

Mark Scheme (Results)

Summer 2014

Pearson Edexcel GCE in Core Mathematics 2 (6664\_01)

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Summer 2014
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### **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### PEARSON EDEXCEL GCE MATHEMATICS

# **General Instructions for Marking**

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

#### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- · awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

# **General Principles for Core Mathematics Marking**

(But note that specific mark schemes may sometimes override these general principles).

# Method mark for solving 3 term quadratic:

### 1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q)$$
, where  $|pq| = |c|$ , leading to  $x = ...$ 

$$(ax^2 + bx + c) = (mx + p)(nx + q)$$
, where  $|pq| = |c|$  and  $|mn| = |a|$ , leading to  $x = ...$ 

### 2. Formula

Attempt to use the correct formula (with values for a, b and c).

# 3. Completing the square

Solving 
$$x^2 + bx + c = 0$$
:  $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c = 0$ ,  $q \neq 0$ , leading to  $x = \dots$ 

# Method marks for differentiation and integration:

# 1. Differentiation

Power of at least one term decreased by 1.  $(x^n \rightarrow x^{n-1})$ 

# 2. Integration

Power of at least one term increased by 1.  $(x^n \rightarrow x^{n+1})$ 

# Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

#### **Exact answers**

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Question Number	Scheme				Marks	
	<u>x</u> 1	1.25	1.5	1.75	2	
	y 1.414	1.601	1.803	2.016	2.236	
1.(a)	$\{\text{At } x = 1.25,\}\ y = 1.60$	l (only)			the table and can of their working in	B1 cao
	1					[1]
	$\frac{1}{2}$ × 0.25;× $\left\{1\right\}$	414 + 2.236 + 2	2(their 1.60			B1; M1 A1ft
	B1; for using $\frac{1}{2} \times 0.25$ or $\frac{1}{8}$ or equivalent.	<u>M1: Str</u>	<u>ucture of</u> }	as show	or the correct expression on following through the sy value found in	
	M1 requires the correct structure for the y values. It needs to contain first y value <b>plus</b> last y value and the second bracket to be multiplied by 2 and to be the summation of the remaining y values in the table with no additional values. If the only mistake is a copying error or is to omit one value from 2() bracket this may be regarded as a slip and the M mark can be allowed (nb: an extra repeated term, however, forfeits the M mark). M0 if any values used are x values instead of y values.  A1ft: for the correct underlined expression as shown following through candidate's y value found in part (a).  Bracketing mistakes: e.g.					
	$\left(\frac{1}{2} \times \frac{1}{4}\right) (1.414 + 2.236) + 2 \left(\text{their } 1.601 + 1.803 + 2.016\right) (=11.29625)$ $\left(\frac{1}{2} \times \frac{1}{4}\right) 1.414 + 2.236 + 2 \left(\text{their } 1.601 + 1.803 + 2.016\right) (=13.25275)$ Both score B1 M1 A0 unless the final answer implies that the calculation has been done correctly (then full marks could be given).					
	Alternative: Separate trapezia may be used, and this can be marked equivalently.					
	$\left[ \frac{1}{8} (1.414 + 1.601) + \frac{1}{8} (1.601 + 1.803) + \frac{1}{8} (1.803 + 2.016) + \frac{1}{8} (2.016 + 2.236) \right]$ B1 for $\frac{1}{8}$ (aef), M1 for correct structure, 1st A1ft for correct expression, ft their 1.601					
	$\left\{ = \frac{1}{8}(14.49) \right\} = 1.81125$		1.81 or a	wrt 1.81		A1
		et answer <u>only</u>				
	If required accuracy is not so	een in (a), full	marks can	still be score	ed in (b) (e.g. uses 1.6)	f A1
						[4] Total 5

