



# Mark Scheme (Results)

January 2014

Pearson Edexcel International  
Advanced Level  
Core Mathematics C34 (WMA02/01)

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

**EDEXCEL GCE MATHEMATICS****General Instructions for Marking**

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.
3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod – benefit of doubt
  - ft – follow through
  - the symbol  $\surd$  will be used for correct ft
  - cao – correct answer only
  - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
  - isw – ignore subsequent working
  - awrt – answers which round to
  - SC: special case
  - oe – or equivalent (and appropriate)
  - dep – dependent
  - indep – independent
  - dp decimal places
  - sf significant figures
  - \* The answer is printed on the paper
  - $\square$  The second mark is dependent on gaining the first mark
4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
  5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
  6. If a candidate makes more than one attempt at any question:
    - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
    - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
  7. Ignore wrong working or incorrect statements following a correct answer.

## General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

### Method mark for solving 3 term quadratic:

#### 1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q), \text{ where } |pq| = |c|, \text{ leading to } x = \dots$$

$$(ax^2 + bx + c) = (mx + p)(nx + q), \text{ where } |pq| = |c| \text{ and } |mn| = |a|, \text{ leading to } x = \dots$$

#### 2. Formula

Attempt to use the correct formula (with values for  $a$ ,  $b$  and  $c$ ).

#### 3. Completing the square

$$\text{Solving } x^2 + bx + c = 0: \left(x \pm \frac{b}{2}\right)^2 \pm q \pm c = 0, \quad q \neq 0, \quad \text{leading to } x = \dots$$

### Method marks for differentiation and integration:

#### 1. Differentiation

Power of at least one term decreased by 1. ( $x^n \rightarrow x^{n-1}$ )

#### 2. Integration

Power of at least one term increased by 1. ( $x^n \rightarrow x^{n+1}$ )

### Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

### Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

### Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

Question Number	Scheme	Marks
1.	$f(x) = \frac{2x}{x^2 + 3} \Rightarrow f'(x) = \frac{(x^2 + 3)2 - 2x \times 2x}{(x^2 + 3)^2} = \left( \frac{6 - 2x^2}{(x^2 + 3)^2} \right)$ $f'(x) > 0 \Rightarrow \frac{6 - 2x^2}{(x^2 + 3)^2} > 0$ <p>Critical values <math>6 - 2x^2 = 0 \Rightarrow x = \pm\sqrt{3}</math></p> <p>Inside region chosen <math>-\sqrt{3} &lt; x &lt; \sqrt{3}</math></p>	<p>M1A1</p> <p>M1A1</p> <p>dM1A1</p> <p><b>(6 marks)</b></p>

**Notes**

- M1 Applies the Quotient rule, a form of which appears in the formula book, to  $\frac{2x}{x^2 + 3}$   
 If the formula is quoted it must be correct. There must have been some attempt to differentiate both terms.  
 If the rule is not quoted nor implied by their working, meaning that terms are written out  
 $u = 2x, v = x^2 + 3, u' = \dots, v' = \dots$  followed by their  $\frac{vu' - uv'}{v^2}$ , then only accept answers of the form  
 $\frac{(x^2 + 3)A - 2x \times Bx}{(x^2 + 3)^2} \quad A, B > 0$ . Condone invisible brackets for the M.  
 Alternatively applies the product rule with  $u = 2x, v = (x^2 + 3)^{-1}$   
 If the formula is quoted it must be correct. There must have been some attempt to differentiate both terms.  
 If the rule is not quoted nor implied by their working, meaning that terms are written out  
 $u = 2x, v = (x^2 + 3)^{-1}, u' = \dots, v' = \dots$  followed by their  $vu' + uv'$ , then only accept answers of the form  
 $(x^2 + 3)^{-1} \times A \pm 2x \times (x^2 + 3)^{-2} \times Bx$ .  
 Condone invisible brackets for the M.
- A1 Any fully correct (unsimplified) form of  $f'(x)$   
 Accept versions of  $f'(x) = \frac{(x^2 + 3)2 - 2x \times 2x}{(x^2 + 3)^2}$  for the quotient rule or  
 Versions of  $f'(x) = (x^2 + 3)^{-1} \times 2 - 2x \times (x^2 + 3)^{-2} \times 2x$  for use of the product rule.
- M1 Setting their numerator of  $f'(x) = 0$  or  $> 0$ , and proceeding to find two critical values.
- A1 Both critical values  $\pm\sqrt{3}$  are found. Accept for this mark expressions like  $x > \pm\sqrt{3}$  and  $\pm 1.73$
- dM1 For choosing the inside region of their critical values.  
 The inequality (if seen) must have been of the correct form. Either  $Ax^2 \dots - B < 0$ ,  $C \dots - Dx^2 > 0$   
 or  $x^2 < C$ . It is dependent upon having set the numerator  $> 0$  or  $= 0$ .
- A1 Correct solution only.  $-\sqrt{3} < x < \sqrt{3}$ . Accept  $(-\sqrt{3}, \sqrt{3})$   $x < \sqrt{3}$  and  $x > -\sqrt{3}$   
 Do not accept  $x < \sqrt{3}$  or  $x > -\sqrt{3}$  or  $-1.73 < x < 1.73$ .  
 Do not accept a correct answer coming from an incorrect inequality. This would be dM0A0.  
 Condone a solution  $x^2 < 3 \Rightarrow x < \pm\sqrt{3} \Rightarrow -\sqrt{3} < x < \sqrt{3}$   
 Do not accept a solution without seeing a correct  $f'(x)$  first. Note that this is a demand of the question.

Question Number	Scheme	Marks
2	$\frac{\tan 2x + \tan 50^\circ}{1 - \tan 2x \tan 50^\circ} = 2 \Rightarrow \tan(2x + 50^\circ) = 2$ $\Rightarrow 2x + 50^\circ = 63.43^\circ, (243.43^\circ, 423.43^\circ)$ $\Rightarrow x = \text{awrt } 6.72^\circ \text{ or } 96.72^\circ \text{ or } 186.72^\circ$ $\Rightarrow 2x + 50^\circ = 243.43^\circ (423.43^\circ) \Rightarrow x = ..$ $x = \text{awrt } 6.72^\circ, 96.72^\circ, 186.72^\circ$	<p>M1A1</p> <p>dM1, A1</p> <p>dM1</p> <p>A1</p> <p><b>(6 marks)</b></p>

Notes

- M1 Uses the compound angle identity  $\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$  to write the equation in the form  $\tan(2x \pm 50^\circ) = 2$ . Accept a sign error in bracket.
- A1  $\tan(2x + 50^\circ) = 2$
- dM1 Uses the correct order of operations to find one solution in the range.  
 Moves from  $\tan(2x \pm 50^\circ) = 2 \Rightarrow 2x \pm 50^\circ = \arctan 2 \Rightarrow x = \dots$   
 This is dependent upon having scored the first M1
- A1 One correct answer, usually awrt  $6.72^\circ$ , but accept any of  $6.72^\circ, 96.72^\circ, 186.72^\circ$
- dM1 Uses the correct order of operations to find a second solution in the range.  
 This can be scored by  $2x \pm 50^\circ = 180 + \text{their } 63 \text{ or } 360 + \text{their } 63 \Rightarrow x = ..$   
 It may be implied by  $90 + \text{their } 6.7$ , or  $180 + \text{their } 6.7$  as long as no incorrect working is seen.  
 This is dependent upon having scored the first M1
- A1 All three answers in the range,  $x = \text{awrt } 6.72^\circ, 96.72^\circ, 186.72^\circ$   
 Any extra solutions in the range withhold the last A mark.  
 Ignore any solutions outside the range  $0 \leq x \leq 270^\circ$   
 Radian solutions will be unlikely, but could be worth marks only if  $50^\circ \rightarrow 0.873$  radians.  
 $\tan(2x + 50^\circ) = 2 \Rightarrow 2x + 50^\circ = 1.107..$  will score M1A1dM0 and nothing else.

