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Mark Scheme (Results)

June 2011

GCE Core Mathematics C4 (6666) Paper 1

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EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- The total number of marks for the paper is 75.
- The Edexcel Mathematics mark schemes use the following types of marks:
 - method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise M marks: indicated.
 - A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - B marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.

Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- _The second mark is dependent on gaining the first mark

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June 2011 Core Mathematics C4 6666 Mark Scheme

Question Number	Scheme		Marks		
1.	$9x^2 = 1$	$A(x-1)(2x+1)+B(2x+1)+C(x-1)^2$		B1	
		$9 = 3B \implies B = 3$		M1	
	$x \rightarrow -\frac{1}{2}$	$\frac{9}{4} = \left(-\frac{3}{2}\right)^2 C \implies C = 1$	Any two of A , B , C	A1	
	x^2 terms	$9 = 2A + C \implies A = 4$	All three correct	•	4)
	Alternatives f	for finding A.		[4	4]
		$0 = -A + 2B - 2C \implies A = 4$ $\text{ms} 0 = -A + B + C \implies A = 4$			

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Question Number	Scheme	Marks	
2.	$f(x) = (+)^{-\frac{1}{2}}$ $= 9^{-\frac{1}{2}} (+)^{}$ $3^{-1}, \frac{1}{3} \text{ or } \frac{1}{9^{\frac{1}{2}}}$	M1 B1	
	$(1+kx^2)^n = 1+nkx^2 + \dots$ n not a natural number, $k \ne 1$	M1	
	$(1+kx^2)^{-\frac{1}{2}} = \dots + \frac{(-\frac{1}{2})(-\frac{3}{2})}{2}(kx^2)^2$ ft their $k \neq 1$	A1 ft	
	$\left(1 + \frac{4}{9}x^2\right)^{-\frac{1}{2}} = 1 - \frac{2}{9}x^2 + \frac{2}{27}x^4$	A1	
	$f(x) = \frac{1}{3} - \frac{2}{27}x^2 + \frac{2}{81}x^4$	A1 (6)	
		[6]	

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Question Number	Scheme	Marks	
3.	(a) $\frac{dV}{dh} = \frac{1}{2}\pi h - \pi h^2$ or equivalent	M1 A1	
	At $h = 0.1$, $\frac{dV}{dh} = \frac{1}{2}\pi (0.1) - \pi (0.1)^2 = 0.04\pi$ $\frac{\pi}{25}$	M1 A1	(4)
	(b) $\frac{dh}{dt} = \frac{dV}{dt} \div \frac{dV}{dh} = \frac{\pi}{800} \times \frac{1}{\frac{1}{2}\pi h - \pi h^2} \qquad \text{or } \frac{\pi}{800} \div \text{ their (a)}$	M1	
	At $h = 0.1$, $\frac{dh}{dt} = \frac{\pi}{800} \times \frac{25}{\pi} = \frac{1}{32}$ awrt 0.031	A1 ((2)
			[6]

