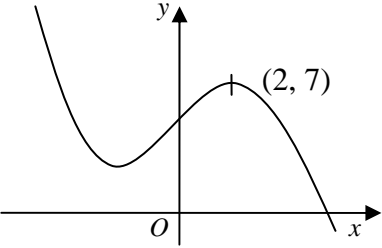
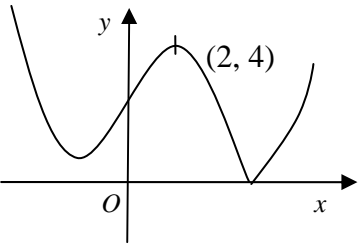
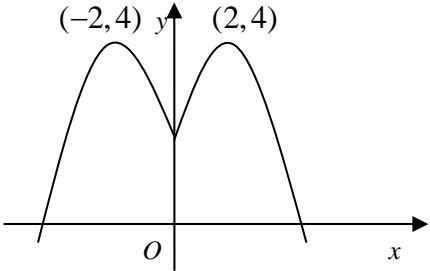


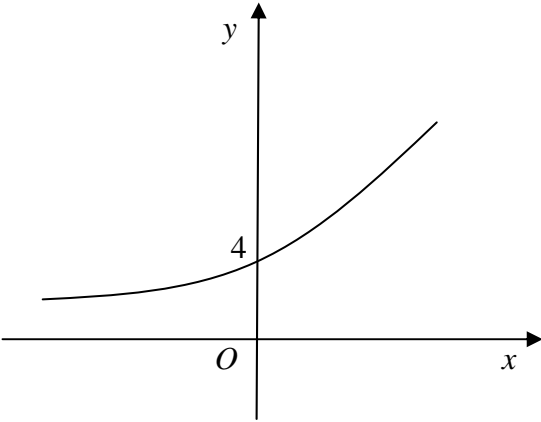
Question Number	Scheme	Marks
1.	(a) 	Shape unchanged Point B1 B1 <b>(2)</b>
	(b) 	Shape Point B1 B1 <b>(2)</b>
	(c) 	Shape (2, 4) (-2, 4) B1 B1 B1 <b>(3)</b> <b>[7]</b>

Question Number	Scheme	Marks
2.	$x^2 - x - 2 = (x - 2)(x + 1)$ <p>At any stage</p> $\frac{2x^2 + 3x}{(2x + 3)(x - 2)} = \frac{x(2x + 3)}{(2x + 3)(x - 2)} = \frac{x}{x - 2}$ $\frac{2x^2 + 3x}{(2x + 3)(x - 2)} - \frac{6}{x^2 - x - 2} = \frac{x(x + 1) - 6}{(x - 2)(x + 1)}$ $= \frac{x^2 + x - 6}{(x - 2)(x + 1)}$ $= \frac{(x + 3)(x - 2)}{(x - 2)(x + 1)}$ $= \frac{x + 3}{x + 1}$ <p>Alternative method</p> $x^2 - x - 2 = (x - 2)(x + 1)$ <p>At any stage</p> <p><math>(2x + 3)</math> appearing as a factor of the numerator at any stage</p> $\frac{2x^2 + 3x}{(2x + 3)(x - 2)} - \frac{6}{(x - 2)(x + 1)} = \frac{(2x^2 + 3x)(x + 1) - 6(2x + 3)}{(2x + 3)(x - 2)(x + 1)}$ $= \frac{2x^3 + 5x^2 - 9x - 18}{(2x + 3)(x - 2)(x + 1)}$ <p>can be implied</p> $= \frac{(x - 2)(2x^2 + 9x + 9)}{(2x + 3)(x - 2)(x + 1)} \quad \text{or} \quad \frac{(2x + 3)(x^2 + x - 6)}{(2x + 3)(x - 2)(x + 1)} \quad \text{or} \quad \frac{(x + 3)(2x^2 - x - 6)}{(2x + 3)(x - 2)(x + 1)}$ <p>Any one linear factor <math>\times</math> quadratic</p> $= \frac{(2x + 3)(x - 2)(x + 3)}{(2x + 3)(x - 2)(x + 1)}$ <p>Complete factors</p> $= \frac{x + 3}{x + 1}$	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1 A1</p> <p>A1 (7)</p> <p>[7]</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>(7)</p>