Question Number	Scheme	Marks
2(alt 1)	$\frac{\tan 2x + \tan 50^\circ}{1 - \tan 2x \tan 50^\circ} = 2 \Rightarrow \tan 2x + \tan 50^\circ = 2(1 - \tan 2x \tan 50^\circ)$ $\tan 2x = \frac{2 - \tan 50^\circ}{1 + 2 \tan 50^\circ} = (0.239\dots)$ $2x = 13.435^\circ \Rightarrow x = \text{awrt } 6.72^\circ$ $\Rightarrow 2x^\circ = 193.435^\circ (373.435^\circ) \Rightarrow x = ..$ $x = \text{awrt } 6.72^\circ, 96.72^\circ, 186.72^\circ$	<p>M1A1</p> <p>dM1 A1</p> <p>dM1</p> <p>A1</p> <p><b>(6 marks)</b></p>

Notes

- M1 Cross multiplies, collects terms in  $\tan 2x$  and makes  $\tan 2x$  the subject.  
Allow for  $\tan 2x = \dots$
- A1 Accept  $\tan 2x = \frac{2 - \tan 50^\circ}{1 + 2 \tan 50^\circ}$  or the decimal equivalent  $\tan 2x = \text{awrt } 0.239$
- dM1 Correct order of operations to find one solution  $\tan 2x = \dots \Rightarrow 2x = \arctan \dots \Rightarrow x = ..$   
This is dependent upon having scored the first M1
- A1 One correct solution usually awrt  $6.72^\circ$
- dM1 Uses the correct order of operations to find another solution in the range.  
This can be scored by Either  $2x = 180 + \text{their } 13.4$  or  $360 + \text{their } 13.4 \Rightarrow x = ..$   
Or  $90 + \text{their } 6.7$ , or  $180 + \text{their } 6.7$   
This is dependent upon having scored the first M1
- A1 All three answers in the range,  $x = \text{awrt } 6.72^\circ, 96.72^\circ, 186.72^\circ$   
Any extra solutions in the range withhold the last A mark.  
Ignore any solutions outside the range  $0 \leq x \leq 270^\circ$

Question Number	Scheme	Marks
2(alt 2)	<p>Similar to alt 1 but additionally uses <math>\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}</math></p> $(2 - \tan 50) \tan^2 x + (2 + 4 \tan 50) \tan x + (\tan 50 - 2) = 0$ $\tan x = \text{awrt } 0.118, -8.49$ $x = 6.72, 96.72, 186.72$	<p>M1A1</p> <p>dM1 A1dM1A1</p>



Question Number	Scheme	Marks
<p><b>3(a)</b></p>	$4x^3 + 2x^2 + 17x + 8 \equiv (Ax + B)(x^2 + 4) + Cx + D$ <p>Compare <math>x^3</math> terms: <math>A=4</math>            Compare <math>x^2</math> terms: <math>B=2</math>            Compare either <math>x</math> term or constant term: <math>4A+C=17</math> or <math>4B+D=8</math>  <math>\Rightarrow C=..</math> or <math>D=..</math>  <math>\Rightarrow C=1, D=0</math></p>	<p>B1            B1            M1            A1  <b>(4)</b></p>
<p><b>(b)</b></p>	$\int_1^4 \frac{4x^3 + 2x^2 + 17x + 8}{x^2 + 4} dx = \int_1^4 4x + 2 + \frac{x}{x^2 + 4} dx$ $= \left[ 2x^2 + 2x + \frac{1}{2} \ln(x^2 + 4) \right]_1^4$ $= \left[ 2 \times 16 + 2 \times 4 + \frac{1}{2} \ln(20) \right] - \left[ 2 \times 1 + 2 \times 1 + \frac{1}{2} \ln(5) \right]$ $= 36 + \frac{1}{2} \ln\left(\frac{20}{5}\right)$ $= 36 + \ln(2)$	<p>M1            M1, M1A1            dM1            A1  <b>(6)</b>  <b>(10 marks)</b></p>

**Notes for Question 3**

(a)

B1 States that  $A=4$ . It may be implied by writing out the rhs as  $(4x + B)(x^2 + 4) + Cx + D$

B1 States that  $B=2$ . It may be implied by writing out the rhs as  $(Ax + 2)(x^2 + 4) + Cx + D$

M1 Compares either the  $x$  or constant terms and proceeding to find a numerical value of either  $C$  or  $D$ .  
This mark may be implied by a correct value of either  $C$  or  $D$ .

A1 Both values correct  $C = 1, D = 0$

Alternatively can be scored via 'division'.

$$\begin{array}{r} x^2 + 0x + 4 \overline{) 4x^3 + 2x^2 + 17x + 8} \\ \underline{4x^3 + 0x^2 + 16x} \phantom{+ 8} \\ \phantom{4x^3 + } 2x^2 + 1x + 8 \\ \phantom{4x^3 + } \underline{2x^2 + 0x + 8} \\ \phantom{4x^3 + } \phantom{2x^2 + } 1x + 0 \end{array}$$

B1, B1 for sight of the 4 and the 2 in quotient  $4x + 2$

M1 for proceeding to get a linear remainder

A1 The correct linear remainder. Accept  $x$ . If their division is unclear accept the answers in the correct place in part b

(b)

M1 For using their answers to part (a) to rewrite the integral in the form

$$\int \frac{4x^3 + 2x^2 + 17x + 8}{x^2 + 4} dx = \int 'A'x + 'B' + \frac{'C'x + 'D'}{x^2 + 4} dx \text{ with numerical values for } A, B, C, \text{ and } D.$$

We will condone a restart to this question in (b) but it would not score marks in (a)

M1 For the correct method of integrating the ' $A$ ' $x$  + ' $B$ ' part. Follow through on their ' $A$ ' and ' $B$ '

Accept  $\frac{A}{2}x^2 + Bx$  or  $\frac{(Ax + B)^2}{2}$ . It cannot be scored for an attempt to integrate  $( 'A'x + 'B' )(x^2 + 4)$

M1 For the correct method of integrating  $\frac{'C'x}{x^2 + 4}$ . Accept constant  $\times \ln(x^2 + 4)$  or constant  $\times x \frac{\ln(x^2 + 4)}{x}$

This can be scored for values of  $D \neq 0$  as long as  $\int \frac{'C'x + 'D'}{x^2 + 4} dx = \int \frac{'C'x}{x^2 + 4} dx + \int \frac{'D'}{x^2 + 4} dx$ .

A1 Correct integral  $2x^2 + 2x + \frac{1}{2} \ln(x^2 + 4) + (c)$ . There is no requirement for  $+c$ .

dM1 For putting in limits, subtracting **and** correctly collecting terms in  $\ln$ 's using subtraction law.

It is dependent upon having scored the previous M. Allow, for example,  $\frac{1}{2} \ln 20 - \frac{1}{2} \ln 5 = \ln 2$

A1 CSO and CAO  $36 + \ln(2)$

Question Number	Scheme	Marks
4(a)	$fg(1) = f(2) = 7$	M1A1 (2)
(b)	Either $g(0)=3$ or $g(x \rightarrow \infty) \rightarrow 0.5$ $0.5 < g(x) \leq 3$	M1 A1 (2)
(c)	Attempt change of subject of $y = \frac{x+9}{2x+3} \Rightarrow y(2x+3) = x+9$ $\Rightarrow 2xy - x = 9 - 3y$ $\Rightarrow x(2y-1) = 9 - 3y \Rightarrow x = \frac{9-3y}{2y-1}$ $g^{-1}(x) = \frac{9-3x}{2x-1}, \quad 0.5 < x \leq 3$	M1 dM1 A1, B1 ft (4)
(d)	Attempts $f(0) = 2 \times 3 + 5 = 11 \Rightarrow k \leq 11$ Or $f(3) = 2 \times 0 + 5 = 5 \Rightarrow k > 5$ $5 < k \leq 11$	M1A1 A1 (3)  (11 marks)

Notes for Question 4

(a)

M1 Full method for their answer to  $g(1)$  being subbed into  $f$ . The order must be correct.Can be scored for seeing 1 being substituted into  $2\left|3 - \frac{x+9}{2x+3}\right| + 5$ 

A1 cso 7. Do not accept multiple answers.

Just '7' would score both marks as long as no incorrect working is seen

(b)

M1 Calculates the value of  $g$  at either 'end'. Sight of 3 or 0.5 is sufficient.A1  $0.5 < g(x) \leq 3$ . Accept  $0.5 < y \leq 3$ Also accept variations such as  $(0.5, 3]$ , All values (of  $y$ ) bigger than 0.5 but less than or equal to 3.Do not accept this in terms of  $x$ .

(c)

M1 For an attempt to make  $x$  (or a switched  $y$ ) the subject of the formula. For this to be scored they must cross multiply and get both  $x$  (or switched  $y$ ) terms on the same side of the equation. Allow slips.dM1 This is dependent upon the first M being scored. In addition to collecting like terms they must factorise and divide. Condone just **one numerical/sign** slip. Accept  $x$  being given as a function of  $y$ .A1  $g^{-1}(x) = \frac{9-3x}{2x-1}$  or  $g^{-1}(x) = \frac{3x-9}{1-2x}$ . Accept the form  $y =$ ,  $g^{-1} =$  instead of  $g^{-1}(x)$  but the functionmust be in terms of  $x$ .B1ft Accept either  $0.5 < x \leq 3$ ,  $(0.5, 3]$  or follow through on the candidates range to part (b).The domain cannot be expressed in terms of  $y$ .Do not follow through on  $y \in \mathbb{R} \Rightarrow x \in \mathbb{R}$ 

(d)

M1 Attempts to find either  $f(0)$  or  $f(3)$ . Evidence could be seeing  $2|3-0|+5$  or  $2|3-3|+5$  or the sight of 5 or 11.A1 For a range with both ends, for example  $5 < k < 11$ ,  $5 \leq k \leq 11$ ,  $5 \leq k < 11$  or alternatively getting one end completely correct  $k \leq 11$ , or  $k > 5$ . Accept  $y \leq 11$  etcA1 cao  $5 < k \leq 11$ . Accept  $(5, 11]$ ,  $k \leq 11$  **and**  $k > 5$ Do not accept  $k \leq 11$  **or**  $k > 5$  **or**  $5 < y \leq 11$  for the final mark

