

Mark Scheme (Results)

Summer 2013

GCE Further Pure Mathematics 1 (6667/01)





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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- ***** The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.
- 8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme

General Principles for Pure Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

- 1. Factorisation
 - $(x^2 + bx + c) = (x + p)(x + q)$, where |pq| = |c|, leading to x =

 $(ax^2 + bx + c) = (mx + p)(nx + q)$, where |pq| = |c| and |mn| = |a|, leading to x =

2. Formula

Attempt to use <u>correct</u> formula (with values for *a*, *b* and *c*).

3. Completing the square

Solving $x^2 + bx + c = 0$: $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c$, $q \neq 0$, leading to x = ...

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ($x^n \rightarrow x^{n-1}$)

2. Integration

Power of at least one term increased by 1. ($x^n \rightarrow x^{n+1}$)

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an <u>exact</u> answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Answers without working

The rubric says that these <u>may</u> not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

| Question Number | Scheme | Notes | Marks |
|--------------------|---|--|---------|
| 1. | $\mathbf{M} = \begin{pmatrix} x \\ 3x - x \end{pmatrix}$ | $ \begin{array}{c} x-2 \\ -6 & 4x-11 \end{array} $ | |
| | $\det \mathbf{M} = x(4x - 11) - (3x - 6)(x - 2)$ | Correct attempt at determinant | M1 |
| | $x^2 + x - 12$ (=0) | Correct 3 term quadratic | A1 |
| | $(x+4)(x-3) (=0) \rightarrow x =$ | Their $3TQ = 0$ and attempts to solve relevant quadratic using factorisation or completing the square or correct quadratic formula leading to $x =$ | M1 |
| | x = -4, x = 3 | Both values correct | A1 |
| | | | (4) |
| | | | Total 4 |
| Notes | | I | |
| | x(4x - 11) = (3x - 6)(x - 2) award first M1 | | |
| | $\pm (x^2 + x - 12)$ seen award first M1A1 | | |
| | Method mark for solving 3 term quadratic 1. <u>Factorisation</u> $(x^2 + bx + c) = (x + p)(x + q)$, where $ pq $ = | | |
| | $(ax^{2}+bx+c) = (mx+p)(nx+q)$, where | pq = c and $ mn = a $, leading to x = | |
| | 2. <u>Formula</u> Attempt to use <u>correct</u> formula (with values for a, b and c). | | |
| | 3. <u>Completing the square</u> | | |
| | Solving $x^2 + bx + c = 0$: $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c$, $q \neq 0$, leading to x = | | |
| | Both correct with no working 4/4, only one correct 0/4 | | |

| Question Number | Scheme | Notes | Marks |
|--------------------|--|--|---------|
| 2 | $f(x) = \cos(x)$ | $(x^{2}) - x + 3$ | |
| (a) | f(2.5) = 1.499 f(3) = -0.9111 | Either any one of $f(2.5) = awrt \ 1.5$ or $f(3) = awrt \ -0.91$ | M1 |
| | Sign change (positive, negative) (and $f(x)$ is continuous) therefore root or equivalent. | Both $f(2.5) = awrt 1.5$ and $f(3) = awrt -0.91$, sign change and conclusion. | A1 |
| | Use of degrees gives $f(2.5) = 1.494$ and $f(3) = 0.988$ which is awarded M1A0 | | (2) |
| (b) | $\frac{3-\alpha}{"0.91113026188"} = \frac{\alpha - 2.5}{"1.4994494182"}$ | Correct linear interpolation method – accept equivalent equation - ensure signs are correct. | M1 A1ft |
| | $\alpha = \frac{3 \times 1.499 + 2.5 \times 0.9111}{1.499 + 0.9111}$ | | |
| | $\alpha = 2.81 (2d.p.)$ | cao | A1 |
| | | | (3) |
| | | | Total 5 |
| Notes | Alternative (b) | | |
| | Gradient of line is $-\frac{'1.499'+'0.9111'}{0.5}$ (= -4.82) (3sf). Attempt to find equation of | | |
| | straight line and equate y to 0 award M1 and A1 | ft for their gradient awrt 3sf. | |