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Question Number	Scheme	Mark	S
4.	(a) 0.0333, 1.3596 awrt 0.0333, 1.3596	B1 B1	(2)
	(b) Area $(R) \approx \frac{1}{2} \times \frac{\sqrt{2}}{4} [\ldots]$	B1	
	$\approx \dots \left[0+2(0.0333+0.3240+1.3596)+3.9210\right]$	M1	
	≈ 1.30 Accept	A1	(3)
	(c) $u = x^2 + 2 \implies \frac{\mathrm{d}u}{\mathrm{d}x} = 2x$	B1	
	Area $(R) = \int_0^{\sqrt{2}} x^3 \ln(x^2 + 2) dx$	B1	
	$\int x^3 \ln(x^2 + 2) dx = \int x^2 \ln(x^2 + 2) x dx = \int (u - 2) (\ln u) \frac{1}{2} du$	M1	
	Hence Area $(R) = \frac{1}{2} \int_{2}^{4} (u-2) \ln u du$	A1	(4)
	(d) $\int (u-2)\ln u du = \left(\frac{u^2}{2} - 2u\right) \ln u - \int \left(\frac{u^2}{2} - 2u\right) \frac{1}{u} du$	-M1 A1	
	$= \left(\frac{u^2}{2} - 2u\right) \ln u - \int \left(\frac{u}{2} - 2\right) du$ $= \left(\frac{u^2}{2} - 2u\right) \ln u - \left(\frac{u^2}{4} - 2u\right) (+C)$	-M1 A1	
	$\operatorname{Area}(R) = \frac{1}{2} \left[\left(\frac{u^2}{2} - 2u \right) \ln u - \left(\frac{u^2}{4} - 2u \right) \right]_2^4$		
	$= \frac{1}{2} \left[(8-8) \ln 4 - 4 + 8 - ((2-4) \ln 2 - 1 + 4) \right]$	M1	
	$= \frac{1}{2} (2 \ln 2 + 1) \qquad \qquad \ln 2 + \frac{1}{2}$	A1	(6) [15]

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Question Number	Scheme	Marks
5.	$\frac{1}{y} \frac{dy}{dx} = \dots$ $\dots = 2 \ln x + 2x \left(\frac{1}{x}\right)$ At $x = 2$, $\ln y = 2(2) \ln 2$ leading to $y = 16$ Accept $y = e^{4 \ln 2}$ $\frac{1}{16} \frac{dy}{dx} = 2 \ln 2 + 2$ $\frac{dy}{dx} = 16(2 + 2 \ln 2)$	B1 - M1 A1 - M1 - A1 - M1 - A1 - (7)
	Alternative $y = e^{2x \ln x}$ $\frac{d}{dx} (2x \ln x) = 2 \ln x + 2x \left(\frac{1}{x}\right)$ $\frac{dy}{dx} = \left(2 \ln x + 2x \left(\frac{1}{x}\right)\right) e^{2x \ln x}$ At $x = 2$, $\frac{dy}{dx} = (2 \ln 2 + 2) e^{4 \ln 2}$	[7] B1 M1 A1 M1 A1
	$=16(2+2\ln 2)$	A1 (7)

Question Number	Scheme	Marks
6.	(a) i : $6-\lambda = -5+2\mu$ j : $-3+2\lambda = 15-3\mu$ Any two equations leading to $\lambda = 3$, $\mu = 4$ $\mathbf{r} = \begin{pmatrix} 6 \\ -3 \\ -2 \end{pmatrix} + 3 \begin{pmatrix} -1 \\ 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 3 \\ 3 \\ 7 \end{pmatrix} \text{ or } \mathbf{r} = \begin{pmatrix} -5 \\ 15 \\ 3 \end{pmatrix} + 4 \begin{pmatrix} 2 \\ -3 \\ 1 \end{pmatrix} = \begin{pmatrix} 3 \\ 3 \\ 7 \end{pmatrix}$ \mathbf{k} : LHS = $-2+3(3)=7$, RHS = $3+4(1)=7$ (As LHS = RHS, lines intersect)	M1 M1 A1 M1 A1 B1 (6)
	Alternatively for B1, showing that $\lambda = 3$ and $\mu = 4$ both give $\begin{bmatrix} 3 \\ 7 \end{bmatrix}$ (b) $\begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix} \begin{bmatrix} 2 \\ -3 \\ 1 \end{bmatrix} = -2 - 6 + 3 = \sqrt{14}\sqrt{14}\cos\theta (\theta \approx 110.92^\circ)$ Acute angle is 69.1° awrt 69.1	M1 A1 A1 (3)
	(c) $\mathbf{r} = \begin{pmatrix} 6 \\ -3 \\ -2 \end{pmatrix} + 1 \begin{pmatrix} -1 \\ 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 5 \\ -1 \\ 1 \end{pmatrix} (\Rightarrow B \text{ lies on } l_1)$	B1 (1)
	(d) Let d be shortest distance from B to l_2 ULUT $AB = \begin{pmatrix} 5 \\ -1 \\ 1 \end{pmatrix} - \begin{pmatrix} 3 \\ 3 \\ 7 \end{pmatrix} = \begin{pmatrix} 2 \\ -4 \\ -6 \end{pmatrix}$ $A \theta$ d l_2	M1
	$\begin{vmatrix} AB \\ AB = \sqrt{(2^2 + (-4)^2 + (-6)^2)} = \sqrt{56} $ awrt 7.5 $\frac{d}{\sqrt{56}} = \sin \theta$	A1 M1
	$d = \sqrt{56}\sin 69.1^{\circ} \approx 6.99$ awrt 6.99	A1 (4) [14]