Question Number	Scheme			
	If there is no labelling, mark (a) and (b) in that order			
	$f(x) = 2x^3 - 7x^2 + 4x + 4$			
	$f(2) = 2(2)^3 - 7(2)^2 + 4(2) + 4$	Attempts f(2) or f(-2)	M1	
<b>2.</b> (a)	f(2) = 0 with no sign or substitution errors $(2(2)^3 - 7(2)^2 + 4(2) + 4 = 0 \text{ is sufficient})$ and for conclusion. Stating "hence factor" or "it is a factor" or a "tick" or "QED" or "no remainder" or "as required" are fine for the conclusion but not = 0 just underlined and not hence (2 or f(2)) is a factor. Note also that a conclusion can be implied from a preamble, eg: "If $f(2) = 0$ , $(x - 2)$ is a factor"		A1	
	Note: Long division scores no marks in part (a). The <u>factor theorem</u> is required.			
(b)	$f(x) = \{(x-2)\}(2x^2 - 3x - 2)$	M1: Attempts long division by $(x-2)$ or other method using $(x-2)$ , to obtain $(2x^2 \pm ax \pm b)$ , $a \ne 0$ , even with a remainder. Working need not be seen as this could be done "by inspection."  A1: $(2x^2 - 3x - 2)$	[2] M1 A1	
	$= (x-2)(x-2)(2x+1)\operatorname{or}(x-2)^{2}(2x+1)$ or equivalent e.g. $= 2(x-2)(x-2)(x+\frac{1}{2})\operatorname{or}2(x-2)^{2}(x+\frac{1}{2})$	dM1: Factorises a 3 term quadratic. (see rule for factorising a quadratic in the General Principles for Core Maths Marking). This is dependent on the previous method mark being awarded but there must have been no remainder. Allow an attempt to solve the quadratic to determine the factors.  A1: cao – needs all three factors on one line. Ignore following work (such as a solution to a quadratic equation.)	<b>d</b> M1 A1	
	Note = $(x-2)(\frac{1}{2}x-1)(4x+2)$ would lose the last mark as it is not <b>fully</b> factorised			
	For correct answers only award full marks in (b)			
			[4]	
			Total 6	

Question Number	Scheme			
<b>3.</b> (a)	$(2-3x)^6 = 64 + \dots$	64 seen as the only constant term in their expansion.	B1	
	$\left\{ (2-3x)^6 \right\} = (2)^6 + \frac{{}^6C_1}{}(2)^5(-3\underline{x}) + \frac{{}^6C_2}{}(2)^4(-3\underline{x})^2 + \dots$			
	M1: $({}^{6}C_{1} \times \times x)$ or $({}^{6}C_{2} \times \times x^{2})$ . For <u>either</u>	the x term $\underline{\text{or}}$ the $x^2$ term. Requires $\underline{\text{correct}}$		
	binomial coefficient in any form with the corcoefficient (perhaps including powers of 2 and/o	or $-3$ ) may be wrong or missing. The terms		
	can be "listed" rather than adde	<u> </u>		
	${}^{6}C_{1}2^{5} - 3x + {}^{6}C_{2}2^{4} - 3x^{2} + \dots$ Scores M0 u			
		A1: Either $-576x$ or $2160x^2$		
	$= 64 - 576x + 2160x^2 + \dots$	(Allow + $-576x$ here) A1: Both $-576x$ and $2160x^2$	A1A1	
		(Do not allow $+ - 576x$ here)		
		(Do not anow + - 370x here)	[4]	
(a) Way 2	$(2-3x)^6 = 64 + \dots$	64 seen as the only constant term in their		
	(2-3x) = 64+	expansion.	B1	
		M1: $({}^{6}C_{1} \times \times x) \operatorname{or} ({}^{6}C_{2} \times \times x^{2})$ . For		
	$\left(1 - \frac{3}{2}x\right)^6 = 1 + \frac{{}^6C_1}{2}\left(\frac{-3}{2}x\right) + \frac{{}^6C_2}{2}\left(\frac{-3}{2}x\right)^2 + \dots$	part of the coefficient (perhaps including powers of 2 and/or $-3$ ) may be wrong or	<u>M1</u>	
		missing. The terms can be "listed" rather than added. Ignore any extra terms.		
		A1: Either $-576x$ or $2160x^2$		
	$= 64 - 576x + 2160x^2 + \dots$	(Allow + -576x here)	A 1 A 1	
		A1: Both $-576x$ and $2160x^2$	A1A1	
		(Do not allow $+ -576x$ here)		
(b)	Candidate writes down $\left(1+\frac{x}{2}\right)\times\left(\text{their part}\right)$	(a) answer, at least up to the term in $x$ ).		
	(Condone missing brackets)			
	$\left(1+\frac{x}{2}\right)\left(64-576x+\right) \text{ or } \left(1+\frac{x}{2}\right)\left(64-576x+2160x^2+\right) \text{ or }$			
	$\left(1+\frac{x}{2}\right)64-\left(1+\frac{x}{2}\right)576x \text{ or } \left(1+\frac{x}{2}\right)64-\left(1+\frac{x}{2}\right)576x+\left(1+\frac{x}{2}\right)2160x^2$			
	or $64+32x,-576x-288x^2$ , $2160x^2+1080x^3$ are fine.			
		A1: At least 2 terms correct as shown. (Allow $+ -544x$ here)		
	$= 64 - 544x + 1872x^2 + \dots$	A1: $64 - 544x + 1872x^2$	A1A1	
		The terms can be "listed" rather than		
		added. Ignore any extra terms.	[3]	
			Total 7	
	SC: If a candidate expands in descending powers of x, only the M marks are available			
	<b>e.g.</b> $\{(2-3x)^6\} = (-3x)^6 + \frac{{}^6C_1}{2}(2x)^6 + \frac{{}^6C_1}{2$	$(-3x)^5 + \frac{^6C_2}{(2)^2(-3x)^4} + \dots$		