| Question Number | Scheme | Notes | Marks |
|--------------------|--|--|---------|
| 3 (a) | Ignore part labels and mark part (a) and part | t (b) together. | |
| | $f\left(\frac{1}{2}\right) = 2\left(\frac{1}{2}\right)^{3} - 9\left(\frac{1}{2}\right)^{2} + k\left(\frac{1}{2}\right) - 13$ | Attempts f(0.5) | M1 |
| | $\left(\frac{1}{4}\right) - \left(\frac{9}{4}\right) + \left(\frac{k}{2}\right) - 13 = 0 \Longrightarrow k = \dots$ | Sets $f(0.5) = 0$ and leading to $k=$ | dM1 |
| | k = 30 | cao | A1 |
| | Alternative using | glong division: | |
| | $2x^3 - 9x^2 + kx - 13 \div (2x - 1)$ | | |
| | $= x^{2} - 4x + \frac{1}{2}k - 2$ (Quotient) | Full method to obtain a remainder as a function of k | M1 |
| | Remainder $\frac{1}{2}k - 15$ | | |
| | $\frac{1}{2}k - 15 = 0$ | Their remainder = 0 | dM1 |
| | <i>k</i> = 30 | | A1 |
| | Alternative by | v inspection: | |
| | | First M for $(2x-1)(x^2+bx+c)$ or | |
| | $(2x-1)(x^2-4x+13) = 2x^3-9x^2+30x-13$ | $(x-\frac{1}{2})(2x^2+bx+c)$ | M1dM1 |
| | | Second M1 for $ax^2 + bx + c$ where ($b = -4$ or $c = 13$)or ($b = -8$ or $c = 26$) | |
| | k = 30 | | A1 |
| | | | (3) |
| (b) | $f(x) = (2x-1)(x^2 - 4x + 13)$ | M1: $(x^2 + bx \pm 13)$ or $(2x^2 + bx \pm 26)$ Uses inspection or long division or compares coefficients and $(2x - 1)$ or | M1 |
| | $or\left(x-\frac{1}{2}\right)\left(2x^2-8x+26\right)$ | $\left(x-\frac{1}{2}\right)$ to obtain a quadratic factor of this form. | |
| | $x^2 - 4x + 13$ or $2x^2 - 8x + 26$ | A1 $(x^2 - 4x + 13)$ or $(2x^2 - 8x + 26)$ seen | A1 |
| | $x = \frac{4 \pm \sqrt{4^2 - 4 \times 13}}{2}$ or equivalent | Use of correct quadratic formula for their $\underline{3TQ}$ or completes the square. | M1 |
| | $x = \frac{4 \pm 6i}{2} = 2 \pm 3i$ | oe | A1 |
| | | | (4) |
| | | | Total 7 |

