right) \times ...$

M1 Correctly proceeds to
$$\frac{dy}{dx} = E\left(\frac{1}{1+(\sqrt{x})^2}\right) \times x^{-\frac{1}{2}}$$

M1 Writes
$$x^{-\frac{1}{2}} = \frac{1}{\sqrt{x}}$$
 and multiplies out bracket to get $\frac{dy}{dx} = E\left(\frac{1}{\frac{1}{x^2} + x^2}\right)$

A1 Correct answer and solution. Accept
$$\frac{1}{8(x^{0.5}+x^{1.5})}$$
, $\frac{1}{8(x^{\frac{1}{2}}+x^{\frac{3}{2}})}$

(ii)

States or uses $\frac{dV}{dt} = 2$. It may be awarded if embedded within the chain rule and assigned to $\frac{dV}{dt}$

States or uses $\frac{dV}{dx} = 3x^2$. It may be awarded if embedded within the chain rule and assigned

to
$$\frac{dV}{dx}$$
 You may also see $x = V^{\frac{1}{3}} \Rightarrow \frac{dx}{dV} = \frac{1}{3}V^{-\frac{2}{3}}$

Accept any variable, for example s, l, a in place of x.

Uses a correct chain rule, eg. $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt}$ with $\frac{dV}{dt} = 2$ and their value of $\frac{dV}{dx}$ OR $\frac{dx}{dV}$ You may see different versions of this. Eg. $\frac{dV}{dx} = \frac{dV}{dt} \div \frac{dx}{dt}$

M1 Substitutes x=4 into their chain rule to find a numerical value for $\frac{dx}{dt} = ...$

Accept a substitution of $V = 64 \Rightarrow \frac{dx}{dV} = \frac{1}{3}V^{-\frac{2}{3}}$ to find a numerical value for $\frac{dx}{dt} = ...$

Condone poor notation for $\frac{dx}{dt}$ and the appearance of an answer from the substitution of x = 4 into an incorrect chain rule expression will be sufficient to award this mark.

A1 cso $\frac{dx}{dt}\Big|_{x=4} = \frac{1}{24} \left(\text{cm s}^{-1}\right)$. Accept awrt 0.0417

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Mathematics C34

Question Number	Scheme	Marks
7(a)	$2\cos(x+30)^{\circ} = \sin(x-30)^{\circ}$	3.61.4.1
	$2(\cos x^{\circ} \cos 30^{\circ} - \sin x^{\circ} \sin 30^{\circ}) = \sin x^{\circ} \cos 30^{\circ} - \cos x^{\circ} \sin 30^{\circ}$ $2\cos 30^{\circ} - 2\tan x^{\circ} \sin 30^{\circ} = \tan x^{\circ} \cos 30^{\circ} - \sin 30^{\circ}$	M1A1
	$\sin 30^{\circ} = \frac{1}{2}, \cos 30^{\circ} = \frac{\sqrt{3}}{2}$	B1
	$\tan x^{\circ} = \frac{2\sqrt{3} + 1}{\sqrt{3} + 2} \Rightarrow \times \frac{\sqrt{3} - 2}{\sqrt{3} - 2} \Rightarrow \tan x^{\circ} = 3\sqrt{3} - 4$	dM1A1*
		(5)
(b)	$\tan(2\theta+10)^\circ=3\sqrt{3}-4$	M1
	2θ +10=50.1,(230.1) \Rightarrow θ =	dM1
	$\theta = 20.1, 110.1$	A1,A1
		(4)
		(9 marks)

(a)

- M1 Uses identities for cos(A + B) and sin(A B) with A = x, B = 30.
 - Condone missing bracket and incorrect signs but the terms must be correct.
- A1 Fully correct equation in sinx and cosx
- B1 Replaces $\sin 30$ by $\frac{1}{2}$ and $\cos 30$ by $\frac{\sqrt{3}}{2}$ throughout their expanded equation.
 - If candidate divides by cos30 it will be for $\tan 30 = \frac{\sqrt{3}}{3}$ or equivalent
- dM1 Either for collecting terms in $\sin x$ and $\cos x$ to reach $(...) \sin x = (...) \cos x$, before then dividing by $\cos x$ to reach $\frac{\sin x}{\cos x} = \frac{(...)}{(...)}$ or $\tan x = \frac{(...)}{(...)}$.