Question Number	Scheme		
4.	$\left\{ \int \left( \frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \frac{x^4}{6(4)} + \frac{x^{-1}}{(3)(-1)}$	M1: $x^n \to x^{n+1}$ A1: At least one of either $\frac{x^4}{6(4)}$ or $\frac{x^{-1}}{(3)(-1)}$ .  A1: $\frac{x^4}{6(4)} + \frac{x^{-1}}{(3)(-1)}$ or equivalent.  e.g. $\frac{x^4}{6} + \frac{x^{-1}}{3}$ (they will lose the final mark	M1A1A1
		if they cannot deal with this correctly)	
	Note that some candidates may change $\int \frac{x^3}{6} + \frac{1}{3x^2} dx = \int 3x^5 + 6dx$ in which case all function and allow the	llow the M1 if $x^n \to x^{n+1}$ for their changed	
	$\left\{ \int_{1}^{\sqrt{3}} \left( \frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \left( \frac{\left(\sqrt{3}\right)}{24} \right)$	4 1)	dM1
	$2^{nd}$ dM1: For using limits of $\sqrt{3}$ and 1 on an integrated expression and subtracting the correct way round. The $2^{nd}$ M1 is dependent on the $1^{st}$ M1 being awarded.		
		$\frac{2}{3} - \frac{1}{9}\sqrt{3}$ or $a = \frac{2}{3}$ and $b = -\frac{1}{9}$ . Allow equivalent fractions for $a$ and/or $b$ and 0.6 recurring and/or 0.1 recurring but do <b>not</b> allow $\frac{6-\sqrt{3}}{9}$	Alcso
	This final mark is cao and cso – there	e must have been no previous errors	T . 1.
	Common Errors (U	Usually 3 out of 5)	Total 5
	$\left\{ \int \left( \frac{x^3}{6} + \frac{1}{3x^2} \right) \mathrm{d}x \right\} = \int \left( \frac{x^3}{6} + 3x^2 \right) \mathrm{d}x$	$(x^{-2})dx = \frac{x^4}{6(4)} + \frac{3x^{-1}}{(-1)} M1A1A0$	
	$\left\{ \int_{1}^{\sqrt{3}} \left( \frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \left( \frac{\left(\sqrt{3}\right)^4}{24} + \frac{1}{3x^2} \right) dx = \left( \frac{1}{3} + \frac{1}{3$	$\left(\frac{(1)}{-1}\right) - \left(\frac{(1)}{24} + \frac{3(1)}{-1}\right) dM1$	
	$= \left(\frac{9}{24} - \frac{3}{\sqrt{3}}\right) - \left(\frac{1}{24} + \frac{3}{-1}\right) = \frac{10}{3} - \sqrt{3} \text{A0}$		
	$\left\{ \int \left(\frac{x^3}{6} + \frac{1}{3x^2}\right) dx \right\} = \int \left(\frac{x^3}{6} + \left(3x\right)^2\right) dx$		
	$\left\{ \int_{1}^{\sqrt{3}} \left( \frac{x^{3}}{6} + \frac{1}{3x^{2}} \right) dx \right\} = \left( \frac{\left(\sqrt{3}\right)^{4}}{24} + \frac{\left(3\sqrt{3}\right)^{-1}}{-1} \right) - \left( \frac{\left(1\right)^{4}}{24} + \frac{\left(3\times1\right)^{-1}}{-1} \right) dM1$		
	$=\left(\frac{9}{24}-\frac{1}{3\sqrt{3}}\right)-\left(\frac{1}{24}\right)$		
	Note this is the correct answer	r but follows incorrect work.	