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Question Number	Scheme		Marks	S
7.	(a) $\tan \theta = \sqrt{3} or \sin \theta = \frac{\sqrt{3}}{2}$ $\theta = \frac{\pi}{3}$	awrt 1.05	M1 A1	(2)
	(b) $\frac{dx}{d\theta} = \sec^2 \theta, \frac{dy}{d\theta} = \cos \theta$ $\frac{dy}{dx} = \frac{\cos \theta}{\sec^2 \theta} (=\cos^3 \theta)$		M1 A1	
	At P , $m = \cos^3\left(\frac{\pi}{3}\right) = \frac{1}{8}$ Using $mm' = -1$, $m' = -8$ For normal $y - \frac{1}{2}\sqrt{3} = -8(x - \sqrt{3})$	Can be implied	A1 M1 M1	
	At Q , $y = 0$ $-\frac{1}{2}\sqrt{3} = -8(x - \sqrt{3})$ leading to $x = \frac{17}{16}\sqrt{3}$ $(k = \frac{17}{16})$	1.0625	A1	(6)
	(c) $\int y^2 dx = \int y^2 \frac{dx}{d\theta} d\theta = \int \sin^2 \theta \sec^2 \theta d\theta$ $= \int \tan^2 \theta d\theta$ $= \int (\sec^2 \theta - 1) d\theta$ $= \tan \theta - \theta (+C)$ $V = \pi \int_0^{\frac{\pi}{3}} y^2 dx = \left[\tan \theta - \theta\right]_0^{\frac{\pi}{3}} = \pi \left[\left(\sqrt{3} - \frac{\pi}{3}\right) - \left(0 - 0\right)\right]$ $= \sqrt{3}\pi - \frac{1}{3}\pi^2 \qquad \left(p = 1, q = -\frac{1}{3}\right)$		M1 A1 A1 M1 A1 M1 A1	(7) [15]

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Question Number	Scheme	Marks
8.	(a) $ \int (4y+3)^{-\frac{1}{2}} dx = \frac{(4y+3)^{\frac{1}{2}}}{(4)(\frac{1}{2})} + C $ $ \left(= \frac{1}{2}(4y+3)^{\frac{1}{2}} + C \right) $	M1 A1 (2)
	(b) $\int \frac{1}{\sqrt{(4y+3)}} dy = \int \frac{1}{x^2} dx$ $\int (4y+3)^{-\frac{1}{2}} dy = \int x^{-2} dx$	B1
	$\frac{1}{2}(4y+3)^{\frac{1}{2}} = -\frac{1}{x} (+C)$	M1
	Using $(-2, 1.5)$ $\frac{1}{2}(4 \times 1.5 + 3)^{\frac{1}{2}} = -\frac{1}{-2} + C$	M1
	leading to $C = 1$ $\frac{1}{2}(4y+3)^{\frac{1}{2}} = -\frac{1}{x}+1$ $(4y+3)^{\frac{1}{2}} = 2 - \frac{2}{x}$	A1
	$(4y+3)^{\frac{1}{2}} = 2 - \frac{2}{x}$	M1
	$y = \frac{1}{4} \left(2 - \frac{2}{x} \right)^2 - \frac{3}{4}$ or equivalent	A1 (6)
		[8]

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