Alternatively, by dividing by $\cos x$ first, producing an equation in $\tan x$, then collecting terms reaching $\tan x = \frac{(...)}{(...)}$

An intermediate line must be seen. $(\sqrt{3} + 2) \tan x^\circ = 2\sqrt{3} + 1 \Rightarrow \tan x^\circ = 3\sqrt{3} - 4$ is dM0 Similarly $(\sqrt{3} + 2) \sin x^\circ = (2\sqrt{3} + 1) \cos x \Rightarrow \tan x^\circ = 3\sqrt{3} - 4$ is dM0

A1* Reaches final answer by showing rationalisation with no errors.

Accept as a minimium
$$\tan x^\circ = \frac{2\sqrt{3}+1}{\sqrt{3}+2} \times \frac{\sqrt{3}-2}{\sqrt{3}-2} \Rightarrow \tan x^\circ = 3\sqrt{3}-4$$

(b)

- M1 For using part (a) to produce (or imply) an equation $\tan(2\theta \pm \alpha)^{\circ} = 3\sqrt{3} 4$ Condone $\alpha = 0$ and θ being replaced by x.
- dM1 Dependent upon the previous M. Score for an attempt at the correct method to find one value of θ Look for $\tan(2\theta \pm \alpha)^{\circ} = 3\sqrt{3} - 4 \Rightarrow \theta = \frac{\operatorname{invtan}(3\sqrt{3} - 4) \pm \alpha}{2}$
- A1 One correct answer awrt 1dp $\theta = 20.1$ or 110.1
- A1 Both $\theta = 20.1$ and 110.1 awrt 1dp and no other solutions within the given range. Ignore extra solutions outside the given range.

An otherwise case for students starting again in part (b).

M1 Expands both sides (see part a) using correct identities, divides by $\cos 2\theta$ and proceeds to an equation of the form $\tan 2\theta = ...$

Note that the correct answer is $\tan 2\theta = \frac{2\cos 40 + \sin 20}{2\sin 40 + \cos 20} (= 0.84219)$

dM1 Uses correct order of operations from $\tan 2\theta = ... \Rightarrow \theta = \frac{1}{2} \arctan...$ to find at least one solution

A1A1 Follows

Correct answers without working scores B1, B1

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Question Number	Scheme	Marks
8 (a)	$1000 < V \le 23000$	B1,B1 (2)
(b)	$\frac{dV}{dt} = 18000 \times -0.2e^{-0.2t} + 4000 \times -0.1e^{-0.1t}$	M1
	$\left \frac{dV}{dt} \right _{t=10} = 18000 \times -0.2e^{-2} + 4000 \times -0.1e^{-1} = \text{awrt}(-)634$	M1A1
(c)	$15000 = 18000e^{-0.2t} + 4000e^{-0.1t} + 1000$	(3)
(-)		
	$0 = (9e^{-0.1t} - 7)(e^{-0.1t} + 1)$	M1A1
	$0 = 9e^{-0.2t} + 2e^{-0.1t} - 7$ $0 = (9e^{-0.1t} - 7)(e^{-0.1t} + 1)$ $9e^{-0.1t} = 7 \Rightarrow t = 10\ln\left(\frac{9}{7}\right) \text{ oe}$	dM1A1
		(4) (9 marks)

(a)

B1 Accept either boundary: V < 23000 or $V \le 23000$ or $V_{\text{max}} = 23000$ for the upper boundary and V > 1000 or $V \ge 1000$ or $V_{\text{min}} = 1000$ for the lower boundary. Answers like $V \ge 23000$ are B0

B1 Completely correct solution.