Question Number	Scheme	Marks
<p><b>5 (a)</b></p> <p><b>(b)</b></p>	<p>Sets <math>y = 2^x</math> and takes <math>\ln</math> of both sides to get <math>\ln y = x \ln 2</math></p> <p>Differentiates wrt <math>x</math> to get <math>\frac{1}{y} \frac{dy}{dx} = \ln 2 \Rightarrow \frac{dy}{dx} = ..</math></p> <p>Rearranges to achieve <math>\frac{dy}{dx} = 2^x \ln 2</math></p> <p>Differentiates wrt <math>x</math> <math>\frac{d}{dx} (2 + 6y \frac{dy}{dx} + 6xy + 3x^2 \frac{dy}{dx}) = 4 \times 2^x \ln 2</math></p> <p>Substitutes <math>(2, 0)</math> <b>AND</b> rearranges to get <math>\frac{dy}{dx}</math></p> <p><math>\Rightarrow 2 + 12 \frac{dy}{dx} = 16 \ln 2 \Rightarrow \frac{dy}{dx} = \frac{16 \ln 2 - 2}{12}</math> (<math>= 0.758</math>)</p> <p>Find equation of tangent using <math>(2, 0)</math> and their numerical <math>\frac{dy}{dx}</math></p> <p><math>y = \frac{(16 \ln 2 - 2)(x - 2)}{12}</math></p> <p>Accept <math>y = 0.76x - 1.52</math></p>	<p>M1</p> <p>dM1</p> <p>cao A1*</p> <p><b>(3)</b></p> <p>oe <u>M1, B1</u>, A1</p> <p>M1</p> <p>dM1</p> <p>oe A1</p> <p><b>(6)</b></p> <p><b>(9 marks)</b></p>
<p><b>Alt 1</b></p> <p><b>5 (a)</b></p>	<p>Writes <math>2^x = e^{x \ln 2}</math></p> <p>Differentiates wrt <math>x</math> to get <math>\frac{d}{dx} (e^{x \ln 2}) = e^{x \ln 2} \ln 2 = 2^x \ln 2</math></p>	<p>M1</p> <p>cao dM1 A1*</p> <p><b>(3)</b></p>
<p><b>Alt 2</b></p> <p><b>5 (a)</b></p>	<p>Sets <math>y = 2^x</math> and takes <math>\ln_2</math> of both sides to get</p> <p><math>\ln_2 y = x \Rightarrow \frac{\ln y}{\ln 2} = x \Rightarrow \ln y = x \ln 2</math></p>	<p>M1</p> <p><b>(3)</b></p>

Notes for Question 5

(a)

M1 Sets  $y = 2^x$ , takes ln of both sides, then uses index law to get  $\ln y = x \ln 2$ dM1 Differentiates wrt  $x$  to get  $\frac{1}{y} \frac{dy}{dx} = \ln 2$  and then proceeds to  $\frac{dy}{dx} = ..$ Alternatively differentiates wrt  $y$  to get  $\frac{1}{y} = \ln 2 \frac{dx}{dy}$ A1\*  $\frac{dy}{dx} = 2^x \ln 2$ . This is a given answer. All aspects of the proof must be present.**(Alt a)**M1 Writes  $2^x = e^{x \ln 2}$ dM1 Differentiates wrt  $x$  to get  $\frac{d}{dx}(e^{x \ln 2}) = Ae^{x \ln 2}$ A1\*  $\frac{d}{dx}(e^{x \ln 2}) = e^{x \ln 2} \ln 2 = 2^x \ln 2$ . This is a given answer. All aspects of the proof must be present

(b)

M1 Uses the product rule to differentiate  $3x^2 y$ . Evidence could be sight of  $Axy + 3x^2 \frac{dy}{dx}$ If the rule is quoted it must be correct. It could be implied by  $u=.., u'=.., v=.., v'=..$  followed by their  $vu'+uv'$ .For this M to be scored  $y$  must differentiate to  $\frac{dy}{dx}$ , it cannot differentiate to 1.B1 Differentiates  $2x + 3y^2 \rightarrow 2 + 6y \frac{dy}{dx}$ Watch for people who divide by 4 first. Then  $\frac{1}{2}x + \frac{3}{4}y^2 \rightarrow \frac{1}{2} + \frac{3}{2}y \frac{dy}{dx}$ 

A1 A completely correct differential. It need not be simplified.

Accept the form  $2dx + 6ydy + 6xydx + 3x^2dy = 4 \times 2^x \ln 2 dx$  for the first three marksNote that  $\frac{dy}{dx} = 2 + 6y \frac{dy}{dx} + 6xy + 3x^2 \frac{dy}{dx} = 4 \times 2^x \ln 2$  is A0 but they can recover if their intention is clear.M1 Substitutes  $x = 2, y = 0$  into their expression, and rearranges to find a 'numerical' value for  $\frac{dy}{dx}$ dM1 Uses their numerical value to  $\frac{dy}{dx}$  and  $(2, 0)$  to find an equation of a tangent.Accept  $\frac{y-0}{x-2} = \text{Numerical} \frac{dy}{dx}$ If  $y = mx + c$  is used then a full method must be seen to find 'c' using both  $(2, 0)$  and a numerical m.A1  $y = \frac{(16 \ln 2 - 2)(x - 2)}{12}$ .Accept alternatives such as  $\frac{y-0}{x-2} = \frac{(16 \ln 2 - 2)}{12}, \frac{y-0}{x-2} = \frac{(2 \ln 16 - 1)}{6}$ As the form of the answer is not required accept awrt  $2dp$   $y = 0.76x - 1.52, \frac{y-0}{x-2} = 0.76$

Question Number	Scheme	Marks
<b>6 (a)</b>	$\frac{6}{\sqrt{(9+Ax^2)}} = 6(9+Ax^2)^{-\frac{1}{2}} = 6 \times 9^{-\frac{1}{2}} \left(1 + \frac{A}{9}x^2\right)^{-\frac{1}{2}} \qquad 9^{-\frac{1}{2}} \text{ or } \frac{1}{3}$ $= 2 \times \left( 1 + \left(-\frac{1}{2}\right)\left(\frac{A}{9}x^2\right) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)}{2} \left(\frac{A}{9}x^2\right)^2 + \dots \right)$ $= 2 \times \left( 1 - \frac{A}{18}x^2 + \frac{A^2}{216}x^4 + \dots \right)$ $= 2 - \frac{A}{9}x^2 + \frac{A^2}{108}x^4 + \dots$ <p>Compare to <math>B - \frac{2}{3}x^2 + Cx^4 \Rightarrow</math></p> $B = 2$ $A = 6$ $C = \frac{1}{108} \times A^2 = \frac{1}{3}$	<p>B1</p> <p><u>M1A1</u></p> <p>B1</p> <p>B1</p> <p>dM1A1</p> <p>(7)</p>
<b>(b)</b>	<p>Coefficient of <math>x^6 = 2 \times \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)}{3!} \times \left(\frac{A}{9}\right)^3 = -\frac{5}{27}</math></p>	<p>M1A1</p> <p>(2)</p> <p><b>(9 marks)</b></p>

**Notes for Question 6**

For this question (a) and (b) can be treated as one whole question. Marks for (a) can be gained in (b)

(a)

B1 For taking out a factor of  $9^{-\frac{1}{2}}$

Evidence would see either  $6 \times 9^{-\frac{1}{2}}$  or  $6 \times \frac{1}{3}$  or 2 before the bracket.

M1 For the form of the binomial expansion with  $n = -\frac{1}{2}$  and a term of  $\left(\frac{A}{9}x^2\right)$

To score M1 it is sufficient to see just either the first two terms. ie.  $1 + \left(-\frac{1}{2}\right)\left(\frac{A}{9}x^2\right) + \dots$

or the first term and a later term if an error was made on term two. Condone poor bracketing  
If the 9 has been removed 'incorrectly' accept for this M mark

$$(1 + kAx^2)^{-\frac{1}{2}} = 1 + \left(-\frac{1}{2}\right)(kAx^2) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)}{2}(kAx^2)^2$$

A1 Any (unsimplified) form of the binomial expansion. Ignore the factor preceding the bracket.

$$1 + \left(-\frac{1}{2}\right)\left(\frac{A}{9}x^2\right) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)}{2}\left(\frac{A}{9}x^2\right)^2 + \dots \text{ is acceptable.}$$

The bracketing must be correct but it is OK for them to recover.

B1 For writing down  $B = 2$

Note that this could be found by substituting  $x = 0$  into both sides of expression

B1 For writing down  $A = 6$

dM1 For substituting their numerical value of  $A$  into their coefficient of  $x^4$  (involving  $A$  or  $A^2$ ) to find  $C$ .  
The coefficient does not need to be correct but the previous M1 must have been scored.

