Past Paper (Mark Scheme)

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Mark Scheme (Results) January 2009

GCE

GCE Mathematics (6667/01)



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January 2009 6667 Further Pure Mathematics FP1 (new) Mark Scheme

Question Number	Scheme	Marks
1		
	x-3 is a factor	B1
	$f(x) = (x-3)(2x^2 - 2x + 1)$	M1 A1
	Attempt to solve quadratic i.e. $x = \frac{2 \pm \sqrt{4 - 8}}{4}$	M1
	$x = \frac{1 \pm i}{2}$	A1 [5]

Notes:

First and last terms in second bracket required for first M1 Use of correct quadratic formula for their equation for second M1

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Que: Num	stion iber	Scheme	Marks	5
2	(a)	$6\sum_{n} r^{2} + 4\sum_{n} r - \sum_{n} 1 = 6\frac{n}{6}(n+1)(2n+1) + 4\frac{n}{2}(n+1), -n$	M1 A1, B	31
		$= \frac{n}{6}(12n^2 + 18n + 6 + 12n + 12 - 6) \text{ or } n(n+1)(2n+1) + (2n+1)n$	M1	
		$= \frac{n}{6}(12n^2 + 30n + 12) = n(2n^2 + 5n + 2) = n(n+2)(2n+1) *$	A1	(5)
	(b)	$\sum_{r=1}^{20} (6r^2 + 4r - 1) - \sum_{r=1}^{10} (6r^2 + 4r - 1) = 20 \times 22 \times 41 - 10 \times 12 \times 21$	M1	
		= 15520	A1	(2) [7]

Notes:

- (a) First M1 for first 2 terms, B1 for -n Second M1 for attempt to expand and gather terms. Final A1 for correct solution only
- (b) Require (r from 1 to 20) subtract (r from 1 to 10) and attempt to substitute for M1

Mathematics FP1

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Ques	stion ber	Scheme	Marks	
3	(a)	$xy = 25 = 5^2$ or $c = \pm 5$	B1	(1)
	(b)	A has co-ords $(5, 5)$ and B has co-ords $(25, 1)$	B1	
		Mid point is at (15, 3)	M1A1	(3) [4]

4

Notes:

(a)
$$xy = 25$$
 only B1, $c^2 = 25$ only B1, $c = 5$ only B1

(b) Both coordinates required for B1 Add theirs and divide by 2 on both for M1

Past Paper (Mark Scheme)

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6	6	6	7

Question Number	Scheme	Marks
4	When $n = 1$, LHS = $\frac{1}{1 \times 2} = \frac{1}{2}$, RHS = $\frac{1}{1+1} = \frac{1}{2}$. So LHS = RHS and result true for $n = 1$	B1
	Assume true for $n = k$; $\sum_{r=1}^{k} \frac{1}{r(r+1)} = \frac{k}{k+1}$ and so $\sum_{r=1}^{k+1} \frac{1}{r(r+1)} = \frac{k}{k+1} + \frac{1}{(k+1)(k+2)}$	M1
	$\sum_{r=1}^{k+1} \frac{1}{r(r+1)} = \frac{k(k+2)+1}{(k+1)(k+2)} = \frac{k^2+2k+1}{(k+1)(k+2)} = \frac{(k+1)^2}{(k+1)(k+2)} = \frac{k+1}{k+2}$	M1 A1
	and so result is true for $n = k + 1$ (and by induction true for $n \in \mathbb{Z}^+$)	B1 [5]

Notes:

Evaluate both sides for first B1

Final two terms on second line for first M1

Attempt to find common denominator for second M1.