Accept $1000 < V \le 23000$, 1000 < Range or $y \le 23000$, (1000,23000], V > 1000 and $V \le 23000$

(b)

M1 Score for a $\frac{dV}{dt} = Ae^{-0.2t} + Be^{-0.1t}$, where $A \neq 18000$, $B \neq 4000$

M1 Sub t = 10 into a $\frac{dV}{dt}$ of the form $Ae^{-0.2t} + Be^{-0.1t}$ where $A \neq 18000$, $B \neq 4000$

Condone substitution of t = 10 into a $\frac{dV}{dt}$ of the form $Ae^{-0.2t} + Be^{-0.1t} + 1000$ $A \neq 18000$, $B \neq 4000$

A1 Correct solution and answer only. Accept ± 634 following correct $\frac{dV}{dt} = -3600e^{-0.2t} - 400e^{-0.1t}$

Watch for students who sub t = 10 into their V first and then differentiate. This is 0,0,0.

Watch for students who achieve +634 following $\frac{dV}{dt} = 3600e^{-0.2t} + 400e^{-0.1t}$. This is 1,1,0

A correct answer with no working can score all marks.

(c)

M1 Setting up 3TQ in $e^{\pm 0.1t}$ AND correct attempt to factorise or solve by the formula. For this to be scored the $e^{\pm 0.2t}$ term must be the x^2 term.

A1 Correct factors $(9e^{-0.1t} - 7)(e^{-0.1t} + 1)$ or $(7e^{0.1t} - 9)(e^{0.1t} + 1)$ or a root $e^{-0.1t} = \frac{7}{9}$

dM1 Dependent upon the previous M1.

This is scored for setting the $ae^{\pm 0.1t} - b = 0$ and proceeding using correct ln work to t = ...

A1 $t = 10\ln\left(\frac{9}{7}\right)$. Accept alternatives such as $t = \frac{1}{0.1}\ln\left(\frac{9}{7}\right), \frac{1}{-0.1}\ln\left(\frac{7}{9}\right), -10\ln\left(\frac{7}{9}\right)$

If any extra solutions are given withhold this mark.

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Past Paper (Mark Scheme)

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WMA02

Question Number	Scheme	Marks	
9 (a)	$\frac{dx}{dt} = \frac{1}{t+2} , \text{Area of R} = \int y dx = \int \frac{4}{t^2} \times \frac{1}{(t+2)} (dt)$	B1, M1	
	Correct proof with limits and no errors Area = $\int_{1}^{3} \frac{4}{t^{2}(t+2)} dt$	A1*)
(b)	$\frac{4}{t^2(t+2)} = \frac{A}{t} + \frac{B}{t^2} + \frac{C}{(t+2)} \text{ or } \frac{4}{t^2(t+2)} = \frac{A}{t^2} + \frac{B}{(t+2)}$	B1	,
	$4 = At(t+2) + B(t+2) + Ct^{2}$ Sub $t = 0 \Rightarrow B = 2$ Sub $t = -2 \Rightarrow C = 1$		
	Compare t^2 $A+C=0 \Rightarrow A=-1$	M1A1	
	$\int_{1}^{3} \frac{4}{t^{2}(t+2)} dt = \int_{1}^{3} \frac{-1}{t} + \frac{2}{t^{2}} + \frac{1}{(t+2)} dt = \left[-\ln t - \frac{2}{t} + \ln(t+2) \right]_{1}^{3}$	M1A1	
	$= \left(-\ln 3 - \frac{2}{3} + \ln 5\right) - \left(-\ln 1 - \frac{2}{1} + \ln 3\right)$		
	$= \ln\left(\frac{5}{9}\right) + \frac{4}{3}$	dM1A1	
(c)	4	(7)
(0)	Sub $t = e^x - 2$ into $y = \frac{4}{t^2} \Rightarrow y = \frac{4}{(e^x - 2)^2}$, $(x > \ln 2)$	M1A1	
		(2)
		(12 marks)	

(a)

B1 States or implies $\frac{dx}{dt} = \frac{1}{t+2}$. Accept $dx = \frac{1}{t+2}dt$

You may award this if embedded within an integral **before the final answer** is given

For example accept Area =
$$\int y \, dx = \int_{1}^{3} \frac{4}{t^{2}} \times \frac{1}{t+2} dt$$

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M1 States and uses Area = $\int y \, dx$ with the y, the dx and the $\int sign$ and replaces both y and dx by functions of t.