Question Number		Scheme	Mark
5.(a)	Area $BDE = \frac{1}{2}(5)^2(1.4)$	M1: Use of the correct formula or method for the area of the sector	M1A
	$=17.5 \text{ (cm}^2)$	A1: 17.5 oe	
<i>a</i> .	P ( (1) 1(		[2
<b>(b)</b>	Parts (b) and (c) can be marked together		
	$6.1^2 = 5^2 + 7.5^2 - (2 \times 5 \times 7.5 \cos DBC)  \text{or}  \cos DBC = \frac{5^2 + 7.5^2 - 6.1^2}{2 \times 5 \times 7.5} \text{ (or equivalent)}$		
		ment involving the angle DBC	
	Angle $DBC = 0.943201$	awrt 0.943	A1
	Note that work for (b) may	be seen on the diagram or in part (c)	[2
(c)	Note that candidates may work in c	<b>legrees in (c)</b> (Angle $DBC = 54.04$ deg rees )	ľ
	Area CBD	$=\frac{1}{2}5(7.5)\sin(0.943)$	
		Area $CBD = \frac{1}{2}5(7.5)\sin(\text{their } 0.943)$ or awrt	
	Angle $EBA = \pi - 1.4 - 0.943$	15.2. (Note area of <i>CBD</i> = 15.177)	M1
	(Maybe seen on the diagram)	A correct method for the area of triangle <i>CBD</i> which can be implied by awrt 15.2	
	$\pi$ – 1.4 – "their 0.943"		
	A value for angle <i>EBA</i> of awrt 0.8 (from 0.7985926536 or 0.7983916536) or value for angle		
	EBA of $(1.74159 \text{their angle } DBC)$ would imply this mark.		
	$AB = 5\cos(\pi - 1.4 - 0.943)$		
	or $AE = 5\sin(\pi - 1.4 - 0.943)$		
		$AB = 5\cos(\pi - 1.4 - \text{their } 0.943)$	
		$AB = 5\cos(0.79859) = 3.488577938$	
		Allow M1 for $AB = \text{awrt } 3.49$	
		Or	
		$AE = 5\sin(\pi - 1.4 - \text{their } 0.943)$	
		$AE = 5\sin(0.79859) = 3.581874365688$	M1
		Allow M1 for $AE = \text{awrt } 3.58$	1411
		It must be clear that $\pi - 1.4 - 0.943$ is	
		being used for angle EBA.  Note that some candidates use the sin	
		rule here but it must be used correctly –	
		do not allow mixing of degrees and	
		radians.	
	2	$-$ "0.943") × $5\sin(\pi - 1.4 -$ "0.943")	
		lent on the previous M1	dM1
		rors in finding the area of triangle EAB or area EAB = awrt 6.2	
		17+ 17.5 + 6.24 = 38.92	
		awrt 38.9	Alcs
			[:
	Note that a sign error in (b) can give the obtuse angle (2.198) and could lead to the correct		Tot
	answer in (c) – this would lose the final m	ark in (c)	