| Question Number | Scheme | Notes | Marks |
|--------------------|---|---|----------------|
| 4(a) | $y = \frac{4}{x} = 4x^{-1} \implies \frac{dy}{dx} = -4x^{-2} = -\frac{4}{x^2}$ | $\frac{\mathrm{d}y}{\mathrm{d}x} = k \; x^{-2}$ | |
| | $xy = 4 \Longrightarrow x \frac{\mathrm{d}y}{\mathrm{d}x} + y = 0$ | Use of the product rule. The sum of two terms including dy/dx , one of which is correct. | M1 |
| | $\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\mathrm{d}y}{\mathrm{d}t} \cdot \frac{\mathrm{d}t}{\mathrm{d}x} = -\frac{2}{t^2} \cdot \frac{1}{2}$ | their $\frac{dy}{dt} \times \left(\frac{1}{\text{their}\frac{dx}{dt}}\right)$ | |
| | $\frac{dy}{dx} = -4x^{-2} \text{ or } x \frac{dy}{dx} + y = 0 \text{ or } \frac{dy}{dx} = -\frac{2}{t^2} \cdot \frac{1}{2}$ or equivalent expressions | Correct derivative $-4x^{-2}$, $-\frac{y}{x}$ or $\frac{-1}{t^2}$ | A1 |
| | So, $m_N = t^2$ | Perpendicular gradient rule $m_N m_T = -1$ | M1 |
| | $y - \frac{2}{t} = t^2 \left(x - 2t \right)$ | $y - \frac{2}{t}$ = their $m_N (x - 2t)$ or $y = mx + c$ with their m_N and $(2t, \frac{2}{t})$ in an attempt to find 'c'. Their gradient of the normal must be different from their gradient of the tangent and have come from calculus and should be a function of t. | M1 |
| | $ty - t^3 x = 2 - 2t^4 *$ | | A1* cso |
| (b) | $t = -\frac{1}{2} \Longrightarrow -\frac{1}{2} y - \left(-\frac{1}{2}\right)^3 x = 2 - 2\left(-\frac{1}{2}\right)^4$ | Substitutes the given value of <i>t</i> into the normal | (5) M1 |
| | 4y - x + 15 = 0 | | |
| | $y = \frac{4}{x} \Longrightarrow x^2 - 15x - 16 = 0 \text{ or}$ $\left(2t, \frac{2}{t}\right) \rightarrow \frac{8}{t} - 2t + 15 = 0 \Longrightarrow 2t^2 - 15t - 8 = 0 \text{ or}$ $x = \frac{4}{y} \Longrightarrow 4y^2 + 15y - 4 = 0.$ $(x+1)(x-16) = 0 \Longrightarrow x = \text{ or}$ | Substitutes to give a quadratic | M1 |
| | $(x+1)(x-16) = 0 \Rightarrow x = \text{ or}$ $(2t+1)(t-8) = 0 \Rightarrow t = \text{ or}$ $(4y-1)(y+4) = 0 \Rightarrow y =$ | Solves their 3TQ | M1 |
| | $(P: x = -1, y = -4)(Q:)x = 16, y = \frac{1}{4}$ | Correct values for <i>x</i> and <i>y</i> | A1 |
| | | | (4) Total 9 |

| Question Number | Scheme | Notes | Marks |
|--------------------|---|--|----------|
| 5(a) | $(r+2)(r+3) = r^2 + 5r + 6$ | | B1 |
| | $\sum \left(r^2 + 5r + 6\right) = \frac{1}{6}n(n+1)(2n+1) + 5 \times \frac{1}{2}n(n+1), +6n$ | M1: Use of correct expressions for $\sum r^2$ and $\sum r$ | M1,B1ft |
| | | B1ft: $\sum k = nk$ | |
| | | M1:Factors out <i>n</i> ignoring treatment of constant. | |
| | $= \frac{1}{3}n\left[\frac{1}{2}(n+1)(2n+1) + \frac{15}{2}(n+1) + 18\right]$ | A1: Correct expression with $\frac{1}{3}n$ or $\frac{1}{6}n$ factored out, allow recovery. | M1 A1 |
| | $\left(= \frac{1}{3}n \left[n^2 + \frac{3}{2}n + \frac{1}{2} + \frac{15}{2}n + \frac{15}{2} + 18 \right] \right)$ $= \frac{1}{3}n \left[n^2 + 9n + 26 \right] *$ | Correct completion to printed answer | A1*cso |
| | | I | (6) |
| 5(b) | $\sum_{r=n+1}^{3n} = \frac{1}{3}3n\left(\left(3n\right)^2 + 9\left(3n\right) + 26\right) - \frac{1}{3}n\left(n^2 + 9n + 26\right)$ | M1: $f(3n) - f(n \text{ or } n+1)$ and attempt to use part (a). A1: Equivalent correct expression | M1A1 |
| | 3f(n) - f(n or n+1) is M0 | | |
| | $(=n(9n^{2}+27n+26)-\frac{1}{3}n(n^{2}+9n+26))$ | | |
| | $=\frac{2}{3}n\left(\frac{27}{2}n^2+\frac{81}{2}n+39-\frac{1}{2}n^2-\frac{9}{2}n-13\right)$ | Factors out $=\frac{2}{3}n$ dependent on previous M1 | dM1 |
| | $=\frac{2}{3}n(13n^2+36n+26)$ | Accept correct expression. | A1 |
| | (a = 13, b = 36, c = 26) | | |
| | | | (4) |
| | | | Total 10 |

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Past Paper (Mark Scheme)