Alternatively states and uses Area = $\int y \frac{dx}{dt} (dt)$ with the y, the $\frac{dx}{dt}$ and the \int sign and replaces

both y and $\frac{dx}{dt}$ by functions of t. There is no need for limits and you can award even if there is a lack of a dt

A1* Correct proof with no errors or omissions **on any line for the integrand** and there must be a d*t* in all integrals in *t*. The limits need only be correct on the final line and they may have just been written in. The two separate fractions must be combined into a single fraction

(b)
B1 Scored for use of partial fractions. Accept the correct form $\left(\frac{4}{t^2(t+2)}\right) = \frac{A}{t} + \frac{B}{t^2} + \frac{C}{(t+2)}$ but also award for the form $\left(\frac{4}{t^2(t+2)}\right) = \frac{A}{t^2} + \frac{B}{(t+2)}$

M1 Substitute values of t and/or use inspection to determine A, B and C from a form equivalent to $4 = At(t+2) + B(t+2) + Ct^2$. The partial fraction must be of the correct form

A1 For $\frac{4}{t^2(t+2)} = \frac{-1}{t} + \frac{2}{t^2} + \frac{1}{(t+2)}$.

M1 $\int \frac{A}{t^2} + \frac{C}{(t+2)} dt = \frac{..}{t} + .. \ln(t+2)$

Note this can be scored from an incorrect assumption that $\frac{4}{t^2(t+2)} = \frac{A}{t^2} + \frac{B}{(t+2)}$

A1 $\int \frac{4}{t^2(t+2)} dt = \left[-\ln t - \frac{2}{t} + \ln(t+2) + (c) \right]$ There is no need to consider limits.

dM1 Dependent upon previous M. Sub in limits, subtracts either way around **and** uses a correct log law at least once to get expression of the form $a + \ln b$.

A1 Correct solution only = $\ln\left(\frac{5}{9}\right) + \frac{4}{3}$

(c)
M1 Rearranges $x = \ln(t+2)$ to reach $t = e^x \pm 2$ and sub in $y = \frac{4}{t^2}$ to get y in terms of x

Alternatively substitutes $t = \sqrt{\frac{4}{y}}$ or equivalent into $x = \ln(t+2)$ and attempts to rearrange to y = ...

A1 $y = \frac{4}{\left(e^x - 2\right)^2}$. Remember to isw.

You can ignore any reference to the domain, $x > \ln 2$, for this mark.

Mathematics C34 WMA02

Past Paper (Mark Scheme)

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Question Number	Scheme	Marks
10(a)	$y = \frac{x^2 \ln x}{3} - 2x + 4 \Rightarrow \frac{dy}{dx} = \underbrace{\frac{2x \ln x}{3} + \frac{x^2}{3x}}_{,-2}, -2$	M1A1, B1
	$\frac{2x\ln x}{3} + \frac{x^2}{3x} - 2 = 0 \Rightarrow x(2\ln x + 1) = 6 \Rightarrow x =$ $\Rightarrow x = \frac{6}{1 + \ln x^2}$	dM1
	$\Rightarrow x = \frac{6}{1 + \ln x^2}$	A1*
		(5)
(b)	$x_1 = \frac{6}{1 + \ln(2.27^2)} = \text{awrt } 2.273$	M1A1
	$x_2 = \text{awrt } 2.271 \text{ and } x_3 = \text{awrt } 2.273$	A1 (3)
(c)	A= (2.3, 0.9)	M1 A1 (2)
		(10 marks)

Past Paper (Mark Scheme)

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(a)