Second M1 dependent upon first.

$$\frac{k+1}{k+2} \text{ for A1}$$

'Assume true for n = k 'and 'so result true for n = k + 1' and correct solution for final B1

6667

Que:	stion ber	Scheme	Marks	
5	(a)	attempt evaluation of $f(1.1)$ and $f(1.2)$ (– looking for sign change)	M1	
		$f(1.1) = 0.30875$, $f(1.2) = -0.28199$ Change of sign in $f(x) \Rightarrow$ root in the interval	A1 (2	(2)
	(b)	$f'(x) = \frac{3}{2}x^{-\frac{1}{2}} - 9x^{-\frac{1}{2}}$	M1 A1 A1	(3)
	(c)	f(1.1) = 0.30875 $f'(1.1) = -6.37086$	B1 B1	
		$x_1 = 1.1 - \frac{0.30875}{-6.37086}$ = 1.15(to 3 sig.figs.)		(4) 91

Notes:

- (a) awrt 0.3 and -0.3 and indication of sign change for first A1
- (b) Multiply by power and subtract 1 from power for evidence of differentiation and award of first M1
- (c) awrt 0.309 B1and awrt -6.37 B1 if answer incorrect

Evidence of Newton-Raphson for M1

Evidence of Newton-Raphson and awrt 1.15 award 4/4

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Question Number	Scheme	Marks
6	At $n = 1$, $u_n = 5 \times 6^0 + 1 = 6$ and so result true for $n = 1$	B1
	Assume true for $n = k$; $u_k = 5 \times 6^{k-1} + 1$, and so $u_{k+1} = 6(5 \times 6^{k-1} + 1) - 5$	M1, A1
	$\therefore u_{k+1} = 5 \times 6^k + 6 - 5 \therefore u_{k+1} = 5 \times 6^k + 1$	A1
	and so result is true for $n = k + 1$ and by induction true for $n \ge 1$	B1 [5]

Notes:

6 and so result true for n = 1 award B1

Sub u_k into u_{k+1} or M1 and A1 for correct expression on right hand of line 2

Second A1 for $\therefore u_{k+1} = 5 \times 6^k + 1$

'Assume true for n = k' and 'so result is true for n = k + 1' and correct solution for final B1

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	estion nber	Scheme	Marks
7	(a)	The determinant is $a - 2$	M1
		$\mathbf{X}^{-1} = \frac{1}{a-2} \begin{pmatrix} -1 & -a \\ 1 & 2 \end{pmatrix}$	M1 A1 (3)
	(b)	$\mathbf{I} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	B1
		Attempt to solve $2 - \frac{1}{a-2} = 1$, or $a - \frac{a}{a-2} = 0$, or $-1 + \frac{1}{a-2} = 0$, or $-1 + \frac{2}{a-2} = 1$	M1
		To obtain $a = 3$ only	A1 cso (3) [6]
		Alternatives for (b) If they use $\mathbf{X}^2 + \mathbf{I} = \mathbf{X}$ they need to identify \mathbf{I} for B1, then attempt to solve suitable equation for M1 and obtain $a = 3$ for A1 If they use $\mathbf{X}^2 + \mathbf{X}^{-1} = \mathbf{O}$, they can score the B1then marks for solving If they use $\mathbf{X}^3 + \mathbf{I} = \mathbf{O}$ they need to identify \mathbf{I} for B1, then attempt to solve suitable equation for M1 and obtain $a = 3$ for A1	

Notes:

(a) Attempt ad-bc for first M1

$$\frac{1}{\det} \begin{pmatrix} -1 & -a \\ 1 & 2 \end{pmatrix}$$
 for second M1

(b) Final A1 for correct solution only

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Questio Number	Scheme	Marks
8 (a	The gradient of the tangent is $\frac{1}{q}$ The equation of the tangent is $y - 2aq = \frac{1}{q}(x - aq^2)$	M1 A1 M1
(t	So $yq = x + aq^2$ * R has coordinates (0, aq) The line l has equation $y - aq = -qx$	A1 (4) B1 M1A1
(c		(3) B1 (1) M1:A1 (2) [10]

Notes:

(a)
$$\frac{dy}{dx} = \frac{2a}{2aq}$$
 OK for M1

Use of y = mx + c to find c OK for second M1

Correct solution only for final A1

- (b) -1/(their gradient in part a) in equation OK for M1
- (c) They must attempt y = 0 or x = a to show correct coordinates of R for B1
- (d) Substitute x = -a for M1.

