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Mark Scheme (Results)

June 2011

GCE Further Pure FP1 (6667) Paper 1

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6667

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EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
 - M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
 - A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - B marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.

Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- The second mark is dependent on gaining the first mark

Past Paper (Mark Scheme)

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June 2011 6667 Further Pure Mathematics FP1 Mark Scheme

Question Number	Scheme	Notes	Marks
1.	$f(x) = 3^x + 3x - 7$		
(a)	f(1) = -1 $f(2) = 8$	Either any one of $f(1) = -1$ or $f(2) = 8$.	M1
	Sign change (positive, negative) (and $f(x)$ is continuous) therefore (a root) α is between $x = 1$ and $x = 2$.	Both values correct, sign change and conclusion	A1
			(2)
(b)	$f(1.5) = 2.696152423 \ \{ \Rightarrow 1,, \alpha,, 1.5 \}$	f(1.5) = awrt 2.7 (or truncated to 2.6)	B1
		Attempt to find $f(1.25)$.	M1
	$f(1.25) = 0.698222038$ $\Rightarrow 1,, \alpha,, 1.25$	f(1.25) = awrt 0.7 with 1,, α ,, 1.25 or $1 < \alpha < 1.25$ or $[1, 1.25]$ or $(1, 1.25)$. or equivalent in words.	A1
	In (b) there is no credit for lir correct answer with no wor	near interpolation and a	(3)
			5