A1 For  $C = \frac{1}{3}$ . Accept equivalents like  $C = \frac{36}{108} = 0.\dot{3}$

(b)

M1 For a correct unsimplified term in  $x^6$  of the binomial exp with  $n = -\frac{1}{2}$  and term =  $\left(\frac{\text{their 'A'}}{9}x^2\right)$ .

Sight of ~~2~~  $\frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)}{3!} \times \left(\frac{A}{9}\right)^3$  with or without the factor of 2 with their numerical  $A$

Accept with or without correct bracketing but must involve  $A^3$ .

You may have to check  $-\frac{5A^3}{11664}$  or  $2 \times -\frac{5A^3}{11664} = -\frac{5A^3}{5832}$  if there is little working

Allow this mark if a candidate has a correct unsimplified fraction in part a, but then uses an incorrect simplification in calculating the term in  $x^6$ . This incorrect simplification must include  $\dots A^3$

A1  $-\frac{5}{27}$  or other exact correct equivalents such as  $-\frac{15}{81}$ ,  $-\frac{3240}{17496}$ . Accept with the  $x^6$



Question Number	Scheme	Marks
<p><b>7 (a)</b></p> <p><b>(b)</b></p> <p><b>(c)</b></p> <p><b>(d)</b></p>	<p>Applies <math>vu' + uv'</math> with <math>u=2x+2x^2</math> and <math>v=\ln x</math> or vice versa</p> $f'(x) = \ln(x)(2 + 4x) + (2x + 2x^2) \times \frac{1}{x}$ <p>Sets <math>\ln(x)(2 + 4x) + (2x + 2x^2) \times \frac{1}{x} = 0</math> and makes <math>\ln x</math> the subject</p> $\ln(x) = -\frac{1+x}{1+2x} \Rightarrow x = e^{-\frac{1+x}{1+2x}}$ <p>Subs <math>x_0 = 0.46</math> into <math>x = e^{-\frac{1+x}{1+2x}}</math></p> <p><math>x_1 = \text{awrt } 0.4675</math>, <math>x_2 = \text{awrt } 0.4684</math> <math>x_3 = \text{awrt } 0.4685</math></p> <p><math>A = (0.47, -1.04)</math></p>	<p>M1A1A1 (3)</p> <p>M1 dM1A1* (3)</p> <p>M1 A1,A1 (3)</p> <p>M1A1 (2)</p> <p><b>(11 marks)</b></p>
<p><b>Alt 7 (a)</b></p>	<p>Writes <math>f(x) = 2x \ln x + 2x^2 \ln x</math> and applies <math>vu' + uv'</math></p> $f'(x) = 2 \ln(x) + 2x \times \frac{1}{x} + 2x^2 \times \frac{1}{x} + 4x \ln x$	<p>M1A1A1 (3)</p>

Notes for Question 7

- (a)
- M1 Fully applies the product rule to  $2x(1+x)\ln x$ . This can be achieved by **Either** setting  $u=2x+2x^2$  and  $v=\ln x$ .
- If the rule is quoted it must be correct and  $\ln x \rightarrow \frac{1}{x}$  when differentiated. If the rule is not quoted, it can be implied by  $u = 2x + 2x^2$ ,  $v = \ln x$ ,  $u' = A + Bx$ ,  $v' = \frac{1}{x}$  followed by their  $vu' + uv'$  only accept answers of the form  $f'(x) = \ln(x)(A + Bx) + (2x + 2x^2) \times \frac{1}{x}$
- Or** writing  $f(x) = 2x \ln x + 2x^2 \ln x$  and attempting to apply the product rule to both parts. It must be seen to be correctly applied to at least one of the products. See above for the rules.
- Again insist on  $\ln x \rightarrow \frac{1}{x}$  when differentiating.
- Or** applying the product rule to a triple product.
- Look for expressions like  $\frac{d}{dx}(uvw) = u'vw + uv'w + uvw'$
- A1 Two out of the four separate terms correct (unsimplified).
- A1 All four terms correct (unsimplified)  $f'(x) = \ln(x)(2 + 4x) + (2x + 2x^2) \times \frac{1}{x}$
- or if two applications  $f'(x) = 2 \ln(x) + 4x \ln(x) + 2x \times \frac{1}{x} + 2x^2 \times \frac{1}{x}$
- (b)
- M1 Sets or implies that their  $f'(x) = 0$  and proceeds to make the  $\ln x$  term the subject of the formula, To score this  $f'(x)$  does not need to be correct but it must be of equal difficulty. Look for more than one term in  $\ln x$  and two other 'unlike terms'
- dM1 Dependent upon the last M1. For moving from  $\ln x = \dots \Rightarrow x = e^{\dots}$
- A1\* CSO  $x = e^{-\frac{1+x}{1+2x}}$ .  
All aspects of the proof must be correct including the position of the minus sign and the bracketing.
- (b) Alt working backwards
- M1 By taking  $\ln$ 's proceeds from  $x = e^{-\frac{1+x}{1+2x}}$  to  $\pm \ln x \times (1 + 2x) = \pm(1 + x)$
- dM1 Dependent upon the last M1. Moves to  $\pm \ln x \times (2 + 4x) \pm (2 + 2x) = 0$
- A1 For a statement that completes the proof. Accept 'hence  $f'(x) = 0 \Rightarrow$  solution is the  $x$  coordinate of  $A$ . All aspects must be correct including their  $f'(x)$ .
- (c)
- M1 For an attempt to find  $x_1$  from the value of  $x_0$  by substituting 0.46 into  $e^{-\frac{1+x}{1+2x}}$
- Possible ways this can be scored could be sight of  $e^{-\frac{1+0.46}{1+2 \times 0.46}}$  or awrt 0.47
- A1  $x_1 =$ awrt 0.4675.
- A1  $x_2 =$  awrt 0.4684  $x_3 =$  awrt 0.4685
- (d)
- M1 For **either**  $x = 0.47$ , **or**  $y = -1.04$  as a result of using  $x_3 = 0.46$  truncated or  $x_3 = 0.47$  rounded from part c. Alternatively for substituting their answer for  $x_3$  in part (c) either to 4dp or rounded to 2dp into  $f(x)$  to find the  $y$  coordinate of  $A$ . Accept sight of  $2 \times x_3(1 + x_3) \ln x_3$
- A1  $A = (0.47, -1.04)$ .

Question Number	Scheme	Marks
<p><b>8 (a)</b></p>	$2\operatorname{cosec}2A - \cot A = \frac{2}{\sin 2A} - \frac{1}{\tan A} \qquad 2\operatorname{cosec}2A = \frac{2}{\sin 2A}$ $= \frac{2}{2\sin A \cos A} - \frac{\cos A}{\sin A}$ $= \frac{2 - 2\cos^2 A}{2\sin A \cos A}$ $\frac{2(1 - \cos^2 A)}{2\sin A \cos A} = \frac{2\sin^2 A}{2\sin A \cos A} = \frac{\sin A}{\cos A} = \tan A$	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1*</p> <p>(4)</p>
<p><b>(b)(i)</b></p>	$2\operatorname{cosec}4\theta - \cot 2\theta = \sqrt{3} \Rightarrow \tan 2\theta = \sqrt{3}$ $\Rightarrow \theta = \frac{\arctan \sqrt{3}}{2} = \frac{\pi}{6} \qquad \text{Accept awrt } 0.524$	<p>M1</p> <p>A1</p>
<p><b>(ii)</b></p>	$\tan \theta + \cot \theta = 5 \Rightarrow \operatorname{cosec}2\theta = \frac{5}{2}$ $\Rightarrow \theta = \frac{1}{2} \arcsin\left(\frac{2}{5}\right) = \text{awrt } 0.206, 1.37$	<p>M1</p> <p>dM1A1A1</p> <p>(6)</p>
<b>(10 marks)</b>		
<p><b>Alt 8 (a)</b></p>	$2\operatorname{cosec}2A - \cot A = \tan A \Rightarrow \frac{2}{\sin 2A} - \frac{1}{\tan A} = \tan A$ $\Rightarrow \frac{2}{2\sin A \cos A} - \frac{\cos A}{\sin A} = \frac{\sin A}{\cos A}$ $\times 2\sin A \cos A \Rightarrow 2 - 2\cos^2 A = 2\sin^2 A$ $\Rightarrow 2(1 - \cos^2 A) = 2\sin^2 A$ $\Rightarrow 2\sin^2 A = 2\sin^2 A \quad \text{QED (minimal statement must be seen)}$	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1* (4)</p>
<p><b>Alt 8b(ii)</b></p>	$\tan \theta + \cot \theta = 5 \Rightarrow \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} = 5 \Rightarrow \frac{1}{\frac{1}{2}\sin 2\theta} = 5 \Rightarrow \sin 2\theta = \frac{2}{5}$ <p>This can now score all of the marks as it is effectively using part (a)</p>	<p>M1</p>
<p><b>SC 8b(ii)</b></p>	$\tan \theta + \cot \theta = 5 \Rightarrow \tan \theta + \frac{1}{\tan \theta} = 5 \Rightarrow \tan^2 \theta - 5 \tan \theta + 1 = 0$ $\Rightarrow \theta = \text{awrt } 0.206, 1.37$ <p>This is not using part (a) and is a special case with one mark per correct answer. One answer = 1000 Two answers = 1100</p>	<p>1,1,0,0</p>