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| $\frac{dx}{y^2 = 4ax \Rightarrow 2y\frac{dy}{dx} = 4a}$ $\frac{y^2 = 4ax \Rightarrow 2y\frac{dy}{dx} = 4a}{y\frac{dx}{dt} = 2a, \frac{1}{2ap}}$ $\frac{dy}{dx} \approx \frac{1}{dt}, \text{ Can be a function of } p \text{ or } l.$ $\frac{dy}{dx} = a^{\frac{1}{2}x^{-\frac{1}{2}}} \text{ or } 2y\frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a, \frac{1}{2ap}$ $\frac{dy}{dx} = a^{\frac{1}{2}x^{-\frac{1}{2}}} \text{ or } 2y\frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a, \frac{1}{2ap}$ $y - 2ap = \frac{1}{p}(x - ap^2)$ $\frac{Applies}{y - 2ap} = \frac{1}{p}(x - ap^2)$ $\frac{Applies}{y - 2ap} = \frac{1}{p}(x - ap^2)$ $\frac{ap^2 - ap^2 = ap^2 *}{y - 2ap} = \frac{1}{p}(x - ap^2)$ $\frac{ap^2 - x - aq^2}{y} = \frac{1}{p}(x - ap^2)$ $\frac{ap^2 - x - aq^2}{y} = \frac{1}{p}(x - ap^2)$ $\frac{Attempt to obtain an equation in one variable x or y}{variable x or y}$ $\frac{ap^2 - ap^2}{y - ap^2}$ $\frac{aq^2 - ap^2}{q - p}$ $aq^2 -$ | Question Number | Scheme | Notes | Marks |
|--|--------------------|---|--|--------|
| $rac{dy}{dx} = \frac{dy}{dt}, \frac{dt}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{dy}{dt}, \frac{dt}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{d}{dt}, \frac{d}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{d}{dt}, \frac{d}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{d}{a}, \frac{1}{x}, \frac{1}{2} \text{ or } 2y, \frac{d}{dt} = 4a \text{ or } \frac{dy}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{d}{a}, \frac{1}{x}, \frac{1}{2} \text{ or } 2y, \frac{d}{dt} = 4a \text{ or } \frac{d}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{d}{a}, \frac{1}{x}, \frac{1}{2} \text{ or } 2y, \frac{d}{dt} = 4a \text{ or } \frac{d}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{d}{a}, \frac{1}{x}, \frac{1}{2} \text{ or } 2y, \frac{d}{dt} = 4a \text{ or } \frac{d}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{d}{a}, \frac{1}{x}, \frac{1}{2} \text{ or } 2y, \frac{d}{dt} = 4a \text{ or } \frac{d}{dt} = 2a, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{1}{a}, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{1}{a}, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{1}{a}, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{1}{a}, \frac{1}{a}, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{1}{a}, \frac{1}{a}, \frac{1}{2ap}$ $rac{dy}{dt} = \frac{1}{a}, \frac{1}{a}$ | 6(a) | $y = 2a^{\frac{1}{2}}x^{\frac{1}{2}} \Longrightarrow \frac{\mathrm{d}y}{\mathrm{d}x} = a^{\frac{1}{2}}x^{-\frac{1}{2}}$ | $x^{\frac{1}{2}} \rightarrow x^{-\frac{1}{2}}$ | |
