

Question Number	Scheme	Marks												
1.	<p>Differentiates</p> <p>to obtain : $6x + 8y \frac{dy}{dx} - 2,$ + $(6x \frac{dy}{dx} + 6y) = 0$ $\left[\frac{dy}{dx} = \frac{2 - 6x - 6y}{6x + 8y} \right]$</p> <p>Substitutes $x = 1, y = -2$ into expression involving $\frac{dy}{dx}$, to give $\frac{dy}{dx} = -\frac{8}{10}$</p> <p>Uses line equation with numerical ‘gradient’ $y - (-2) = (\text{their gradient})(x - 1)$ or finds c and uses $y = (\text{their gradient}) x + "c"$</p> <p>To give $5y + 4x + 6 = 0$ (or equivalent = 0)</p>	M1 A1, +(B1) M1, A1 M1 A1√ [7]												
2. (a)	<table><tr><td>x</td><td>0</td><td>$\frac{\pi}{16}$</td><td>$\frac{\pi}{8}$</td><td>$\frac{3\pi}{16}$</td><td>$\frac{\pi}{4}$</td></tr><tr><td>y</td><td>1</td><td>1.01959</td><td>1.08239</td><td>1.20269</td><td>1.41421</td></tr></table> <p>M1 for one correct, A1 for all correct</p>	x	0	$\frac{\pi}{16}$	$\frac{\pi}{8}$	$\frac{3\pi}{16}$	$\frac{\pi}{4}$	y	1	1.01959	1.08239	1.20269	1.41421	M1 A1 (2)
x	0	$\frac{\pi}{16}$	$\frac{\pi}{8}$	$\frac{3\pi}{16}$	$\frac{\pi}{4}$									
y	1	1.01959	1.08239	1.20269	1.41421									
(b)	<p>Integral = $\frac{1}{2} \times \frac{\pi}{16} \times \{1 + 1.4142 + 2(1.01959 + \dots + 1.20269)\}$ $\left(= \frac{\pi}{32} \times 9.02355 \right) = 0.8859$</p>	M1 A1√ A1 cao (3)												
(c)	<p>Percentage error = $\frac{approx - 0.88137}{0.88137} \times 100 = 0.51\%$ (allow 0.5% to 0.54% for A1)</p> <p>M1 gained for $(\pm) \frac{approx - \ln(1 + \sqrt{2})}{\ln(1 + \sqrt{2})}$</p>	M1 A1 (2) [7]												

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3.	<p>Uses substitution to obtain $x = f(u) \left[\frac{u^2 + 1}{2} \right]$,</p> <p>and to obtain $u \frac{du}{dx} = \text{const. or equiv.}$</p> <p>Reaches $\int \frac{3(u^2 + 1)}{2u} u du$ or equivalent</p> <p>Simplifies integrand to $\int \left(3u^2 + \frac{3}{2} \right) du$ or equiv.</p> <p>Integrates to $\frac{1}{2}u^3 + \frac{3}{2}u$</p> <p>A1✓ dependent on all previous Ms</p> <p>Uses new limits 3 and 1 substituting and subtracting (or returning to function of x with old limits)</p> <p>To give 16 cso</p> <hr/> <p>“By Parts” Attempt at “right direction” by parts M1</p> $\left[3x \left(2x - 1 \right)^{\frac{1}{2}} \right] - \left\{ \int 3 \left(2x - 1 \right)^{\frac{1}{2}} dx \right\}$ <p>..... $- \left(2x - 1 \right)^{\frac{3}{2}}$ M1A1✓</p> <p>Uses limits 5 and 1 correctly; [42 – 26] 16 M1A1</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1 A1✓</p> <p>M1</p> <p>A1</p> <p>[8]</p>