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Question Number	Scheme	Notes	Marks
2. (a)	$ z_1 = \sqrt{(-2)^2 + 1^2} = \sqrt{5} = 2.236$	$\sqrt{5}$ or awrt 2.24	B1
			(1)
(b)	$\arg z = \pi - \tan^{-1}\left(\frac{1}{2}\right)$	$\tan^{-1}\left(\frac{1}{2}\right) \text{ or } \tan^{-1}\left(\frac{2}{1}\right) \text{ or } \cos^{-1}\left(\frac{2}{\sqrt{5}}\right) \text{ or } \sin^{-1}\left(\frac{2}{\sqrt{5}}\right) \text{ or } \sin^{-1}\left(\frac{1}{\sqrt{5}}\right) \text{ or } \cos^{-1}\left(\frac{1}{\sqrt{5}}\right)$	M1
	= 2.677945045 = 2.68 (2 dp)	awrt 2.68	A1 oe
	Can work in degrees for the method	mark (arg $z = 153.4349488^{\circ}$)	(2)
	$\arg z = \tan^{-1} \left(\frac{1}{-2} \right) = -0.46$	on its own is M0	
	but $\pi + \tan^{-1}(\frac{1}{2}) = 2.68 \text{ so}$	cores M1A1	
	$\pi - \tan^{-1} \left(\frac{1}{2} \right) = \text{is M0 as is}$	$\sin \pi - \tan(\frac{1}{2})$ (2.60)	
(c)	$z^2 - 10z + 28 = 0$	(2)	
	$z = \frac{10 \pm \sqrt{100 - 4(1)(28)}}{2(1)}$	An attempt to use the quadratic formula (usual rules)	M1
	$=\frac{10\pm\sqrt{100-112}}{2}$		
	$=\frac{10\pm\sqrt{-12}}{2}$		
	$=\frac{10\pm2\sqrt{3}\mathrm{i}}{2}$	Attempt to simplify their $\sqrt{-12}$ in terms of i. E.g. i $\sqrt{12}$ or i $\sqrt{3\times4}$	M1
	If their b ² -4ac >0 then only the	, ,	=
	So, $z = 5 \pm \sqrt{3}i$. $\{p = 5, q = 3\}$	$5 \pm \sqrt{3}i$	A1 oe
	Correct answers with no wor	<u> </u>	(3)
	See appendix for alternative soluti		
(d)	<i>y</i> •	Note that the points are $(-2, 1)$, $(5, \sqrt{3})$ and $(5, -\sqrt{3})$.	
	• X	The point $(-2, 1)$ plotted correctly on the Argand diagram with/without label.	B1
	•	The distinct points z_2 and z_3 plotted correctly and symmetrically about the <i>x</i> -axis on the Argand diagram with/without label.	B1√
	The points must be correctly placed relative to each other. If you are in doubt about awarding the marks then consult your team leader or use review.		
	NB the second B mark in (d) depends on ha		
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Question Number	Scheme	Notes	Ma	rks
3. (a)	$\mathbf{A} = \begin{pmatrix} 1 & \ddot{O} \ 2 \\ \ddot{O} \ 2 & -1 \end{pmatrix}$			
(i)	$\mathbf{A}^2 = \begin{pmatrix} 1 & \ddot{O} \ 2 \\ \ddot{O} \ 2 & -1 \end{pmatrix} \begin{pmatrix} 1 & \ddot{O} \ 2 \\ \ddot{O} \ 2 & -1 \end{pmatrix}$			
	$= \begin{pmatrix} 1+2 & \ddot{O} \ 2-\ddot{O} \ 2 \\ \ddot{O} \ 2-\ddot{O} \ 2 & 2+1 \end{pmatrix}$	A correct method to multiply out two matrices. Can be implied by two out of four correct elements.	M1	
	$= \begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$	Correct answer	A1	
				(2)
(ii)	Enlargement ; scale factor 3, centre (0, 0).	Enlargement; scale factor 3, centre (0, 0)	B1; B1	
	Allow 'from' or 'about' for centre and 'C	D' or 'origin' for (0, 0)		(2)
	(0 -1)			()
(b)	$\mathbf{B} = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$			
	Reflection; in the line $y = -x$.	Reflection; $y = -x$	B1; B1	
	Allow 'in the axis' 'about the line. The question does not specify a single transformation combinations that are correct e.g. Anticlockwise rotate by a reflection in the x-axis is acceptable. In cases line completely correct and scored as B2 (no part mark Leader.	on so we would need to accept any ion of 90° about the origin followed ke these, the combination has to be		(2)
(c)	$\mathbf{C} = \begin{pmatrix} k+1 & 12 \\ k & 9 \end{pmatrix}, k \text{ is a constant.}$			
	C is singular \Rightarrow det C = 0. (Can be implied)	$\det \mathbf{C} = 0$	B1	