Both coordinates correct for A1.

Ques	stion iber	Scheme	N	/larks
9	(a)	$z_2 = \frac{12 - 5i}{3 + 2i} \times \frac{3 - 2i}{3 - 2i} = \frac{36 - 24i - 15i - 10}{13}$	M1 A1	
	(b)	= 2 - 3i $P(3, 2)$		(2)
		Q(2,-3) $P: B1, Q: B1ft$		B1, B1ft
	(c)	Q(2,-3) $P: B1, Q: B1ftgrad. OP \times \text{grad. } OQ = \frac{2}{3} \times -\frac{3}{2}$		(2)
	OR	$=-1 \Rightarrow \angle POQ = \frac{\pi}{2} (\$)$ $\angle POX = \tan^{-1}\frac{2}{3}, \angle QOX = \tan^{-1}\frac{3}{2}$		
		$Tan(\angle POQ) = \frac{\frac{2}{3} + \frac{3}{2}}{1 - \frac{2}{3} \times \frac{3}{2}}$ M1	M1	
		$\Rightarrow \angle POQ = \frac{\pi}{2} (*) \qquad A1$	A1	(2)
		$z = \frac{3+2}{2} + \frac{2+(-3)}{2}i$	M1	
			A1	(2)
	(e)	$r = \sqrt{\left(\frac{5}{2}\right)^2 + \left(-\frac{1}{2}\right)^2}$	M1	
		$=\frac{\sqrt{26}}{2}$ or exact equivalent	A1	(2) [10]

Notes:

(a)
$$\times \frac{3-2i}{3-2i}$$
 for M1

- (b) Position of points not clear award B1B0
- (c) Use of calculator / decimals award M1A0
- (d) Final answer must be in complex form for A1
- (e) Radius or diameter for M1

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Ques Numl		Scheme	Mar	ks
10	(a)	A represents an enlargement scale factor $3\sqrt{2}$ (centre O)	M1 A1	
		B represents reflection in the line $y = x$ C represents a rotation of $\frac{\pi}{4}$, i.e.45° (anticlockwise) (about O)	B1 B1	(4)
	(b)	$\begin{pmatrix} 3 & -3 \\ 3 & 3 \end{pmatrix}$	M1 A1	(2)
	(c)	$ \begin{pmatrix} 3 & -3 \\ 3 & 3 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} -3 & 3 \\ 3 & 3 \end{pmatrix} $	B1	(1)
	(d)	$ \begin{pmatrix} -3 & 3 \\ 3 & 3 \end{pmatrix} \begin{pmatrix} 0 - 15 & 4 \\ 0 & 15 & 21 \end{pmatrix} = \begin{pmatrix} 0 & 90 & 51 \\ 0 & 0 & 75 \end{pmatrix} $ so $(0, 0)$, $(90, 0)$ and $(51, 75)$	M1A1A	1A1 (4)
	(e)	Area of $\triangle OR'S'$ is $\frac{1}{2} \times 90 \times 75 = 3375$	B1	
		Determinant of E is -18 or use area scale factor of enlargement So area of $\triangle ORS$ is $3375 \div 18 = 187.5$	M1A1	(3) [14]

Notes:

(a) Enlargement for M1 $3\sqrt{2}$ for A1

- (b) Answer incorrect, require CD for M1
- (c) Answer given so require \boldsymbol{DB} as shown for B1
- (d) Coordinates as shown or written as $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$, $\begin{pmatrix} 90 \\ 0 \end{pmatrix}$, $\begin{pmatrix} 51 \\ 75 \end{pmatrix}$ for each A1
- (e) 3375 B1 Divide by theirs for M1