4.	<p>Attempts $V = \pi \int x^2 e^{2x} dx$</p> $= \pi \left[\frac{x^2 e^{2x}}{2} - \int x e^{2x} dx \right]$ <p>(M1 needs parts in the correct direction)</p> $= \pi \left[\frac{x^2 e^{2x}}{2} - \left(\frac{x e^{2x}}{2} - \int \frac{e^{2x}}{2} dx \right) \right]$ <p>(M1 needs second application of parts)</p> <p>M1A1✓ refers to candidates $\int x e^{2x} dx$, but dependent on prev. M1</p> $= \pi \left[\frac{x^2 e^{2x}}{2} - \left(\frac{x e^{2x}}{2} - \frac{e^{2x}}{4} \right) \right]$ <p>A1 cao</p> <p>Substitutes limits 3 and 1 and subtracts to give... [dep. on second and third Ms]</p> <p>dM1</p> $= \pi \left[\frac{13}{4} e^6 - \frac{1}{4} e^2 \right] \text{ or any correct exact equivalent.}$ <p>A1</p> <p>[Omission of π loses first and last marks only]</p>	<p>M1</p> <p>M1 A1</p> <p>M1 A1✓</p> <p>A1 cao</p> <p>dM1</p> <p>A1</p> <p>[8]</p>
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5. (a)	<p>Considers $3x^2 + 16 = A(2+x)^2 + B(1-3x)(2+x) + C(1-3x)$</p> <p>and substitutes $x = -2$, or $x = 1/3$,</p> <p>or compares coefficients and solves simultaneous equations</p> <p>To obtain $A = 3$, and $C = 4$</p> <p>Compares coefficients or uses simultaneous equation to show $B = 0$.</p>	<p>M1</p> <p>A1, A1</p> <p>B1</p> <p>(4)</p>
(b)	<p>Writes $3(1-3x)^{-1} + 4(2+x)^{-2}$</p> <p>$= 3(1+3x, +9x^2 + 27x^3 + \dots) +$</p> $\frac{4}{4}(1 + \frac{(-2)}{1}\left(\frac{x}{2}\right) + \frac{(-2)(-3)}{1.2}\left(\frac{x}{2}\right)^2 + \frac{(-2)(-3)(-4)}{1.2.3}\left(\frac{x}{2}\right)^3 + \dots)$ <p>$= 4 + 8x, + 27\frac{3}{4}x^2 + 80\frac{1}{2}x^3 + \dots$</p> <p>Or uses $(3x^2 + 16)(1-3x)^{-1}(2+x)^{-2}$</p> <p>$(3x^2 + 16)(1+3x, +9x^2 + 27x^3 +) \times$</p> $\frac{1}{4}(1 + \frac{(-2)}{1}\left(\frac{x}{2}\right) + \frac{(-2)(-3)}{1.2}\left(\frac{x}{2}\right)^2 + \frac{(-2)(-3)(-4)}{1.2.3}\left(\frac{x}{2}\right)^3)$ <p>$= 4 + 8x, + 27\frac{3}{4}x^2 + 80\frac{1}{2}x^3 + \dots$</p>	<p>M1</p> <p>(M1, A1)</p> <p>(M1 A1)</p> <p>A1, A1</p> <p>(7)</p> <p>M1</p> <p>(M1A1)×</p> <p>(M1A1)</p> <p>A1, A1</p> <p>(7)</p> <p>[11]</p>

6. (a)	$\lambda = -4 \rightarrow a = 18, \quad \mu = 1 \rightarrow b = 9$	M1 A1, A1 (3)
(b)	$\begin{pmatrix} 8+\lambda \\ 12+\lambda \\ 14-\lambda \end{pmatrix} \bullet \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix} = 0$ $\therefore 8 + \lambda + 12 + \lambda - 14 + \lambda = 0$ <p>Solves to obtain λ ($\lambda = -2$)</p> <p>Then substitutes value for λ to give P at the point (6, 10, 16) (any form)</p>	M1 A1 dM1 M1, A1 (5)
(c)	$OP = \sqrt{36 + 100 + 256}$ $(= \sqrt{392}) = 14\sqrt{2}$	M1 A1 cao (2) [10]
7. (a)	$\frac{dV}{dr} = 4\pi r^2$	B1 (1)
(b)	Uses $\frac{dr}{dt} = \frac{dV}{dt} \cdot \frac{dr}{dV}$ in any form, $= \frac{1000}{4\pi r^2 (2t+1)^2}$	M1, A1 (2)
(c)	$V = \int 1000(2t+1)^{-2} dt$ and integrate to $p (2t+1)^{-1}, \quad = -500(2t+1)^{-1} (+c)$ <p>Using $V=0$ when $t=0$ to find c, ($c = 500$, or equivalent)</p> $\therefore V = 500\left(1 - \frac{1}{2t+1}\right) \quad (\text{any form})$	M1, A1 M1 A1 (4)
(d)	<p>(i) Substitute $t = 5$ to give V,</p> <p>then use $r = \sqrt[3]{\left(\frac{3V}{4\pi}\right)}$ to give $r, = 4.77$</p> <p>(ii) Substitutes $t = 5$ and $r =$ 'their value' into 'their' part (b)</p> $\frac{dr}{dt} = 0.0289 \quad (\approx 2.90 \times 10^{-2}) \text{ (cm/s) } * \quad \text{AG}$	M1, M1, A1 (3) M1 A1 (2) [12]

8. (a)	<p>Solves $y = 0 \Rightarrow \cos t = \frac{1}{2}$ to obtain $t = \frac{\pi}{3}$ or $\frac{5\pi}{3}$ (need both for A1)</p> <p>Or substitutes both values of t and shows that $y = 0$</p>	
(b)	$\frac{dx}{dt} = 1 - 2\cos t$ $\text{Area} = \int y dx = \int_{\pi/3}^{5\pi/3} (1 - 2\cos t)(1 - 2\cos t) dt = \int_{\pi/3}^{5\pi/3} (1 - 2\cos t)^2 dt \quad * \quad \text{AG}$	
(c)	$\begin{aligned} \text{Area} &= \int 1 - 4\cos t + 4\cos^2 t dt && 3 \text{ terms} \\ &= \int 1 - 4\cos t + 2(\cos 2t + 1) dt && (\text{use of correct double angle formula}) \\ &= \int 3 - 4\cos t + 2\cos 2t dt \\ &= [3t - 4\sin t + \sin 2t] \end{aligned}$ <p>Substitutes the two correct limits $t = \frac{5\pi}{3}$ and $\frac{\pi}{3}$ and subtracts.</p> $= 4\pi + 3\sqrt{3}$	