	Special Case $\frac{1}{9(k+1)-12k} = 0$ B 1	l(implied)M0A0		
	9(k+1) - 12k (= 0) $9k+9 = 12k$	Applies $9(k+1) - 12k$	M1	
	9 = 3k			
	k = 3 with no working can scar	k = 3	A1	(2)
	k = 3 with no working can scor	e tuil marks		(3)
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Question Number	Scheme	Notes	Marks
4.	$f(x) = x^2 + \frac{5}{2x} - 3x - 1, x \neq 0$		
(a)	$f(x) = x^2 + \frac{5}{2}x^{-1} - 3x - 1$		
	$f'(x) = 2x - \frac{5}{2}x^{-2} - 3\{+0\}$	At least two of the four terms differentiated correctly. Correct differentiation. (Allow any correct unsimplified form)	M1 A1
	$\left\{ f'(x) = 2x - \frac{5}{2x^2} - 3 \right\}$		(2)
(b)	$f(0.8) = 0.8^2 + \frac{5}{2(0.8)} - 3(0.8) - 1 = 0.365 = \frac{73}{200}$	A correct numerical expression for f(0.8)	B1
	$f'(0.8) = -5.30625 \left(= \frac{-849}{160} \right)$	Attempt to insert $x = 0.8$ into their $f'(x)$. Does not require an evaluation. (If $f'(0.8)$ is incorrect for their derivative and there is no working score M0)	M1
	$\alpha_2 = 0.8 - \left(\frac{"0.365"}{"-5.30625"}\right)$	Correct application of Newton-Raphson using their values. Does not require an evaluation.	M1
	= 0868786808		
	= 0.869 (3dp)	0.869	A1 cao
	A correct answer only with no working so Ignore any further appl		(4)
	A derivative of $2x - 5(2x)^{-2} - 3$ is quite common		-
	answer of 0.909. This would normally s		
	Similarly for a derivative of $2x - 10x^{-2} - 3$	` /	
	f'(0.8) = -17.025 and a		
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Question Number	Scheme	Notes	Marks
5. (a)	$\mathbf{A} = \begin{pmatrix} -4 & a \\ b & -2 \end{pmatrix}, \text{ where } a \text{ and } b \text{ are constants.}$ $\mathbf{A} \begin{pmatrix} 4 \\ 6 \end{pmatrix} = \begin{pmatrix} 2 \\ -8 \end{pmatrix}$		
	Therefore, $\begin{pmatrix} -4 & a \\ b & -2 \end{pmatrix} \begin{pmatrix} 4 \\ 6 \end{pmatrix} = \begin{pmatrix} 2 \\ -8 \end{pmatrix}$ Do not allow this mark for other incorrect statem e.g. $\begin{pmatrix} 4 \\ 6 \end{pmatrix} \begin{pmatrix} -4 & a \\ b & -2 \end{pmatrix} = \begin{pmatrix} 2 \\ -8 \end{pmatrix}$ would be M0 unless follows.		M1
	So, $-16 + 6a = 2$ and $4b - 12 = -8$ Allow $\begin{pmatrix} -16 + 6a \\ 4b - 12 \end{pmatrix} = \begin{pmatrix} 2 \\ -8 \end{pmatrix}$	Any one correct equation. Any correct horizontal line	M1
	giving $a = 3$ and $b = 1$.	Any one of $a = 3$ or $b = 1$. Both $a = 3$ and $b = 1$.	A1 A1 (4)
(b)	$\det \mathbf{A} = 8 - (3)(1) = 5$	Finds determinant by applying 8 – their ab . $\det \mathbf{A} = 5$	M1 A1
	Special case: The equations -16 + 6b = 2 and 4 from incorrect matrix multiplication. This will in (b).		
	Note that $\det \mathbf{A} = \frac{1}{8 - ab}$ scores M0 here but the beware $\det \mathbf{A} = \frac{1}{8 - ab} = \frac{1}{5} \Rightarrow area S = \frac{30}{\frac{1}{5}} = 150$	ne following 2 marks are available. However,	
	This scores M0A0 M1A0 Area $S = (\det \mathbf{A})(\text{Area } R)$		
	Area $S = 5 \times 30 = 150 \text{ (units)}^2$	$\frac{30}{\text{their det } \mathbf{A}} \text{ or } 30 \times (\text{their det } \mathbf{A})$ 150 or ft answer	M1 A1 √
	If their det A < 0 then allow ft provided final answer > 0 In (b) Candidates may take a more laborious route for the area scale factor and find the area of the unit square, for example, after the transformation represented by A. This needs to be a complete method to score any marks. Correctly establishing the area scale factor M1. Correct answer 5 A1. Then mark as original scheme.		