Applying the product rule to $x^2 \ln x$ or multiples of it such as $\frac{x^2 \ln x}{3}$ and even $\frac{x^2}{3} \times \frac{\ln x}{3}$ If the rule is quoted it must be correct. It may be implied by, for example, $u = \frac{x^2}{3}, v = \ln x, u' = ..., v' = ... \text{ followed by their } vu' + uv'$

If it is not quoted nor implied only accept expressions of the form $Ax \ln x + Bx^2 \times \frac{1}{x}$

- A1 A correct (unsimplified) derivative for $\frac{x^2 \ln x}{3} \rightarrow \frac{2x \ln x}{3} + \frac{x^2}{3x}$
- B1 The derivative of the -2x+4 term is seen or implied to be -2
- dM1 Dependent upon the previous M being scored. It is for setting their $\frac{dy}{dx} = 0$, taking out a common factor of x and proceeding to x=.. Alternatively they could state that $\frac{dy}{dx} = 0$ and write out a line from their derivative equivalent to $\frac{2x \ln x}{3} + \frac{x^2}{3x} = 2$
- A1* Correct solution only $x = \frac{6}{1 + \ln x^2}$. Note that this is a given answer. All aspects need to be correct. $2 \ln x + 1 \Rightarrow \ln x^2 + 1$ may just be stated

Note: If the candidate multiplies by 3 to get $3y = x^2 \ln x - 6x + 12 \Rightarrow 3 \frac{dy}{dx} = 2x \ln x + x - 6$ before setting $\frac{dy}{dx} = 0$ they can score all marks if they proceed to the given answer.

If they multiply by 3 and leave the subject as y (or perhaps ignore the lhs) they can score a special case $1 \ 0 \ 1 \ 1 \ 0$ for $2x \ln x + x - 6 = 0 \Rightarrow x(2 \ln x + 1) = 6 \Rightarrow x = \frac{6}{(2 \ln x + 1)} \Rightarrow x = \frac{6}{(\ln x^2 + 1)}$

(b)

- M1 Attempts $\frac{6}{1 + \ln 2.27^2}$. Awrt 2.273 implies this method
- A1 $x_1 = \text{awrt } 2.273$. The subscript is not important. Mark as the first value given.
- A1 $x_2 = \text{awrt } 2.271(3\text{dp}) \text{ and } x_3 = \text{awrt } 2.273(3\text{dp})$

(c)

- M1 Deduces the *x* coordinate of *A* is 2.3. The sight of 2.3 is sufficient to award this as long as their values in (b) round to this.

 Alternatively uses their (rounded) answer from part (b) and substitutes it into equation for *y* to find the *y* coordinate of *A*. In a similar way to that of the *x* coordinate, the sight of 0.9 would be sufficient evidence for this award.
- A1 (2.3, 0.9). Accept x = 2.3, y = 0.9

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Question Number	Scheme	Marks
11 (a)	$\begin{pmatrix} -2\\1\\4 \end{pmatrix} \cdot \begin{pmatrix} q\\2\\1 \end{pmatrix} = -2 \times q + 1 \times 2 + 4 \times 1 = 0 \Rightarrow q = 3$	M1A1*
(b)	Equate the <i>y</i> and <i>z</i> coordinates	(2)
(1)	Equate the y and 2 coordinates $\begin{pmatrix} 14 \\ -6 \\ -13 \end{pmatrix} + \lambda \begin{pmatrix} -2 \\ 1 \\ 4 \end{pmatrix} = \begin{pmatrix} p \\ -7 \\ 4 \end{pmatrix} + \mu \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix} \Rightarrow -6 + 1\lambda = -7 + 2\mu$ $-13 + 4\lambda = 4 + 1\mu$	M1
	Full method to find either λ or μ	dM1
	(2) $\Rightarrow \lambda = -1 + 2\mu$ subbed into (3) $-13 + 8\mu - 4 = 4 + \mu \Rightarrow \mu = 3$ Sub $\mu = 3$ into (2) $\Rightarrow -6 + 1\lambda = -7 + 2 \times 3 \Rightarrow \lambda = 5$ Sub values back into x coordinates $14 - 2 \times 5 = p + 3 \times 3 \Rightarrow p = -5$	A1either ddM1 A1
		(5)
(c)	Point of intersection is $\begin{pmatrix} 14 \\ -6 \\ -13 \end{pmatrix} + 5 \begin{pmatrix} -2 \\ 1 \\ 4 \end{pmatrix}$ OR $\begin{pmatrix} '-5' \\ -7 \\ 4 \end{pmatrix} + 3 \times \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix} = (4, -1, 7)$	M1,A1
		(2)
(d)	$ \overrightarrow{AX} = \begin{pmatrix} -2\\1\\4 \end{pmatrix} \qquad \overrightarrow{OB} = \overrightarrow{OA} \pm 2\overrightarrow{AX} = \begin{pmatrix} 6\\-2\\3 \end{pmatrix} \pm 2 \times \begin{pmatrix} -2\\1\\4 \end{pmatrix} $	M1 either
	$\overline{OB} = \begin{pmatrix} 2\\0\\11 \end{pmatrix} \overline{OB} = \begin{pmatrix} 10\\-4\\-5 \end{pmatrix}$	A1A1
		(3) (12 marks)