Question Number	Sc	heme	Marks	
6(a)	s _ 20160	M1: Use of a correct $S_{\infty}$ formula	3.51.1.1	
	$S_{\infty} = \frac{20}{1 - \frac{7}{8}} \; ; = 160$	A1: 160	M1A1	
	Accept correct	answer only (160)		
			[2]	
<b>(b)</b>	$20(1-(7)^{12})$	M1: Use of a correct $S_n$ formula with $n = 12$		
	$S_{12} = \frac{20(1-(\frac{7}{8})^{12})}{1-\frac{7}{2}}$ ; = 127.77324	(condone missing brackets around 7/8)	M1A1	
	$1-\frac{\cdot}{8}$	A1: awrt 127.8		
	T & I in (b) requires all 12 terms to be calc	ulated correctly for M1 and A1 for awrt 127.8		
(c)	20/1 (7) N	Applies $S_N$ ( <b>GP only</b> ) with $a = 20$ , $r = \frac{7}{8}$ and		
	$160 - \frac{20(1 - (\frac{7}{8})^N)}{1 - \frac{7}{2}} < 0.5$	"uses" 0.5 and their $S_{\infty}$ at any point in their	M1	
	$1-\frac{\cdot}{8}$	working. (condone missing brackets around $7/8$ )(Allow =, <, >, $\geq$ , $\leq$ ) but see note below.		
	$(7)^N$ $(7)^N$ $(0.5)$	Attempt to isolate $+160\left(\frac{7}{8}\right)^N$ or $+\left(\frac{7}{8}\right)^N$ oe		
	$160\left(\frac{7}{8}\right)^{N} < (0.5) \text{ or } \left(\frac{7}{8}\right)^{N} < \left(\frac{0.5}{160}\right)$	(Allow $=$ , $<$ , $>$ , $\ge$ , $\le$ ) but see note below.	dM1	
	(0) (100)	Dependent on the previous M1		
		Uses the power law of logarithms or takes logs base 0.875 correctly to obtain an equation or an inequality of the form		
	$N\log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{160}\right)$	$N\log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{\text{their }\mathbf{S}_{\infty}}\right)$ or	M1	
		$N > \log_{0.875} \left( \frac{0.5}{\text{their S}_{\infty}} \right)$		
		(Allow =, $<$ , $>$ , $\ge$ , $\le$ ) but see note below.		
	$N > \frac{\log(\frac{0.5}{160})}{\log(\frac{7}{8})} = 43.19823 \Rightarrow N = 44$	$N = 44$ (Allow $N \ge 44$ but not $N > 44$	A1 cso	
	Some candidates do not realise that the direct	e in a candidate's working loses the final mark. tion of the inequality is reversed in the final line full marks for using =, as long as no incorrect		
			[4]	
	70 * 3.0.7	(M. 1. 1. ( )	Total 8	
		provement Method in (c):		
		or $S_N$ with at least one value for $N > 40$		
		$0 - S_N$ or $S_N$ with $N = 43$ or $N = 44$		
	$3^{\text{rd}}$ M1: For evidence of examining $160 - S_N$ or $S_N$ for <b>both</b> $N = 43$ <b>and</b> $N = 44$ with <b>both</b> correct to 2 DP			
	Eg: $160 - S_{43} = \text{awrt } 0.51 \text{ and } 160 - S_{44} = \text{awrt } 0.45$			
	or $S_{43} = \text{awrt} 159.49 \text{ and } S_{44} = \text{awrt} 159.55$			
	A1: $N = 44 \operatorname{cso}$			
	Answer of $N = 44$ only with no working scores no marks			