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Question Number	Scheme	Notes	Marks
6.	$z + 3iz^* = -1 + 13i$		
	(x+iy)+3i(x-iy)	$z^* = x - iy$ Substituting $z = x + iy$ and their z^* into $z + 3iz^*$	B1 M1
	x + i y + 3i x + 3 y = -1 + 13i	Correct equation in x and y with $i^2 = -1$. Can be implied.	A1
	(x+3y)+i(y+3x)=-1+13i		
	Re part: $x + 3y = -1$ Im part: $y + 3x = 13$	An attempt to equate real and imaginary parts. Correct equations.	M1 A1
	3x + 9y = -3 $3x + y = 13$		
	$8y = -16 \implies y = -2$	Attempt to solve simultaneous equations to find one of x or y. At least one of the equations must contain both x and y terms.	M1
	$x + 3y = -1 \implies x - 6 = -1 \implies x = 5$	Both $x = 5$ and $y = -2$.	A1
	$\left\{ z = 5 - 2i \right\}$		(7

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Question Number	Scheme	Notes	Mai	rks
7.	$\{S_n = \} \sum_{r=1}^n (2r-1)^2$			
(a)	$= \sum_{r=1}^{n} 4r^2 - 4r + 1$	Multiplying out brackets and an attempt to use at least one of the two standard formulae correctly.	M1	
	$= 4.\frac{1}{6}n(n+1)(2n+1) - 4.\frac{1}{2}n(n+1) + n$	First two terms correct. + n	A1 B1	
	$= \frac{2}{3}n(n+1)(2n+1) - 2n(n+1) + n$			
	$= \frac{1}{3}n\{2(n+1)(2n+1) - 6(n+1) + 3\}$	Attempt to factorise out $\frac{1}{3}n$	M1	
	$= \frac{3}{3}n\{2(n+1)(2n+1) - 6(n+1) + 5\}$	Correct expression with $\frac{1}{3}n$ factorised out with no errors seen.	A1	
	$= \frac{1}{3}n\{2(2n^2+3n+1) - 6(n+1) + 3\}$			
	$= \frac{1}{3}n\{4n^2+6n+2-6n-6+3\}$			
	$= \frac{1}{3}n(4n^2-1)$			
	$= \frac{1}{3}n(2n+1)(2n-1)$	Correct proof. No errors seen.	A1 *	(6)
	Note that there are no marks	for proof by induction.		(6)
(b)	$\sum_{r=n+1}^{3n} (2r-1)^2 = S_{3n} - S_n$			
	$= \frac{1}{3} \cdot 3n(6n+1)(6n-1) - \frac{1}{3}n(2n+1)(2n-1)$	Use of $S_{3n} - S_n$ or $S_{3n} - S_{n+1}$ with the result from (a) used at least once. Correct unsimplified expression. E.g. Allow 2(3n) for 6n.	M1 A1	
	Note that (b) says hence so they hav $= n(36n^2 - 1) - \frac{1}{3}n(4n^2 - 1)$	•		
	$= \frac{1}{3}n(108n^2 - 3 - 4n^2 + 1)$	Factorising out $\frac{1}{3}n$ (or $\frac{2}{3}n$)	dM1	
	$= \frac{1}{3}n(104n^2 - 2)$			
	$= \frac{2}{3}n(52n^2 - 1)$	$\frac{2}{3}n(52n^2-1)$	A1	
	${a=52, b=-1}$			(4)
				10