| $\frac{dx}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a \cdot \frac{1}{2ap}$ Differentiation is accurate. $A1$ $\frac{dy}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a \cdot \frac{1}{2ap}$ Differentiation is accurate. $A1$ $\frac{dy}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a \cdot \frac{1}{2ap}$ Differentiation is accurate. $A1$ $\frac{dy}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a \cdot \frac{1}{2ap}$ Differentiation is accurate. $A1$ $\frac{dy}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a \cdot \frac{1}{2ap}$ Differentiation is accurate. $A1$ $\frac{dy}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a \cdot \frac{1}{2ap}$ Differentiation is accurate. $A1$ $\frac{dy}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a \cdot \frac{1}{2ap}$ Differentiation is accurate. $\frac{dy}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 4a \text{ or } \frac{dy}{dx} = 2a \cdot \frac{1}{2ap}$ Differentiation is accurate. $\frac{dy}{dx} = a^{\frac{1}{2}} (x - ap^{2})$ $\frac{dy}{dx} = a^{\frac{1}{2}} (x - ap^{2})$ Correct completion to printed answer* $\frac{dy}{dx} = a^{\frac{1}{2}} x^{\frac{1}{2}} \text{ or } y$ Differentiation is accurate. $\frac{dy}{dy} = x = aq^{2}$ B1 $\frac{dy}{dy} = x = aq^{2}$ $\frac{dy}{dy} = a^{\frac{1}{2}} - ap^{2}$ Attempt to obtain an equation in one variable x or y M1 $\frac{dy}{dy} = a^{\frac{1}{2}} - ap^{2}$ Attempt to isolate x or y $\frac{dy}{dy} = a^{\frac{1}{2}} - ap^{\frac{1}{2}}$ $\frac{dy}{dy} = a^{\frac{1}{2}} - ap^{\frac{1}{2}}$ Attempt to isolate x or y $\frac{dy}{dy} = a^{\frac{1}{2}} - ap^{\frac{1}{2}}$ $\frac{dy}{dy} = a^{\frac{1}{$ | | $y^2 = 4ax \Longrightarrow 2y \frac{dy}{dx} = 4a$ | $ky\frac{\mathrm{d}y}{\mathrm{d}x} = c$ | M1 |
| $y - 2ap = \frac{1}{p}(x - ap^{2})$ $y = (\text{their } m)x + c \text{ using } x = ap^{2} \text{ and } y = 2ap \text{ in an attempt to find } c. Their m must be a function of p from calculus.}$ $py - x = ap^{2} *$ $Correct completion to printed answer* All cso$ (c) $qy - aq^{2} = py - ap^{2}$ $y = \frac{aq^{2} - ap^{2}}{q - p}$ $y = a(p + q)or ap + aq x = ap^{2}$ (c) (d) (d) $pq = -1$ $Answer only: Scores 2/2 if x coordinate of R = -a$ $M1$ | | or $\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = 2a \cdot \frac{1}{2ap}$ | $\frac{dy}{dt} \times \frac{1}{\frac{dx}{dt}}$. Can be a function of <i>p</i> or <i>t</i> . | |
| $y - 2ap = \frac{1}{p}(x - ap^{2})$ or $y = (\text{their } m)x + c \text{ using}$ $x = ap^{2} and y = 2ap \text{ in an attempt to find}$ c. Their m must be a function of p from calculus. $py - x = ap^{2} *$ Correct completion to printed answer* A1 cso (c) $qy - aq^{2} = py - ap^{2}$ $y = \frac{aq^{2} - ap^{2}}{q - p}$ Attempt to obtain an equation in one variable x or y $y = \frac{aq^{2} - ap^{2}}{q - p}$ Attempt to isolate x or y $M1$ $y = a(p + q) \text{ or } ap + aq$ $x = apq$ A1: Either one correct simplified coordinates $(R(apq, ap + aq))$ (d) $pq = -1$ Answer only: Scores 2/2 if x coordinate of $R = -a$ $M1$ | | $\frac{\mathrm{d}y}{\mathrm{d}x} = a^{\frac{1}{2}}x^{-\frac{1}{2}} \text{ or } 2y\frac{\mathrm{d}y}{\mathrm{d}x} = 4a \text{ or } \frac{\mathrm{d}y}{\mathrm{d}x} = 2a.\frac{1}{2ap}$ | Differentiation is accurate. | A1 |