Question Number	Sch	neme	Marks
7	(i) $9\sin(\theta + 60^{\circ})$	$=4; 0 \le \theta < 360^{\circ}$	
7.	(ii) $2\tan x - 3\sin$	$x = 0; -\pi \le x < \pi$	
(i)	$\sin(\theta + 60^{\circ}) = \frac{4}{9}$ , so $(\theta + 60^{\circ}) = 26.3877$	Sight of $\sin^{-1}\left(\frac{4}{9}\right)$ or awrt $26.4^{\circ}$ or $0.461^{\circ}$	M1
	$(\alpha = 26.3877)$	Can also be implied for $\theta = \text{awrt} - 33.6$ (i.e. $26.4 - 60$ )	
		$\theta + 60^{\circ}$ = either "180 – their $\alpha$ " or	
		" $360^{\circ}$ + their $\alpha$ " and not for $\theta$ = either	
	So, $\theta + 60^{\circ} = \{153.6122, 386.3877\}$	" $180$ – their $\alpha$ " or " $360^{\circ}$ + their $\alpha$ ". This	M1
	50, 0 1 00 (15510122, 50015077)	can be implied by later working. The candidate's $\alpha$ could also be in radians but do not allow mixing of degrees and radians.	WII
		A1: At least one of	
	and $\theta = \{93.6122, 326.3877\}$	awrt 93.6° or awrt 326.4°	A1 A1
		A1: Both awrt 93.6° and awrt 326.4°	
		nust come from correct work	
	Ignore extra solutions outside the range.		
	In an otherwise fully correct solution deduct the final A1for any extra solutions in range		
(ii)	$2\left(\frac{\sin x}{\cos x}\right) - 3\sin x = 0$	Applies $\tan x = \frac{\sin x}{\cos x}$	M1
	Note: Applies $\tan x = \frac{\sin x}{\cos x}$ can be implied by $2\tan x - 3\sin x = 0 \Rightarrow \tan x (2 - 3\cos x)$		
	$2\sin x - 3\sin x \cos x = 0$		
	$\sin x(2-3\cos x)=0$		
	$\cos x = \frac{2}{3}$	$\cos x = \frac{2}{3}$	A1
		A1: One of either awrt 0.84 or awrt -0.84	
	$x = \operatorname{awrt}\{0.84, -0.84\}$	A1ft: You can apply ft for $x = \pm \alpha$ , where	A1A1ft
		$\alpha = \cos^{-1} k$ and $-1 \le k \le 1$	
	In this part of the solution, if there are any extra answers in range in an otherwise		
	correct solution	withhold the A1ft.	
	$\{\sin x = 0 \implies\} x = 0 \text{ and } -\pi$	<b>Both</b> $x = 0$ <b>and</b> $-\pi$ or awrt $-3.14$ from $\sin x = 0$	B1
	, , , , , , , , , , , , , , , , , , ,	In this part of the solution, ignore extra solutions in range.	
	Note solutions are: $x = \{-3.14\}$		
	`	,	
	Ignore extra solutions outside the range For <b>all</b> answers in degrees in (ii) M1A1A0A1ftB0 is possible		
	Allow the use of $\theta$ in place of $x$ in (ii)		
			[5]
			Total 9