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Question Number	Scheme	Notes	Marks
8.	$C: y^2 = 48x$ with general point $P(12t^2, 24t)$.		
0.	(121 , 241).		
(a)	$y^2 = 4ax \implies a = \frac{48}{4} = 12$	Using $y^2 = 4ax$ to find a.	M1
	So, directrix has the equation $x + 12 = 0$	x + 12 = 0	A1 oe
	Correct answer with no work	ing allow full marks	(2)
(b)	$y = \sqrt{48} x^{\frac{1}{2}} \implies \frac{dy}{dx} = \frac{1}{2} \sqrt{48} x^{-\frac{1}{2}} \left(= 2\sqrt{3} x^{-\frac{1}{2}} \right)$ or (implicitly) $y^2 = 48x \implies 2y \frac{dy}{dx} = 48$	$\frac{dy}{dx} = \pm k x^{-\frac{1}{2}}$ $ky \frac{dy}{dx} = c$	
	or (chain rule) $\frac{dy}{dx} = \frac{dy}{dt} \times \frac{dt}{dx} = 24 \times \frac{1}{24t}$	their $\frac{dy}{dt} \times \left(\frac{1}{\text{their } \frac{dx}{dt}} \right)$	M1
	When $x = 12t^2$, $\frac{dy}{dx} = \frac{\sqrt{48}}{2\sqrt{12t^2}} = \frac{\sqrt{4}}{2t} = \frac{1}{t}$ or $\frac{dy}{dx} = \frac{48}{2y} = \frac{48}{48t} = \frac{1}{t}$	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{t}$	A1
	T : $y - 24t = \frac{1}{t}(x - 12t^2)$	Applies $y - 24t = \text{their } m_T (x - 12t^2)$ or $y = (\text{their } m_T)x + c$ using $x = 12t^2$ and $y = 24t$ in an attempt to find c. Their m_T must be a function of t .	M1
	$\mathbf{T}: \ ty - 24t^2 = x - 12t^2$		
	T : $x - ty + 12t^2 = 0$	Correct solution.	A1 cso *
	Special case: If the gradient is quoted as Commons $P(12x^2, 24x)$ with $(2, 12)$ gives $(2, 12)$		(4)
(c)	Compare $P(12t^2, 24t)$ with $(3, 12)$ gives $t = \frac{1}{2}$. NB $x - ty + 12t^2 = 0$ with $x = 3$ and $y = 12$ gives 4	$t = \frac{1}{2}$ $t^2 - 4t + 1 = 0 = (2t - 1)^2 \Rightarrow t = \frac{1}{2}$	B1
	$t = \frac{1}{2}$ into T gives $x - \frac{1}{2}y + 3 = 0$	Substitutes their t into \mathbf{T} .	M1
	See Appendix for an alternative app	proach to find the tangent	
	At X , $x = -12 \Rightarrow -12 - \frac{1}{2}y + 3 = 0$	Substitutes their x from (a) into \mathbf{T} .	M1
	So, $-9 = \frac{1}{2}y \implies y = -18$		
	So the coordinates of <i>X</i> are $(-12, -18)$.	(-12, -18)	A1
	The coordinates must be together at the end for the	/	(4)
			10
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Question Number	Scheme	Notes	Marks
9. (a)	$n=1$; LHS = $\begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^1 = \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}$		
	RHS = $\begin{pmatrix} 3^1 & 0 \\ 3(3^1 - 1) & 1 \end{pmatrix} = \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}$		
	As LHS = RHS, the matrix result is true for $n = 1$.	Check to see that the result is true for $n = 1$.	B1
	Assume that the matrix equation is true for $n = k$, ie. $\begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^k = \begin{pmatrix} 3^k & 0 \\ 3(3^k - 1) & 1 \end{pmatrix}$		
	With $n = k+1$ the matrix equation becomes $\begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^{k+1} = \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^{k} \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}$		
	$= \begin{pmatrix} 3^k & 0 \\ 3(3^k - 1) & 1 \end{pmatrix} \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix} \text{or} \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix} \begin{pmatrix} 3^k & 0 \\ 3(3^k - 1) & 1 \end{pmatrix}$	$\begin{pmatrix} 3^k & 0 \\ 3(3^k - 1) & 1 \end{pmatrix} $ by $\begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}$	M1
	$= \begin{pmatrix} 3^{k+1} + 0 & 0 + 0 \\ 9(3^k - 1) + 6 & 0 + 1 \end{pmatrix} \text{or} \begin{pmatrix} 3^{k+1} + 0 & 0 + 0 \\ 6 \cdot 3^k + 3(3^k - 1) & 0 + 1 \end{pmatrix}$	Correct unsimplified matrix with no errors seen.	A1
	$= \begin{pmatrix} 3^{k+1} & 0 \\ 9(3^k) - 3 & 1 \end{pmatrix}$		
	$= \begin{pmatrix} 3^{k+1} & 0 \\ 3(3(3^k) - 1) & 1 \end{pmatrix}$		
	$= \begin{pmatrix} 3^{k+1} & 0 \\ 3(3^{k+1} - 1) & 1 \end{pmatrix}$	Manipulates so that $k \rightarrow k+1$ on at least one term. Correct result with no errors seen with some working between this and the previous A1	dM1
	If the result is true for $n = k$, (1) then it is now true for $n = k+1$. (2) As the result has shown to be true for $n = 1$, (3) then the result is true for all n . (4) All 4 aspects need to be mentioned at some point for the last A1 .	Correct conclusion with all previous marks earned	A1 cso
		•	(6)



Question Number	Scheme	Notes	Marks
9. (b)	$f(1) = 7^{2-1} + 5 = 7 + 5 = 12,$	Shows that $f(1) = 12$.	B1
	{which is divisible by 12}. { \therefore f (n) is divisible by 12 when $n = 1$.}		
	Assume that for $n = k$,		
	$f(k) = 7^{2k-1} + 5 \text{ is divisible by } 12 \text{ for } k \in \mathcal{C}^+.$		
	So, $f(k+1) = 7^{2(k+1)-1} + 5$	Correct unsimplified expression for $f(k + 1)$.	B1
	giving, $f(k+1) = 7^{2k+1} + 5$		
	$\therefore f(k+1) - f(k) = (7^{2k+1} + 5) - (7^{2k-1} + 5)$	Applies $f(k+1) - f(k)$. No simplification is necessary and condone missing brackets.	M1
	$=7^{2k+1}-7^{2k-1}$		
	$= 7^{2k-1} \left(7^2 - 1 \right)$	Attempting to isolate 7 ^{2k-1}	M1
	$=48\left(7^{2k-1}\right)$	$48(7^{2k-1})$	A1cso
	$\therefore f(k+1) = f(k) + 48(7^{2k-1}), \text{ which is divisible by}$		_
	12 as both $f(k)$ and $48(7^{2k-1})$ are both divisible by	Compost complyation with me	
	12.(1) If the result is true for $n = k$, (2) then it is now true for $n = k+1$. (3) As the result has shown to be true for $n = 1$,(4) then the result is true for all n . (5).	Correct conclusion with no incorrect work. Don't condone missing brackets.	A1 cso
	All 5 aspects need to be mentioned at some point for the last A1.		
	There are other ways of proving this by induction. If you are in any doubt consult your team leader		(6)
			12