Notes for Question 8

(a)

B1 Writes  $2 \operatorname{cosec} 2A$  as  $\frac{2}{\sin 2A}$ M1 Uses the double angle formula for  $\sin 2A$  (see below) and  $\cot A = \frac{\cos A}{\sin A}$  to write the given expression in terms of just  $\sin A$  and  $\cos A$ For the double angle formula accept sight of  $\frac{2}{2 \sin A \cos A}$  or  $\frac{2}{\sin A \cos A + \cos A \sin A}$ Condone  $\sin 2A = 2 \sin \cos$  for this method within their solution.M1 For writing the given expression as a single fraction in terms of just  $\sin A$  and  $\cos A$   
The denominator must be correct for their fraction and at least one numerator must have been modified.Accept  $\frac{2}{2 \sin A \cos A} - \frac{\cos A}{\sin A} \rightarrow \frac{2 \sin A - 2 \sin A \cos^2 A}{2 \sin^2 A \cos A}$  - not the lowest common denominator.Accept  $\frac{1}{2 \sin A \cos A} - \frac{\cos A}{\sin A} \rightarrow \frac{\sin A - 2 \cos^2 A}{2 \sin A \cos A}$  Incorrect 'fraction' but denominator correct

A1\* A completely correct proof. This is a given solution and there must not be any errors.

For this mark do not condone expressions like  $\sin 2A = 2 \sin \cos$ 

The 2's must be cancelled at some point. It is OK for them to 'just' disappear

The  $1 - \cos^2 A$  term must be replaced with  $\sin^2 A$ .  $\frac{2 \sin^2 A}{2 \sin A \cos A}$ The expression  $\frac{\sin A}{\cos A}$  must be clearly seen before being replaced by  $\tan A$  but  $\frac{2 \sin^2 A}{2 \sin A \cancel{\cos A}}$  is OK

(b (i))

M1 Uses part (a) to write given equation in form  $\tan 2\theta = \sqrt{3}$  and proceeding to  $\theta = ..$ This may be implied by  $A = 2\theta$  as long as they proceed to  $\theta = ..$ Accept a restart as long as they get to the line  $\tan 2\theta = \sqrt{3}$ A1  $\theta = \frac{\pi}{6}$ . Accept awrt 0.524 (radians) but not  $30^\circ$ . Ignore extra solutions outside the range.

Withhold this mark if extra solutions are given inside the range.

The answer without working **does not** score any marks. The demand of the question is clearly stated – Hence solve...meaning that you should see an equivalent statement to  $\tan 2\theta = \sqrt{3}$ 

(b (ii))

M1 Uses part (a) to write given equation in form  $\operatorname{cosec} 2\theta = C$ , where  $C$  is a constant.It may be implied by  $\sin 2\theta = ..$ 

dM1 Dependent upon the first method and is scored for the correct 'order' of operations.

The mark is scored for  $\operatorname{cosec} 2\theta = C \Rightarrow \sin 2\theta = \frac{1}{C} \Rightarrow 2\theta = \arcsin\left(\frac{1}{C}\right) \Rightarrow \theta = ..$ It can be implied by a correct answer only if the line  $\operatorname{cosec} 2\theta = C$  is present.A1 One correct solution awrt 0.206 or 1.37. Accept awrt  $0.0656\pi$ ,  $0.436\pi$ . Remember to isw here.Accept awrt  $11.8^\circ$  or  $78.2^\circ$  if the mark in (bi) had been lost for  $30^\circ$ 

A1 Both solutions correct and no extras inside the range. See above for alternatives.

The correct answers without working **does not** score any marks.**Special case** where they produce answers from a quadratic in  $\tan \theta$  can score 1100 if they get both answers and no others inside the range.

Question Number	Scheme	Marks
<p><b>9(a)</b></p> <p><b>(b)</b></p> <p><b>(c)</b></p>	$u = 4 - \sqrt{x} \Rightarrow x = (4 - u)^2 \Rightarrow \frac{dx}{du} = -2(4 - u)$ $\int \frac{dx}{4 - \sqrt{x}} = \int \frac{-2(4 - u)du}{u} = \int -\frac{8}{u} + 2du$ $= -8\ln u + 2u \quad (+c)$ $= -8\ln 4 - \sqrt{x}  + 2(4 - \sqrt{x}) + c \quad \text{oe}$ <p>Height increases when <math>\frac{dh}{dt} = \frac{4 - \sqrt{h}}{20} &gt; 0 \Rightarrow (0 &lt;) h &lt; 16</math></p> $\frac{dh}{dt} = \frac{4 - \sqrt{h}}{20} \Rightarrow \int \frac{dh}{4 - \sqrt{h}} = \int \frac{dt}{20}$ $\Rightarrow -8\ln(4 - \sqrt{h}) + 2(4 - \sqrt{h}) = \frac{t}{20} + c$ <p>Substitute <math>t=0, h=1 \quad -8\ln 3 + 6 = c</math></p> $\Rightarrow -8\ln(4 - \sqrt{h}) + 2(4 - \sqrt{h}) = \frac{t}{20} - 8\ln 3 + 6 \quad \text{oe}$ <p>Substitute <math>h=10</math> into <math>\Rightarrow -8\ln(4 - \sqrt{10}) + 2(4 - \sqrt{10}) = \frac{t}{20} - 8\ln 3 + 6</math></p> $\Rightarrow t = \text{awrt } 118 \text{ (years)}$	<p>M1A1</p> <p>M1A1</p> <p>dM1</p> <p>A1</p> <p><b>(6)</b></p> <p>M1A1</p> <p><b>(2)</b></p> <p>B1</p> <p>M1A1</p> <p>dM1</p> <p>A1</p> <p>ddM1</p> <p>A1</p> <p><b>(7)</b></p> <p><b>(15 marks)</b></p>
<p><b>Alt (c)</b></p>	$\frac{dh}{dt} = \frac{4 - \sqrt{h}}{20} \Rightarrow \int \frac{dh}{4 - \sqrt{h}} = \int \frac{dt}{20}$ $\Rightarrow -8\ln(4 - \sqrt{h}) + 2(4 - \sqrt{h}) = \frac{t}{20}$ $\Rightarrow \left[ -8\ln(4 - \sqrt{h}) + 2(4 - \sqrt{h}) \right]_{h=1}^{h=10} = \left[ \frac{t}{20} \right]_{t=0}^T$ $\Rightarrow \left( -8\ln(4 - \sqrt{10}) + 2(4 - \sqrt{10}) \right) - \left( -8\ln(4 - \sqrt{1}) + 2(4 - \sqrt{1}) \right) = \frac{T}{20}$ $\Rightarrow T = \text{awrt } 118 \text{ (years)}$	<p>B1</p> <p>M1</p> <p>A1</p> <p>dM1, ddM1, A1</p> <p>A1</p>

Notes for Question 9

(a)

M1 Scored for an attempt to write  $x$  in terms of  $u$  **and** differentiating to get either  $dx$  in terms of  $du$  or  $\frac{dx}{du}$  in

terms of  $u$ . Accept for the M incorrect expressions like  $x = 16 - u^2 \Rightarrow \frac{dx}{du} = -2u$

The minimum expectation is that the expression in  $u$  is quadratic and the derivative in  $u$  is linear.

Alternatively uses  $u = 4 - \sqrt{x}$  to find  $\frac{du}{dx} = Cx^{-0.5}$  and attempts to get  $\frac{dx}{du} = f(u)$  or similar.

A1 Either  $\frac{dx}{du} = -2(4-u)$  or  $dx = -2(4-u)du$  or  $x' = -2(4-u)$  or equivalents. Condone  $dx = -8 + 2u$

Accept these within the integral for both marks as long as no incorrect working is seen.

M1 An attempt to divide their  $dx$  by  $u$  to get an integral of the form  $\int \frac{A}{u} + B(du)$ .

A1 A fully correct integral in terms of  $u$ . Condone the omission of  $du$  if the intention is clear.

Accept forms such as  $\int -\frac{8}{u} + 2du$   $\int -8u^{-1} + 2du$   $-2\left(\int \frac{4}{u} - 1\right)$

dM1 For integrating  $\frac{1}{u} \rightarrow \ln u$  and increasing the power of any other term(s). It is dependent upon the previous

method mark. There is no need to set the answer in terms of  $x$ . There is no need to have  $+c$

A1 For a correct answer in terms of  $x$  with or without  $+c$ . There is no requirement for modulus signs.

Accept either  $= -8\ln|4 - \sqrt{x}| + 2(4 - \sqrt{x}) (+c)$  or  $= -8\ln(4 - \sqrt{x}) - 2\sqrt{x} (+c)$  oe

(b)

M1 Setting  $\frac{dh}{dt} = 0 \Rightarrow h = \dots$  or  $\frac{dh}{dt} > 0 \Rightarrow h < \dots$  Accept  $h=16$  for this mark.