(a)

M1 Attempts to find a solution for q by setting the scalar product of the direction vectors = 0 Condone one sign error in $-2 \times q + 1 \times 2 + 4 \times 1 = 0$ leading to q = ...

Alternatively set q = 3 and attempt the scalar product

A1* q = 3. This is a given answer.

In the alternative, there must be a statement (=0) and a conclusion, (hence true/hence perpendicular)

- M1 Equate y and z coordinates. Condone sign errors
- dM1 Dependent upon the previous M. Scored for a full method to find either λ or μ
- A1 Either $\lambda = 5$ or $\mu = 3$
- ddM1 Dependent upon both previous M's.

Either uses both of their values for λ and μ in the equation for the x coordinates in order to find a numerical value for p. Condone sign slips. Look for $14 - 2\lambda = p + 3\mu$ with their λ and μ leading to a solution of p.

Alternatively uses the value of one variable, expresses the other variable in terms of this and substitutes both in the equation for the x coordinates in order to find a numerical value for p.

- A1 p = -5
- (c)
- M1 Uses their value of λ in h, or their values of μ , p and q in l_2 to find the coordinate of X
- A1 Coordinates of X = (4, -1, 7). Accept in vector form $\overrightarrow{OX} = \begin{pmatrix} 4 \\ -1 \\ 7 \end{pmatrix}$
- (d)

M1 Uses either
$$\overline{OB} = \overline{OA} \pm 2\overline{AX}$$
 $\overline{AX} = \pm \begin{pmatrix} 6 - 4' \\ -2 - 1' \\ 3 - 7' \end{pmatrix}$ with an attempt to find one possible value of

vector B

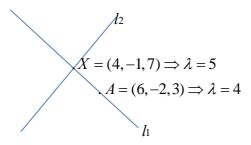
Or uses mid points. Sight of (a,b,c) appearing from solving $\frac{6+a}{2}=4, \frac{-2+b}{2}=-1, \frac{3+c}{2}=7$

Or attempts to find the value of one value of λ and uses it correctly to find one position of *B* You may see $|\lambda_B - \lambda_A| = 2 \times |\lambda_A - \lambda_X|$ or a version of

$$\sqrt{(14-2\lambda-6)^2+(-6+\lambda+2)^2+(-13+4\lambda-3)^2}=2\times\sqrt{(6-4)^2+(-2-4)^2+(3-7)^2}\Rightarrow \lambda=..$$

followed by λ being substituted into line l_1

A more simple version of this could be using a diagram and deducing that $\lambda = 2$ or 6 followed by λ being substituted into line l_1



- A1 Gives one possible vector $\overline{OB} = \begin{pmatrix} 2 \\ 0 \\ 11 \end{pmatrix} = (2i+11k) \text{ or } \overline{OB} = \begin{pmatrix} 10 \\ -4 \\ -5 \end{pmatrix} = 10i-4j-5k$
- A1 Gives both possible position vectors or coordinates