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Appendix

Question Number	Scheme	Notes	Marks
Aliter			
2. (c)	$z^2 - 10z + 28 = 0$		
Way 2			
	$(z-5)^2 - 25 + 28 = 0$	$(z \pm 5)^2 \pm 25 + 28 = 0$	M1
	$\left(z-5\right)^2=-3$		
	$z - 5 = \sqrt{-3}$		
	$z - 5 = \sqrt{3}i$	Attempt to express their $\sqrt{-3}$	M1
	· •	in terms of i.	
	0 5 5	5 . 5:	
	So, $z = 5 \pm \sqrt{3}i$. $\{p = 5, q = 3\}$	$5 \pm \sqrt{3}i$	A1 oe
			(3)

Scheme		Mar	ks
$z^{2} - 10z + 28 = 0$ $\left(z - \left(p + i\sqrt{q}\right)\right)\left(z - \left(p - i\sqrt{q}\right)\right) = z^{2} - 2pz + p^{2} + q$ $2p = \pm 10 and p^{2} \pm q = 28$ $2p = \pm 10 \Rightarrow p = 5$ $p = 5 and q = 3$	Uses sum and product of roots Attempt to solve for $p(\text{or }q)$	M1 M1 A1	(3)
	$z^{2} - 10z + 28 = 0$ $\left(z - \left(p + i\sqrt{q}\right)\right)\left(z - \left(p - i\sqrt{q}\right)\right) = z^{2} - 2pz + p^{2} + q$ $2p = \pm 10 and p^{2} \pm q = 28$ $2p = \pm 10 \Rightarrow p = 5$	$z^{2} - 10z + 28 = 0$ $\left(z - \left(p + i\sqrt{q}\right)\right)\left(z - \left(p - i\sqrt{q}\right)\right) = z^{2} - 2pz + p^{2} + q$ $2p = \pm 10 and p^{2} \pm q = 28$ $2p = \pm 10 \Rightarrow p = 5$ Uses sum and product of roots $2p = \pm 10 \Rightarrow p = 5$ Attempt to solve for $p(\text{or } q)$	$z^{2} - 10z + 28 = 0$ $\left(z - \left(p + i\sqrt{q}\right)\right)\left(z - \left(p - i\sqrt{q}\right)\right) = z^{2} - 2pz + p^{2} + q$ $2p = \pm 10 and p^{2} \pm q = 28$ $2p = \pm 10 \Rightarrow p = 5$ Uses sum and product of roots $2p = \pm 10 \Rightarrow p = 5$ Attempt to solve for $p(\text{or } q)$

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Question Number	Scheme	Notes	Marks
Aliter			
8. (c)	$\frac{dy}{dx} = 2\sqrt{3} x^{-\frac{1}{2}} = \frac{2\sqrt{3}}{\sqrt{3}} = 2$		B1
Way 2			
	Gives $y - 12 = 2(x - 3)$	Uses (3, 12) and their "2" to find the equation of the tangent.	M1
		T	
	$x = -12 \Rightarrow y - 12 = 2(-12 - 3)$	Substitutes their <i>x</i> from (a) into their tangent	M1
	y = -18		
	So the coordinates of <i>X</i> are $(-12, -18)$.		A1
		,	(4)