A1 Stating either  $h < 16$  or  $0 < h < 16$  or  $0 \leq h < 16$  or all values up to 16.

A correct answer can score both marks as long as no incorrect working is seen.

(c)

B1 Writing  $\int \frac{dh}{4 - \sqrt{h}} = \int \frac{dt}{20}$  or equivalent. It must include  $dh$  and  $dt$  but  $\int$  could be implied

M1 For an attempt to integrate **both** sides, no need for  $c$

Follow through on **their** answer to part (a) for  $x$  or  $u$  with ' $h$ ' on the lhs with  $At$  on the rhs.

A1 A fully correct answer with  $+c$   $-8\ln(4 - \sqrt{h}) + 2(4 - \sqrt{h}) = \frac{t}{20} + c$

dM1 Substitute  $t = 0, h = 1$  in an attempt to find  $c$ . Minimal evidence is required. Accept  $t = 0, h = 1 \Rightarrow c = \dots$  The previous M must have been awarded.

A1 A correct equation  $\Rightarrow -8\ln(4 - \sqrt{h}) + 2(4 - \sqrt{h}) = \frac{t}{20} - 8\ln 3 + 6$  oe.

Accept  $\Rightarrow -8\ln(4 - \sqrt{h}) + 2(4 - \sqrt{h}) = \frac{t}{20} + \text{awrt } 2.79$

ddM1 Substitute  $h=10$  into their equation involving  $h, t$  and their value of  $c$  in an attempt to find  $t$ .

It is dependent upon both M's being scored in this part of the question. Again accept minimal evidence

A1 Awrt 118 (years). The answer without any correct working scores 0 marks.

Condone  $x$  and  $h$  being interchanged in this part of the question.

(c Alt)

A1 Setting the limits is equivalent to understanding that there is a constant.

dM1 Using limits of 1 and 10 and subtracting ddM1 Using limits of ' $t$ ' and 0 and subtracting

A1 A fully correct expression involving just ' $t$ ' A1 Awrt 118 (years). No working = 0 marks

Question Number	Scheme	Marks
<p><b>10 (a)</b></p>	$\begin{pmatrix} 1 \\ 5 \\ 5 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 1 \\ -1 \end{pmatrix} = \begin{pmatrix} 0 \\ 2 \\ 12 \end{pmatrix} + \mu \begin{pmatrix} 3 \\ -1 \\ 5 \end{pmatrix} \Rightarrow \begin{matrix} 1+2\lambda = 3\mu \\ 5+\lambda = 2-\mu \\ 5-\lambda = 12+5\mu \end{matrix} \text{ any two of}$ <p>Full method to find both <math>\lambda</math> and <math>\mu</math></p> $(2) + (3) \Rightarrow 10 = 14 + 4\mu \Rightarrow \mu = -1$ <p>Sub <math>\mu = -1</math> into (2) <math>\Rightarrow 5 + 1\lambda = 2 - (-1) \Rightarrow \lambda = -2</math></p> <p>Check values in 3<sup>rd</sup> equation <math>1 + 2(-2) = 3(-1)</math>.</p> <p>Position vector of intersection is <math>\begin{pmatrix} 1 \\ 5 \\ 5 \end{pmatrix} + -2 \begin{pmatrix} 2 \\ 1 \\ -1 \end{pmatrix}</math> OR <math>\begin{pmatrix} 0 \\ 2 \\ 12 \end{pmatrix} + (-1) \begin{pmatrix} 3 \\ -1 \\ 5 \end{pmatrix} = \begin{pmatrix} -3 \\ 3 \\ 7 \end{pmatrix}</math></p>	<p>M1</p> <p>dM1</p> <p>A1</p> <p>B1</p> <p>ddM1,A1</p> <p><b>(6)</b></p>
<p><b>(b)</b></p>	$\begin{pmatrix} 2 \\ 1 \\ -1 \end{pmatrix} \cdot \begin{pmatrix} 3 \\ -1 \\ 5 \end{pmatrix} = 2 \times 3 + 1 \times -1 + -1 \times 5 = 0$ <p>Scalar product = 0, lines are perpendicular</p>	<p>M1</p> <p>A1</p> <p><b>(2)</b></p>
<p><b>(c)</b></p>	<p>Let <math>X</math> be the point of intersection <math>\overline{OX} = \begin{pmatrix} -3 \\ 3 \\ 7 \end{pmatrix}</math></p> $\overline{AX} = \overline{OX} - \overline{OA} = \begin{pmatrix} -8 \\ -4 \\ 4 \end{pmatrix}$ $\overline{OB} = \overline{OX} + \overline{AX} = \begin{pmatrix} -3 \\ 3 \\ 7 \end{pmatrix} + \begin{pmatrix} -8 \\ -4 \\ 4 \end{pmatrix} = \begin{pmatrix} -11 \\ -1 \\ 11 \end{pmatrix}$	<p>M1</p> <p>M1A1</p> <p><b>(3)</b></p> <p><b>(11 marks)</b></p>

**Notes for Question 10**

(a)

M1 For writing down any two equations that give the coordinates of the point of intersection.

Accept two of  $1 + 2\lambda = 3\mu$ ,  $5 + \lambda = 2 - \mu$ ,  $5 - \lambda = 12 + 5\mu$

There must be an attempt to set the coordinates equal but condone slips.

dM1 A full method to find **both**  $\lambda$  and  $\mu$ .

Don't be overly concerned with the mechanics of the method but it must end with values for both. It is dependent upon the previous method

A1 Both values correct  $\mu = -1$   $\lambda = -2$

B1 The correct values of  $\lambda$  and  $\mu$  must be substituted into **both** sides of the third equation with some calculation (or statement) showing both sides are equal. This can also be scored via the substitution of  $\mu = -1$   $\lambda = -2$  into **both** equations of the lines resulting in the same coordinate.

ddM1 Substitutes their value of  $\lambda$  into  $l_1$  to find the coordinates or position vector of the point of intersection. It is dependent upon having scored both methods so far.

Alternatively substitutes their value of  $\mu$  into  $l_2$  to find the coordinates or position vector of the point of intersection. It may be implied by 2 out of 3 correct coordinates.

A1 Correct answer only. Accept as a vector or a coordinate. Accept (-3, 3, 7)

(b)

M1 A clear attempt to find the scalar product of the gradient vectors  $\begin{pmatrix} 2 \\ 1 \\ -1 \end{pmatrix} \cdot \begin{pmatrix} 3 \\ -1 \\ 5 \end{pmatrix}$

You must see an attempt to multiply and add. Eg  $2 \times 3 + 1 \times -1 + -1 \times 5$  or  $6 - 1 - 5$ . Allow for slips.

A1 The above method must be followed by a reason and a conclusion. The scalar product must be zero. Accept '=0, hence perpendicular'. Accept '=0, therefore proven'

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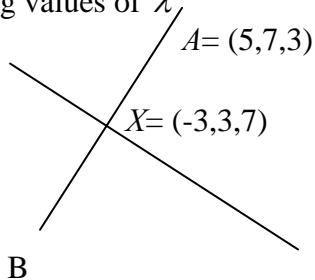
M1 An attempt to find the vector  $\overrightarrow{AX}$  where  $X$  is their point of intersection using  $\overrightarrow{AX} = \overrightarrow{OX} - \overrightarrow{OA}$   
This is scored if the 'difference' between the vectors or coordinates are attempted

M1 Attempts to find the coordinate or vector of  $B$  using  $\overrightarrow{OB} = \overrightarrow{OX} + \overrightarrow{AX}$  or  $\overrightarrow{OB} = \overrightarrow{OA} + 2 \times \overrightarrow{AX}$   
Allow a misunderstanding on the direction of  $\overrightarrow{AX}$

A1 Correct answer only.  $\overrightarrow{OB} = \begin{pmatrix} -11 \\ -1 \\ 11 \end{pmatrix}$  or  $-11i - 1j + 11k$

Do NOT accept the coordinate for this mark. Correct answer with no working scores all 3 marks.  
The correct coordinate would score 2 out of 3.