(13 marks)

Past Paper (Mark Scheme)

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Question Number	Scheme	Marks	
12(a)	0.9242 exactly	B1	<i>(</i> 4)
(b)	Strip width =0.5	B1	(1)
	Area $\approx \frac{0.5}{2} ((2+1.2958+2\times(1.3041+'0.9242'+0.9089)))$	M1	
	=2.393	A1	
			(3)
(c)	$\int \frac{x^2 \ln x}{3} - 2x + 4 \mathrm{d}x$		
	$= \frac{x^3}{9} \ln x - \int \frac{x^3}{9} \times \frac{1}{x} dx, -x^2 + 4x$	M1A1, B1	
	$= \frac{x^3}{9} \ln x - \frac{x^3}{27} \left(-x^2 + 4x \right)$	A1	
	Area = $\left[\frac{x^3}{9}\ln x - \frac{x^3}{27} - x^2 + 4x\right]_1^3 = (3\ln 3 - 1 - 9 + 12) - \left(-\frac{1}{27} - 1 + 4\right)$	dM1	
	$= \ln 27 - \frac{26}{27}$	A1	
	21		(6)
(d)	% error = $\pm \frac{ real - approx }{real} \times 100 = \text{Accept awrt } \pm 2.6\%$	M1A1	
(e)	Increase the number of 'strips'	B1	(2)
	mercase are number of surps	(12)	(1)

(a) B1 0.9242 exactly either in the table or within the trapezium rule in part (b)

(b) B1 Uses a strip width of 0.5 or equivalent.

M1 Uses the correct form of the trapezium rule, a form of which appears in the formula booklet.

Look for
$$\frac{\dots}{2} ((2+1.2958+2\times(1.3041+\text{their }0.9242+0.9089)))$$

Accept for this the sum of four trapezia

A1 Awrt 2.393 (3dp)

Past Paper (Mark Scheme)

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- (c)
- M1 Uses integration by parts, the correct way around.

Accept integration on either $x^2 \ln x$ or multiples like $\frac{x^2 \ln x}{3}$ or even $\frac{x^2}{3} \times \frac{\ln x}{3}$

Accept as evidence an expression of the form $px^3 \ln x - \int \frac{qx^3}{x} (dx)$

- A1 Using integration by parts to arrive at an intermediate form $\frac{x^3}{k} \ln x \int \frac{x^3}{k} \times \frac{1}{x} (dx)$ where k most likely will be a multiple of 3.
- B1 Integrates the -2x+4 to $-x^2+4x+(c)$. Ignore any constants. Watch for candidates who take out a common factor $\frac{1}{3}(...-6x+12)$ to $\frac{1}{3}(...-3x^2+12x+(c))$
- A1 The correct integral for $\frac{x^2 \ln x}{3}$ Accept equivalent expressions to $\frac{x^3}{9} \ln x \frac{x^3}{27} + (c)$ This is independent of the integral for the -2x + 4 term.
- dM1 Dependent upon the M mark it is for substituting in both x=3 and x=1 and subtracting (either way around).
- A1 Correct solution only = $\ln 27 \frac{26}{27}$. The answer must be in this form and $3 \ln 3 \rightarrow \ln 27$
- (d)
 M1 Uses their answer obtained by integration in part c and their answer obtained by the trapezium rule in part b and calculates $\pm \frac{|c-b|}{a}$
- A1 Accept awrt $\pm 2.6\%$.
- (e)
 B1 Makes a reference to increasing the number of strips. Accept decrease the width of the strips, use more trapezia Be generous with statements like more values or strips as the intention is clear. Also accept more x's, more y's but don't accept use more decimal places.