Question Number	Scheme			Marks
8.	Graph of $y = 3^x$ and solving	$3^{2x} - 9(3^x) + 18$	=0	
(a)			the three criteria correct. notes below.)	B1
			e criteria correct. notes below.)	B1
	v <b>▲</b> /		er 1: Correct shape of and at least touches the	
			er 2: Correct shape of . Must not touch the x-	
	(0.1)	axis or have any Criteria numb	y turning points. er 3: (0, 1) stated or in	
	O $x$	a table or 1 marked on the <i>y</i> -axis. Allow (1, 0) rather than (0, 1) if		
		marked in the "correct" place on the y-axis.		
				[2]
(b)	$(3^x)^2 - 9(3^x) + 18 = 0$	_	tic of the correct form in	
	or	-	ere " $y$ " = $3^x$ or even in $x$	M1
	$y = 3^x \implies y^2 - 9y + 18 = 0$	where " $x$ " = $3^x$		
	$\{(y-6)(y-3) = 0 \text{ or } (3^x-6)(3^x-3) = 0 \}$			
	$y = 6$ , $y = 3$ or $3^x = 6$ , $3^x = 3$	<b>Both</b> $y = 6$ and $y = 3$ .		A1
		A valid method	for solving $3^x = k$	
	$\left\{3^x = 6 \Rightarrow\right\} x \log 3 = \log 6$	where $k > 0$ , $k \neq 1$ , $k \neq 3$		
	or $x = \frac{\log 6}{\log 3}$ or $x = \log_3 6$		$x \log 3 = \log k$ or	dM1
	$\log 3 = \log_3 0$	to give either	$x = \frac{\log k}{\log 3} \text{ or } x = \log_3 k$	
	x = 1.63092	awrt 1.63		A1cso
	Provided the first M1A1 is scored, the second	d M1A1 can be implied by awrt 1.63		
	<i>x</i> = 1	x = 1 stated as a solution from <i>any</i> working.		B1
				[5]
				Total 7

Question Number	Scheme					
Ivuilioci	Mark (a) and (b) to	gether				
9. (a)	$OQ^2 = (6\sqrt{5})^2 + 4^2 \text{ or } OQ = \sqrt{(6\sqrt{5})^2 + 4^2}  \{=14\}$	Uses the addition form of Pythagoras on $6\sqrt{5}$ and 4. Condone missing brackets on $\left(6\sqrt{5}\right)^2$ (Working or 14 may be seen on the diagram)	M1			
	$y_Q = \sqrt{14^2 - 11^2}$	$y_Q = \sqrt{(\text{their } OQ)^2 - 11^2}$ Must include $$ and is dependent on the first M1 and requires OQ > 11	dM1			
	$=\sqrt{75} \text{ or } 5\sqrt{3}$	$\sqrt{75}$ or $5\sqrt{3}$	A1cso			
			[3]			
(b)	$(x-11)^2 + (y-5\sqrt{3})^2 = 16$	M1: $(x \pm 11)^2 + (y \pm \text{their } k)^2 = 4^2$ Equation must be of this form and must use $x$ and $y$ not other letters. $k$ could be their last answer to part (a). Allow their $k \neq 0$ or just the letter $k$ .  A1: $(x-11)^2 + (y-5\sqrt{3})^2 = 16$ or $(x-11)^2 + (y-5\sqrt{3})^2 = 4^2$ NB $5\sqrt{3}$ must come from correct work in (a) and allow awrt 8.66	- M1A1			
	Allow in expanded form for					
	e.g. $x^2 - 22x + 121 + y^2 - 10$	$\sqrt{3}y + 75 = 16$				
			[2]			
			Total 5			
	Watch out for:					
	(a) $OQ = \sqrt{(6\sqrt{5})^2}$ $y_Q = \sqrt{46 - 11^2} \text{ N}$ $y_Q = \sqrt{7}$ (b) $(x - 11)^2 + (y - 5)^2$	$\frac{M0 \text{ (OQ} < 11)}{5 \text{ A0}}$				