(c Alt) Using values of  $\lambda$



M1 Attempts to find  $\lambda$  on  $l_1$  at  $X$  ( $\lambda = -2$ ) and  $A$  ( $\lambda = 2$ )

M1 Uses the difference between  $\lambda$  values to find  $\lambda$  (-6) at  $B$

A1 cao



Question Number	Scheme	Marks
11(a)	$6 \sin t = 3 \Rightarrow \sin t = 0.5 \Rightarrow t = \frac{\pi}{6}$	B1  <b>(1)</b>
(b)	$\frac{dy}{dx} = \frac{dy/dt}{dx/dt} = \frac{6 \cos t}{-20 \sin 2t}$	M1A1
	Sub $t = \frac{\pi}{6}$ into $\frac{dy}{dx} = \frac{6 \cos t}{-20 \sin 2t} = \frac{6 \cos\left(\frac{\pi}{6}\right)}{-20 \sin\left(\frac{\pi}{3}\right)} = -\frac{3}{10}$	M1A1
	Uses normal gradient with (5, 3) $\Rightarrow \frac{y-3}{x-5} = \frac{10}{3}$ $\Rightarrow 3y = 10x - 41$	M1 A1* <b>(6)</b>
©	Sub $x = 10 \cos 2t$ , $y = 6 \sin t$ , into $3y = 10x - 41$ $\Rightarrow 18 \sin t = 100 \cos 2t - 41$ $\Rightarrow 18 \sin t = 100(1 - 2 \sin^2 t) - 41$ $\Rightarrow 200 \sin^2 t + 18 \sin t - 59 = 0$ $\Rightarrow (2 \sin t - 1)(100 \sin t + 59) = 0$ $\Rightarrow \sin t = -\frac{59}{100} (\Rightarrow t = -0.63106\dots)$ Using either their $t$ or $\sin t$ to find either coord of B Hence B has co-ordinates (3.038, - 3.54). These are exact values The equivalent fractional answers are $\left(\frac{1519}{500}, -\frac{177}{50}\right)$	M1  M1, A1  M1A1 M1 A1,A1  <b>(8)</b>  <b>(15 marks)</b>

Notes for Question 11

(a)

B1  $t = \frac{\pi}{6}$  Accept awrt 0.5236 (4dp). Answers in degrees  $30^\circ$  is B0

(b)

M1 Uses  $\frac{dy}{dx} = \frac{dy/dt}{dx/dt}$  and differentiates to obtain a gradient function of the form  $\frac{A \cos t}{B \sin 2t}$ A1  $\frac{dy}{dx} = \frac{6 \cos t}{-20 \sin 2t} = \left( -\frac{3 \cos t}{10 \sin 2t} \right)$ . There is no requirement to simplify this.M1 Substitutes their value of  $t$  (from part a) into their  $\frac{dy}{dx}$  to get a numerical value for the gradient.Accept also their  $t$  being substituted into  $\frac{dx}{dy}$  or  $-\frac{dx}{dy}$ A1 Achieves a correct numerical answer for  $\frac{dy}{dx} = -\frac{3}{10} \left( \frac{dx}{dy} = -\frac{10}{3} \text{ or } -\frac{dx}{dy} = \frac{10}{3} \right)$ .It needs to be attributed to the correct derivative. Do not accept  $\frac{dx}{dy} = -\frac{3}{10}$ 

This may be implied by the correct value in the gradient of the normal.

M1 Award for a correct method to find the equation of the normal.

They must use (5, 3) and their numerical value of  $-\frac{dx}{dy}$ . Eg  $\frac{y-5}{x-3} = -\frac{dx}{dy}$ If  $y = mx + c$  is used then it must be a full method using (5, 3) and with  $m = -\frac{dx}{dy}$  as far as  $c = ..$ A1\* cso. This is a proof and you must be convinced of all aspects including the sight of an intermediate line between  $\frac{y-3}{x-5} = \frac{10}{3}$  and  $3y = 10x - 41$ 

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M1 An attempt to substitute both  $x = 10 \cos 2t$  and  $y = 6 \sin t$  into  $3y = 10x - 41$  forming a trigonometrical equation in just the variable  $t$ .M1 Uses the identity  $\cos 2t = 1 - 2 \sin^2 t$  and rearranges to produce a quadratic equation in  $\sin t$ . If the identity  $\cos 2t = \cos^2 t - \sin^2 t$  or  $\cos 2t = 2 \cos^2 t - 1$  is used instead, one further step, using the identity  $\cos^2 t = 1 - \sin^2 t$ , must be seen before the mark can be awarded.A1 A correct  $3TQ=0$  in  $\sin t$ . Look for  $200 \sin^2 t + 18 \sin t - 59 = 0$  or equivalent.M1 For a correct attempt at solving the  $3TQ=0$  (usual rules) in  $\sin t$ . Accept a correct answer (from a graphical calculator) as justification.A1 Award for either  $\sin t = -\frac{59}{100}$  oe or  $t = -0.63..$ M1 Using either their  $t$  or  $\sin t$  to find either the  $x$  or  $y$  coordinate of  $B$ . Accept as evidence sight of  $10 \cos 2 \times 't'$  or  $6 \sin 't'$  or one correct answer (awrt 2dp).

A1 One coordinate both correct and exact. These are exact answers (3.038, - 3.54).

A1 Both coordinates correct and exact. Cso and cao (3.038, - 3.54).

Alternative solution to parts b and c using the Cartesian equation of C

Question Number	Scheme	Marks
<b>Alt11(b)</b>	$x = 10(1 - 2\sin^2 t) \Rightarrow x = 10 - \frac{5}{9}y^2$ $\frac{dx}{dy}_{y=3} = -\frac{10y}{9} = -\frac{10 \times 3}{9} = -\frac{10}{3}$ $\frac{y-3}{x-5} = \frac{10}{3} \Rightarrow 3y = 10x - 41$	<p>M1A1</p> <p>M1A1</p> <p>M1A1</p> <p style="text-align: right;"><b>(6)</b></p>
<b>Alt(c)</b>	<p>Sub <math>x = 10 - \frac{5}{9}y^2</math> into <math>3y = 10x - 41 \Rightarrow 3y = 10\left(10 - \frac{5}{9}y^2\right) - 41</math></p> $\Rightarrow 50y^2 + 27y - 531 = 0$ $\Rightarrow (y-3)(50y+177) = 0$ $\Rightarrow y = \dots$ <p>Substitutes <math>y = \dots</math> into <math>x = 10 - \frac{5}{9}y^2</math></p> $\Rightarrow x = 3.038, y = -3.54$	<p>M1</p> <p>M1A1</p> <p>M1A1</p> <p>M1</p> <p>A1A1</p> <p style="text-align: right;"><b>(8)</b></p>
<b>Alt(c)</b>	<p>Sub <math>y = 6\sqrt{\frac{10-x}{20}}</math> into <math>3y = 10x - 41 \Rightarrow 36\sqrt{\frac{10-x}{20}} = 10x - 41</math></p> $\Rightarrow 36^2 \left(\frac{10-x}{20}\right) = (10x-41)^2$ $\Rightarrow 500x^2 - 4019x + 7595 = 0$ $\Rightarrow (500x - 1519)(x - 5) = 0$ <p>Substitutes <math>x = \dots</math> into <math>y = 6\sqrt{\frac{10-x}{20}}</math></p> $\Rightarrow x = 3.038, y = -3.54$	<p>M1</p> <p>M1A1</p> <p>M1A1</p> <p>M1</p> <p>A1A1</p> <p style="text-align: right;"><b>(8)</b></p>

Notes for Question 11

(b)

M1 Uses the double angle formula  $\cos 2t = 1 - 2\sin^2 t$  to get the equation of C in the form  $x = f(y^2)$ .A1 The correct equation is obtained. That is  $x = 10 - \frac{5}{9}y^2$  or equivalent  $x = 10 \left( 1 - 2 \left( \frac{y}{6} \right)^2 \right)$ M1 Differentiates wrt  $y$  (usual rules) and subs  $y=3$  to get a numerical value to  $\frac{dx}{dy}$ A1  $\frac{dx}{dy} = -\frac{10}{3}$  This may be implied by the correct value in the gradient of the normal.

M1 Award for a correct method to find the equation of the normal.

They must use (5, 3) and their numerical value of  $-\frac{dx}{dy}$ . Eg  $\frac{y-5}{x-3} = -\frac{dx}{dy}$ If  $y = mx + c$  is used then it must be a full method with (5, 3) and with  $m = -\frac{dx}{dy}$  " as far as  $c = ..$ 

A1\* cso. This is a proof and you must be convinced of all aspects including the last line of

$$\frac{y-3}{x-5} = \frac{10}{3} \Rightarrow 3y = 10x - 41$$

(c)

M1 Sub **their**  $x = 10 - \frac{5}{9}y^2$  into  $3y = 10x - 41$  to produce an equation in  $y$ Alternatively subs **their**  $y = 6\sqrt{\frac{10-x}{20}}$  into  $3y = 10x - 41$  to produce an equation in  $x$ M1 Forms a quadratic equation in  $y$  (or  $x$ )A1 For achieving  $50y^2 + 27y - 531 = 0$  /  $500x^2 - 4019x + 7595 = 0$  or equivalentM1 For a correct attempt at solving the 3TQ=0 in  $y$  (or  $x$ ).

If you see the answers you can award this. We are accepting answers from a calculator.