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Mathematics	C34
\//	MAAOO

Question Number	Scheme	Marks
13(a)	$R = \sqrt{109}$	B1
	$\tan \alpha = \frac{3}{10} \Rightarrow \alpha = \text{awrt} 16.70^{\circ}$	M1A1
		(3)
(b)(i)	Max height = $12 + \sqrt{109} = 22.44 \text{ m}$	M1A1
(ii)	Occurs when $30t + 16.70' = 180 \Rightarrow t = 5.44$	M1A1
	6	(4)
(c)	$18 = 12 - \sqrt{109}\cos(30t + 16.70) \Rightarrow \cos(30t + 16.70) = -\frac{6}{\sqrt{109}} (-0.57)$	M1A1
	$\Rightarrow 30t + 16.70 = \arccos\left(-\frac{6}{\sqrt{109}}\right) \Rightarrow t =$	dM1
	t = awrt 3.61(2dp)	A1 (4)
(d)	Attempting $30t = 360 \Rightarrow t =$ or $30t = 720 \Rightarrow t =$ 2 revolutions in 24 minutes	M1 A1
		(13 marks) (2)

Past Paper (Mark Scheme)

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(a)

- Accept $R = \pm \sqrt{109}$. Remember to isw after a correct answer. Eg $R = \sqrt{109} = 10...$
- M1 For $\tan \alpha = \pm \frac{3}{10}$ or $\tan \alpha = \pm \frac{10}{3}$. If R is used to find α , only accept $\cos \alpha = \pm \frac{10}{R}$ or $\sin \alpha = \pm \frac{3}{R}$
- A1 $\alpha = \operatorname{awrt} 16.70^{\circ} \text{ (2dp)}$. Condone $\alpha = 16.7^{\circ}$ Note that the answer of $\alpha = \operatorname{awrt} 0.29 \text{ radians scores A0}$.

(b)(i)

- M1 For 12 +their R
- A1 Awrt 22.44 m. Accept $12 + \sqrt{109}$

(b) (ii)

- M1 For arriving at a solution for t from $30t \pm '16.70' = 180 \Rightarrow t = ..$ If radians were used in part a then accept $30t \pm '0.29' = \pi \Rightarrow t = ..$
- A1 t = awrt 5.44 only.

If multiple solutions are found, 5.44 must be referred to as their 'chosen' solution

.....

Answers from calculus will be rare. They can be scored as follows.

From the original function:

For (b)(ii) M1
$$\frac{dH}{dt} = 0 \rightarrow 30t = 180 - \arctan\left(\frac{3}{10}\right) \Rightarrow t = ...$$
 A1 $t = \text{awrt } 5.44 \text{ only}$

(b)(i) M1 Sub their
$$t = \text{awrt } 5.44 \text{ obtained from } \frac{dH}{dt} = 0$$
 A1 Awrt 22.44 m

From the adapted function:

For (b)(ii) M1
$$\frac{dH}{dt} = 0 \rightarrow (30t + '16.70') = 180 \Rightarrow t = ..$$
 A1 $t = \text{awrt } 5.44 \text{ only}$

(b)(i) M1 Sub their
$$t = \text{awrt } 5.44 \text{ obtained from } \frac{dH}{dt} = 0$$
 A1 Awrt 22.44 m

.....

(c)

- M1 Attempts to substitute H = 18 into $H = 12 10\cos 30t + 3\sin 30t$ and use their answer to part (a) to proceed to $\cos(30t \pm their'16.70') = ...$
- A1 $\cos(30t + their'16.70') = -\frac{6}{\sqrt{109}}$ or awrt -0.57. It may be implied by $30t + '16.70' = awrt125^\circ$
- dM1 Dependent upon previous M. Score for $cos(30t \pm '16.70') = -... \Rightarrow t = ...$

The cos(..) must be negative, the order of operations must be seen to be correct with the 'invcos' being attempted first and the second quadrant must be chosen for their calculation.

A1 t = 3.61.

The answer with no incorrect working scores all 4 marks.

If multiple solutions are found, 3.61 must be referred to as their 'chosen' solution

(d)

- M1 Attempting $30t = 360 \Rightarrow t = ...$ or $30t = 720 \Rightarrow t = ...$
- A1 24 minutes. **Both** 24 **and** minutes are required.

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