Question Number	Scheme		Marks		
10. (a)	or $2x \times 15x$ or $\left(\frac{1}{2}4x \times (9x-6x)+6x \times 4x\right)$ or $6x^2+24x^2$ or $\left(9x \times 4x-\frac{1}{2}4x \times (9x-6x)\right)$ or $36x^2-6x^2$ M1: Correct attempt at the area of a trapezium.  Note that $30x^2$ on its own or $30x^2$ from incorrect work e.g. $5x \times 6x$ is M0.  If there is a clear intention to find the area of the trapezium correctly allow the M1 but the A1 can be withheld if there are any slips.  A1: Correct proof with at least one		M1A1cso		
	$\Rightarrow 30x^2y = 9600 \Rightarrow y = \frac{9600}{30x^2} \Rightarrow y = \frac{320}{x^2} *$	A1: Correct proof with at least one intermediate step and no errors seen.  "y =" is required.			
			[2]		
(b)	$(S =) \frac{1}{2} (9x + 6x) 4x + \frac{1}{2} (9x + 6x) 4x + 6xy + 9xy + 5xy + 4xy$				
	M1: An attempt to find the area of six faces of the	prism. The 2 trapezia may be combined as			
	$(9x + 6x)4x$ or $60x^2$ and the 4 other faces may be combined as $24xy$ but all six faces must be				
	included. There must be attempt at the areas of two trapezia that are dimensionally correct.  A1: Correct expression in any form.  Allow just $(S =) 60x^2 + 24xy$ for M1A1				
	$y = \frac{320}{x^2} \Rightarrow (S =) 30x^2 + 30x^2 + 24x \left(\frac{320}{x^2}\right)$				
	Substitutes $y = \frac{320}{x^2}$ into their expression for <i>S</i> (may be done earlier). <i>S</i> should have at least				
	one $x^2$ term and one $xy$ term but there may be other terms which may be dimensionally incorrect.				
	So, $(S =) 60x^2 + \frac{7680}{x}$ * Correct solution only. "S = " is <b>not</b> required here.				
			[4]		

10(c)	$\frac{dS}{dx} = 120x - 7680x^{-2} \left\{ = 120x - \frac{7680}{x^2} \right\}$	M1: Either $60x^2 \rightarrow 120x$ or $\frac{7680}{x} \rightarrow \frac{\pm \lambda}{x^2}$ A1: Correct differentiation (need not be	M1
		A1: Correct differentiation (need not be simplified).	A1 aef
	$120x - \frac{7680}{x^2} = 0$ $\Rightarrow x^3 = \frac{7680}{120}; = 64 \Rightarrow x = 4$	M1: $S' = 0$ and "their $x^3 = \pm$ value" or "their $x^{-3} = \pm$ value" Setting their $\frac{dS}{dx} = 0$ and "candidate's ft <u>correct</u> power of $x = a$ value". The power of $x$ must be consistent with their differentiation. If inequalities are used this mark cannot be gained until candidate states value of $x$ or $S$ from their $x$ without inequalities. $S' = 0$ can be implied by $120x = \frac{7680}{x^2}$ . Some may spot that $x = 4$ gives $S' = 0$ and provided they clearly show $S'(4) = 0$ allow this mark as long as $S'$ is correct. (If $S'$ is incorrect this method is allowed if their derivative is clearly zero for their value of $x$ ) Note that the value of $x$ is not explicitly required so the use of $x = \sqrt[3]{64}$ to give $S = 2880$ would imply this mark.	M1A1cso
	Note some candidates stop here and do	o not go on to find S – maximum mark is 4/6	
	$\{x = 4,\}$	Substitute candidate's value of $x \neq 0$ into a formula for S. <b>Dependent on both previous M</b> marks.	ddM1
	$S = 60(4)^2 + \frac{7680}{4} = 2880 \text{ (cm}^2\text{)}$	2880 cso (Must come from correct work)	A1 cao and cso
			[6]

10(d)	M1: Attempt $S''(x^n \to x^{n-1})$ and considers sign.  This mark requires an attempt at the second derivative and some consideration of its sign.  There does not necessarily need to be any substitution. An attempt to solve $S'' = 0$ is M0  A1: $120 + \frac{15360}{x^3}$ and $> 0$ and conclusion.  Requires a correct second derivative of $120 + \frac{15360}{x^3}$ (need not be simplified) and a valid reason (e.g. $> 0$ ), and conclusion.  Only follow through a correct second derivative	M1A1ft
	i.e. x may be incorrect <b>but must be positive</b> and/or S' may have been evaluated incorrectly.	
	A correct S'' followed by S''("4") = "360" therefore minimum would score no marks in (d)	
	A correct $S''$ followed by $S''("4") = "360"$ which is positive therefore minimum would score	
	both marks	
		[2]
	Note parts (c) and (d) can be marked together.	
		Total 14