A1 Correct factors. If the correct  $y$  (or  $x$ ) is given then this mark is automatically awarded.M1 Substitutes their  $y =$  into their  $x = f(y^2) \Rightarrow x = ..$  or vice versaA1 One correct, either  $x = 3.038$  or  $y = -3.54$  The values must be exactA1 Both correct.  $x = 3.038$  and  $y = -3.54$ 

$$\text{Accept } x = \frac{1519}{500}, y = -\frac{177}{50},$$

Question Number	Scheme	Marks
<p><b>12(a)</b></p>	$y^2 = (x(\sin x + \cos x))^2 = x^2(\sin x + \cos x)^2$ $= x^2(\sin^2 x + \cos^2 x + 2\sin x \cos x)$ $= x^2(1 + \sin 2x)$ $V = \int_0^{\frac{\pi}{4}} \pi y^2 dx = \int_0^{\frac{\pi}{4}} \pi x^2(1 + \sin 2x) dx$	<p>M1 A1 A1*</p> <p>(3)</p>
<p><b>(b)</b></p>	$V = \int_0^{\frac{\pi}{4}} \pi x^2(1 + \sin 2x) dx = \int_0^{\frac{\pi}{4}} (\pi x^2 + \pi x^2 \sin 2x) dx$ $= \int_0^{\frac{\pi}{4}} \pi x^2 dx + \int_0^{\frac{\pi}{4}} \pi x^2 \sin 2x dx$ $\int_0^{\frac{\pi}{4}} \pi x^2 dx = \left[ \pi \frac{x^3}{3} \right]_0^{\frac{\pi}{4}} = \pi \frac{\left(\frac{\pi}{4}\right)^3}{3} \quad \text{OR} \quad \int_0^{\frac{\pi}{4}} x^2 dx = \left[ \frac{x^3}{3} \right]_0^{\frac{\pi}{4}} = \frac{\left(\frac{\pi}{4}\right)^3}{3}$ $\cancel{\int x^2 \sin 2x dx = \cancel{\left( \pm Bx^2 \cos 2x \pm C \int x \cos 2x dx \right)}}$ $= \cancel{\left( -x^2 \frac{\cos 2x}{2} + \int x \cos 2x dx \right)}$ $= \cancel{\left( \pm Bx^2 \cos 2x \pm Cx \sin 2x \pm \int D \sin 2x dx \right)}$ $= \cancel{\left( -x^2 \frac{\cos 2x}{2} + x \frac{\sin 2x}{2} + \frac{\cos 2x}{4} \right)}$ $\cancel{\int_{x=0}^{x=\frac{\pi}{4}} x^2 \sin 2x dx = \cancel{\left[ \pm Bx^2 \cos 2x \pm Cx \sin 2x \pm D \cos 2x \right]_0^{\frac{\pi}{4}} = \cancel{\left( \frac{\pi}{8} - \frac{1}{4} \right)}}$ $V = \int_0^{\frac{\pi}{4}} \pi x^2(1 + \sin 2x) dx = \int_0^{\frac{\pi}{4}} \pi x^2 dx + \int_0^{\frac{\pi}{4}} \pi x^2 \sin 2x dx$ $= \left( \frac{\pi^4}{192} \right) + \left( \frac{\pi^2}{8} - \frac{\pi}{4} \right)$	<p>M1A1 M1 A1 dM1 A1 ddM1 oe A1,A1</p> <p>(9) (12 marks)</p>

Notes for Question 12

(a)  
M1 For squaring  $y$  AND attempting to multiply out the bracket. The minimum requirement is that  $y^2 = x^2(\sin^2 x + \cos^2 x + \dots)$ . There is no need to include ' $\pi$ ' for this mark.

A1 Using  $\sin^2 x + \cos^2 x = 1$  **and**  $2\sin x \cos x = \sin 2x$  to achieve  $y^2 = x^2(1 + \sin 2x)$   
There is no need to include ' $\pi$ ' for this mark.  
You may accept  $\sin^2 x + 2\sin x \cos x + \cos^2 x = 1 + \sin 2x$

A1\* It must be stated or implied that  $V = \int_0^{\frac{\pi}{4}} \pi y^2 dx$ .

It may be implied by replacing  $y^2$  by  $(x(\sin x + \cos x))^2$

A correct proof must follow involving all that is required for the previous M1A1

The limits could just appear in the final line without any explanation. Note that this is a given answer

(b)

M1 For splitting the given integral into a sum **and** integrating  $x^2$  or  $\pi x^2$  to  $Ax^3$ .  
There is no need for limits at this stage

A1  $\int_0^{\frac{\pi}{4}} x^2 dx = \left[ \frac{x^3}{3} \right]_0^{\frac{\pi}{4}} = \frac{\left(\frac{\pi}{4}\right)^3}{3}$ . There is no need to simplify this. Accept  $\int_0^{\frac{\pi}{4}} \pi x^2 dx = \pi \left[ \frac{x^3}{3} \right]_0^{\frac{\pi}{4}} = \pi \frac{\left(\frac{\pi}{4}\right)^3}{3}$

M1 For integrating  $\int \pi x^2 \sin 2x dx$  or  $\int x^2 \sin 2x dx$  by parts. The integration must be the correct way

around. There is no need for limits. If the rule is quoted it must be correct, a version of which appears in the formula booklet.

Accept for this mark expressions of the form  $\int x^2 \sin 2x dx = \pm Bx^2 \cos 2x \pm \int Cx \cos 2x dx$

A1  $\int x^2 \sin 2x dx = -x^2 \frac{\cos 2x}{2} + \int x \cos 2x dx$  OR  $\int \pi x^2 \sin 2x dx = -\pi x^2 \frac{\cos 2x}{2} + \int \pi x \cos 2x dx$

dm1 A second application by parts, the correct way around. No need for limits. See the previous M1 for how to award. It is dependent upon this having been awarded.

Look for  $\int x^2 \sin 2x dx = \pm Bx^2 \cos 2x \pm Cx \sin 2x \pm \int D \sin 2x dx$

A1 A fully correct answer to the integral of  $\int x^2 \sin 2x dx = -x^2 \frac{\cos 2x}{2} + x \frac{\sin 2x}{2} + \frac{\cos 2x}{4}$

ddM1 For substituting in both limits and subtracting. The two M's for int by parts must have been scored.

A1 Either of  $\left(\frac{\pi^4}{192}\right)$  linked to first M or  $\left(\frac{\pi^2}{8} - \frac{\pi}{4}\right)$  linked to ddM. Accept in the form  $\pi \left(\frac{\pi^3}{192} + \dots\right)$

A1 Correct answer and correct solution only. Accept exact equivalents  $V = \pi \left(\frac{\pi^3}{192} + \frac{\pi}{8} - \frac{1}{4}\right)$

Alt way (2)- Where candidate does not split up first.

<p>(b)</p>	$V = \int_0^{\frac{\pi}{4}} x^2(1 + \sin 2x) dx = x^2(x \pm A \cos 2x) - \int Bx(x \pm A \cos 2x) dx$ $= x^2\left(x - \frac{\cos 2x}{2}\right) - \int_0^{\frac{\pi}{4}} 2x\left(x - \frac{\cos 2x}{2}\right) dx$ $= x^2\left(x \pm A \cos 2x\right) - Bx\left(Cx^2 \pm D \sin 2x\right) \pm \int_0^{\frac{\pi}{4}} Ex^2 \pm F \sin 2x dx$ $= x^2\left(x - \frac{\cos 2x}{2}\right) - 2x\left(\frac{x^2}{2} - \frac{\sin 2x}{4}\right) + \int_0^{\frac{\pi}{4}} 2\left(\frac{x^2}{2} - \frac{\sin 2x}{4}\right) dx$ $= x^2\left(x - \frac{\cos 2x}{2}\right) - 2x\left(\frac{x^2}{2} - \frac{\sin 2x}{4}\right) + 2\left(\frac{x^3}{6} + \frac{\cos 2x}{8}\right)$ $V = x^2\left[x - \frac{\cos 2x}{2}\right] - 2x\left[\frac{x^2}{2} - \frac{\sin 2x}{4}\right] + 2\left[\frac{x^3}{6} + \frac{\cos 2x}{8}\right] \Bigg _0^{\frac{\pi}{4}}$ $= \frac{\pi^4}{192}, + \frac{\pi^2}{8} - \frac{\pi}{4}$	<p>2<sup>nd</sup> M1</p> <p>A1</p> <p>3<sup>rd</sup> dM1</p> <p>A1</p> <p>1<sup>st</sup> M1A1</p> <p>ddM1</p> <p>A1, A1</p>
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(9)

1<sup>ST</sup> M1,A1 Seen after two (not necessarily) correct applications of integration by parts, it is for integrating the  $x^2$  term

2<sup>nd</sup> M1A1 It is for the first attempt at an application of integration by parts on  $\int x^2(1 + \sin 2x) dx$

Look for  $x^2(x \pm A \cos 2x) - \int_0^{\frac{\pi}{4}} Bx(x \pm A \cos 2x) dx$  for the method

3<sup>rd</sup> dM1A1 It is for a further attempt at an application of integration by parts the correct way around. It is dependent upon the first method having been awarded.

Look for  $= x^2(x \pm A \cos 2x) - Bx(Cx^2 \pm D \sin 2x) \pm \int_0^{\frac{\pi}{4}} Ex^2 \pm F \sin 2x dx$