Question Number	Scheme	Notes	Marks
Aliter			
9. (b)	$f(1) = 7^{2-1} + 5 = 7 + 5 = 12,$	Shows that $f(1) = 12$.	B1
Way 2	{which is divisible by 12}.		
	$\{ : f(n) \text{ is divisible by } 12 \text{ when } n = 1. \}$		
	Assume that for $n = k$,		
	$f(k) = 7^{2k-1} + 5$ is divisible by 12 for $k \in \mathcal{C}^+$.		
	So, $f(k+1) = 7^{2(k+1)-1} + 5$	Correct expression for $f(k + 1)$.	B1
	giving, $f(k+1) = 7^{2k+1} + 5$		
	$7^{2k+1} + 5 = 49 \times 7^{2k-1} + 5$	Attempt to isolate 7 ^{2k-1}	M1
	$=49\times \left(7^{2k-1}+5\right)-240$	M1 Attempt to isolate $7^{2k-1} + 5$	M1
	$f(k+1) = 49 \times f(k) - 240$	Correct expression in terms of $f(k)$	A1
	As both $f(k)$ and 240 are divisible by 12 then so is $f(k + 1)$. If the result is true for $n = k$, then it		
	is now true for $n = k+1$. As the result has	Correct conclusion	A1
	shown to be true for $n = 1$, then the result is true		
	for all n.		
			(6)

Past Paper (Mark Scheme)



Question Number	Scheme	Notes	Marks
4 124 am			
Aliter 9. (b)	$f(1) = 7^{2-1} + 5 = 7 + 5 = 12,$	Shows that $f(1) = 12$.	— B1
Way 3	$\{$ which is divisible by 12 $\}$.	510 %5 that 1 (1) 12.	B1
way 5	{ \therefore f (n) is divisible by 12 when $n = 1$.}		
	Assume that for $n = k$, $f(k)$ is divisible by 12		
	$so f(k) = 7^{2k-1} + 5 = 12m$		
	So, $f(k+1) = 7^{2(k+1)-1} + 5$	Correct expression for $f(k + 1)$.	B1
	giving, $f(k+1) = 7^{2k+1} + 5$		
	$7^{2k+1} + 5 = 7^2 \cdot 7^{2k-1} + 5 = 49 \times 7^{2k-1} + 5$	Attempt to isolate 7 ^{2k-1}	M1
	$=49\times(12m-5)+5$	Substitute for <i>m</i>	M1
	$f(k+1) = 49 \times 12m - 240$	Correct expression in terms of <i>m</i>	A1
	As both $49 \times 12m$ and 240 are divisible by 12 then so is $f(k + 1)$. If the result is true for $n = k$,		
	then it is now true for $n = k+1$. As the result	Correct conclusion	A1
	has shown to be true for $n = 1$, then the result is		
	true for all <i>n</i> .		
			(6)

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Question Number	Scheme	Notes	Marks
Aliter			
9. (b)	$f(1) = 7^{2-1} + 5 = 7 + 5 = 12,$	Shows that $f(1) = 12$.	B1
Way 4	{which is divisible by 12}.		-
	$\{ :: f(n) \text{ is divisible by } 12 \text{ when } n = 1. \}$		-
	Assume that for $n = k$,		-
	$f(k) = 7^{2k-1} + 5$ is divisible by 12 for $k \in \mathcal{C}^+$.		_
	$f(k+1) + 35f(k) = 7^{2(k+1)-1} + 5 + 35(7^{2k-1} + 5)$	Correct expression for $f(k + 1)$.	B1
	$f(k+1) + 35f(k) = 7^{2k+1} + 5 + 35(7^{2k-1} + 5)$	Add appropriate multiple of $f(k)$ For 7^{2k} this is likely to be 35 (119, 203,.) For 7^{2k-1} 11 (23, 35, 47,)	M1
	giving, $7.7^{2k} + 5 + 5.7^{2k} + 175$	Attempt to isolate 7 ^{2k}	M1
	$=180+12\times 7^{2k}=12(15+7^{2k})$	Correct expression	A1
	:. $f(k+1) = 12(7^{2k} + 15) - 35f(k)$. As both $f(k)$		-
	and $12(7^{2k} + 15)$ are divisible by 12 then so is		
	f(k + 1). If the result is true for $n = k$, then it is now true for $n = k+1$. As the result has shown	Correct conclusion	A1
	to be true for $n = 1$, then the result is true for all		
	<i>n</i> .		(6)

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