Question Number	Scheme	Marks
3.	$\frac{dy}{dx} = \frac{1}{x}$ <p>accept <math>\frac{3}{3x}</math></p> $\text{At } x = 3, \frac{dy}{dx} = \frac{1}{3} \Rightarrow m' = -3$ <p>Use of <math>mm' = -1</math></p> $y - \ln 1 = -3(x - 3)$ $y = -3x + 9$ <p>Accept <math>y = 9 - 3x</math></p> <p><math>\frac{dy}{dx} = \frac{1}{3x}</math> leading to <math>y = -9x + 27</math> is a maximum of</p>	<p>M1 A1</p> <p>M1</p> <p>M1</p> <p>A1 (5) [5]</p>
4.	<p>(a) (i)</p> $\frac{d}{dx}(e^{3x+2}) = 3e^{3x+2} \quad (\text{or } 3e^2 e^{3x})$ <p>At any stage</p> $\frac{dy}{dx} = 3x^2 e^{3x+2} + 2x e^{3x+2}$ <p>Or equivalent</p> <p>(ii)</p> $\frac{d}{dx}(\cos(2x^3)) = -6x^2 \sin(2x^3)$ <p>At any stage</p> $\frac{dy}{dx} = \frac{-18x^3 \sin(2x^3) - 3 \cos(2x^3)}{9x^2}$ <p>Alternatively using the product rule for second</p> $y = (3x)^{-1} \cos(2x^3)$ $\frac{dy}{dx} = -3(3x)^{-2} \cos(2x^3) - 6x^2 (3x)^{-1} \sin(2x^3)$ <p>Accept equivalent unsimplified forms</p> <p>(b)</p> $1 = 8 \cos(2y + 6) \frac{dy}{dx} \quad \text{or} \quad \frac{dx}{dy} = 8 \cos(2y + 6)$ $\frac{dy}{dx} = \frac{1}{8 \cos(2y + 6)}$ $\frac{dy}{dx} = \frac{1}{8 \cos\left(\arcsin\left(\frac{x}{4}\right)\right)} \quad \left( = (\pm) \frac{1}{2\sqrt{(16-x^2)}} \right)$	<p>B1</p> <p>M1 A1+A1 (4)</p> <p>M1 A1</p> <p>M1 A1 (4)</p> <p>M1</p> <p>M1 A1</p> <p>M1 A1 (5) [13]</p>

Question Number	Scheme	Marks
5.	<p>(a) <math>2x^2 - 1 - \frac{4}{x} = 0</math> Dividing equation by <math>x</math> M1</p> <p><math>x^2 = \frac{1}{2} + \frac{4}{2x}</math> Obtaining <math>x^2 = \dots</math> M1</p> <p><math>x = \sqrt{\left(\frac{2}{x} + \frac{1}{2}\right)} *</math> cso A1 (3)</p>	
	<p>(b) <math>x_1 = 1.41, x_2 = 1.39, x_3 = 1.39</math> B1, B1, B1</p> <p>If answers given to more than 2 dp, penalise first time then accept awrt above. (3)</p>	
	<p>(c) Choosing (1.3915, 1.3925) or a tighter interval M1</p> <p><math>f(1.3915) \approx -3 \times 10^{-3}, f(1.3925) \approx 7 \times 10^{-3}</math> Both, awrt A1</p> <p>Change of sign (and continuity) <math>\Rightarrow \alpha \in (1.3915, 1.3925)</math></p> <p><math>\Rightarrow \alpha = 1.392</math> to 3 decimal places * cso A1 (3)</p>	[9]
6.	<p>(a) <math>R \cos \alpha = 12, R \sin \alpha = 4</math></p> <p><math>R = \sqrt{12^2 + 4^2} = \sqrt{160}</math> Accept if just written down, awrt 12.6 M1 A1</p> <p><math>\tan \alpha = \frac{4}{12}, \Rightarrow \alpha \approx 18.43^\circ</math> awrt <math>18.4^\circ</math> M1, A1(4)</p>	
	<p>(b) <math>\cos(x + \text{their } \alpha) = \frac{7}{\text{their } R} (\approx 0.5534)</math> M1</p> <p><math>x + \text{their } \alpha = 56.4^\circ</math> awrt <math>56^\circ</math> A1</p> <p><math>= \dots, 303.6^\circ</math> <math>360^\circ - \text{their principal value}</math> M1</p> <p><math>x = 38.0^\circ, 285.2^\circ</math> Ignore solutions out of range A1, A1 (5)</p> <p>If answers given to more than 1 dp, penalise first time then accept awrt above.</p>	
	<p>(c)(i) minimum value is <math>-\sqrt{160}</math> ft their <math>R</math> B1ft</p>	
	<p>(ii) <math>\cos(x + \text{their } \alpha) = -1</math> M1</p> <p><math>x \approx 161.57^\circ</math> cao A1 (3)</p>	[12]

Question Number	Scheme	Marks
7.	(a) (i) Use of $\cos 2x = \cos^2 x - \sin^2 x$ in an attempt to prove the identity. $\frac{\cos 2x}{\cos x + \sin x} = \frac{\cos^2 x - \sin^2 x}{\cos x + \sin x} = \frac{(\cos x - \sin x)(\cos x + \sin x)}{\cos x + \sin x} = \cos x - \sin x$ * cso	M1 A1 (2)
	(ii) Use of $\cos 2x = 2\cos^2 x - 1$ in an attempt to prove the identity. Use of $\sin 2x = 2\sin x \cos x$ in an attempt to prove the identity. $\frac{1}{2}(\cos 2x - \sin 2x) = \frac{1}{2}(2\cos^2 x - 1 - 2\sin x \cos x) = \cos^2 x - \cos x \sin x - \frac{1}{2}$ * cso	M1 M1 A1 (3)
	(b) $\cos \theta (\cos \theta - \sin \theta) = \frac{1}{2}$ $\cos^2 \theta - \cos \theta \sin \theta - \frac{1}{2} = 0$ $\frac{1}{2}(\cos 2\theta - \sin 2\theta) = 0$ $\cos 2\theta = \sin 2\theta$ *	Using (a)(i) M1   Using (a)(ii) M1 A1 (3)
	(c) $\tan 2\theta = 1$ $2\theta = \frac{\pi}{4}, \left(\frac{5\pi}{4}, \frac{9\pi}{4}, \frac{13\pi}{4}\right)$ $\theta = \frac{\pi}{8}, \frac{5\pi}{8}, \frac{9\pi}{8}, \frac{13\pi}{8}$ Obtaining at least 2 solutions in range The 4 correct solutions	M1 A1  M1 A1 (4)
	If decimals (0.393, 1.963, 3.534, 5.105) or degrees (22.5°, 112.5°, 202.5°, 292.5°) are given, but all 4 solutions are found, penalise one A mark only. Ignore solutions out of range.	[12]

Question Number	Scheme	Marks
8.	<p>(a)</p> $\begin{aligned} \text{gf}(x) &= e^{2(2x+\ln 2)} \\ &= e^{4x} e^{2\ln 2} \\ &= e^{4x} e^{\ln 4} \\ &= 4e^{4x} \end{aligned}$ <p>(Hence <math>\text{gf} : x \mapsto 4e^{4x}, \quad x \in \mathbb{R}</math>)</p> <p>(b)</p>  <p>(c)</p> <p>Range is <math>\mathbb{R}_+</math></p> <p>(d)</p> $\begin{aligned} \frac{d}{dx}[\text{gf}(x)] &= 16e^{4x} \\ e^{4x} &= \frac{3}{16} \\ 4x &= \ln \frac{3}{16} \\ x &\approx -0.418 \end{aligned}$	<p>M1 M1 M1 A1 (4)</p> <p>Give mark at this point, cso</p> <p>Shape and point B1 (1)</p> <p>Accept <math>\text{gf}(x) &gt; 0, y &gt; 0</math> B1 (1)</p> <p>M1 A1 M1 A1 (4) [10]</p>