| (b) $qy - x = aq^2$ B1(c) $qy - aq^2 = py - ap^2$ Attempt to obtain an equation in one variable x or yM1 $y(q-p) = aq^2 - ap^2$ $y = \frac{aq^2 - ap^2}{q-p}$ Attempt to isolate x or yM1 $y = aq^2 - ap^2$ $q-p$ Attempt to isolate x or yM1 $y = aq^2 - ap^2$ $q-p$ Attempt to isolate x or yM1 $y = a(p+q) or ap + aq$ $x = apq$ A1: Either one correct simplified coordinate A1: Both correct simplified coordinatesA1,A1(d)' $apq' = -a$ Their x coordinate of $R = -a$ M1 $pq = -1$ Answer only: Scores 2/2 if x coordinate of R is apq otherwise 0/2.A1 | | $y - 2ap = \frac{1}{p}(x - ap^2)$ | or $y = (\text{their } m)x + c$ using $x = ap^2$ and $y = 2ap$ in an attempt to find c. Their m must be a function of p from | M1 |
| (b) $qy - x = aq^2$ B1(c) $qy - aq^2 = py - ap^2$ Attempt to obtain an equation in one variable x or yM1 $y(q-p) = aq^2 - ap^2$ $y = \frac{aq^2 - ap^2}{q - p}$ Attempt to isolate x or yM1 $y = a(p+q) or ap + aq$ $x = apq$ A1: Either one correct simplified coordinate A1: Both correct simplified coordinatesA1,A1(d)' $apq' = -a$ Their x coordinate of $R = -a$ M1 $pq = -1$ Answer only: Scores 2/2 if x coordinate of R is apq otherwise 0/2.A1 | | $py-x=ap^2 *$ | Correct completion to printed answer* | A1 cso |
| $qy - x - aq$ B1(c) $qy - aq^2 = py - ap^2$ Attempt to obtain an equation in one variable x or yM1 $y(q-p) = aq^2 - ap^2$ Attempt to isolate x or yM1 $y = \frac{aq^2 - ap^2}{q - p}$ Attempt to isolate x or yM1 $y = a(p+q)orap + aq$ $x = apq$ A1: Either one correct simplified coordinate A1: Both correct simplified coordinatesA1,A1(d)' $apq' = -a$ Their x coordinate of $R = -a$ M1 $pq = -1$ Answer only: Scores 2/2 if x coordinate of R is apq otherwise 0/2.A1 | | | | (4 |
| (c) $qy - aq^2 = py - ap^2$ Attempt to obtain an equation in one variable x or yM1 $y(q-p) = aq^2 - ap^2$ $y = \frac{aq^2 - ap^2}{q-p}$ Attempt to isolate x or yM1 $y = a(p+q) \text{ or } ap + aq$ $x = apq$ Attempt to isolate x or yM1 $(R(apq, ap + aq))$ A1: Either one correct simplified coordinate A1: Both correct simplified coordinatesA1,A1(d)'apq' = -aTheir x coordinate of $R = -a$ M1 $pq = -1$ Answer only: Scores 2/2 if x coordinate of R is apq otherwise 0/2.A1 | (b) | $qy - x = aq^2$ | | B1 |
| $\frac{qy - aq = py - ap}{y(q - p) = aq^2 - ap^2}$ $y = \frac{aq^2 - ap^2}{q - p}$ $y = a(p + q) or ap + aq$ $x = apq$ $(R(apq, ap + aq))$ $\frac{qy - aq^2 - ap^2}{q - p}$ $Attempt to isolate x or y$ $A1: Either one correct simplified coordinates$ $A1,A1$ $A1: Both correct simplified coordinates$ $(R(apq, ap + aq))$ (a) $\frac{qy - aq^2 - ap^2}{q - p}$ (a) $\frac{qy - aq^2 - ap^2}{q - p}$ $Attempt to isolate x or y$ $A1: Either one correct simplified coordinates$ $A1,A1$ $A1: Both correct simplified coordinates$ (a) $\frac{qy - aq^2 - ap^2}{q - p}$ (a) $A1: Either one correct simplified coordinates$ $A1,A1$ $A1: Both correct simplified coordinates$ $A1,A1$ $A1: A1: Both correct of R = -a$ $A1$ $A1: A1: A1: A1: A1: A1: A1: A1: A1: A1: $ | | | | (1 |
| $y = \frac{aq^2 - ap^2}{q - p}$ Attempt to isolate x or yM1 $y = a(p+q) \text{ or } ap + aq$ $x = apq$ A1: Either one correct simplified coordinate A1: Both correct simplified coordinatesA1,A1(R(apq, ap + aq))(a)(a)(a)(a)(a)(b)(a)(a)(c)(a)(a) <tr< td=""><td>(c)</td><td></td><td>· ·</td><td>M1</td></tr<> | (c) | | · · | M1 |
| y = a(p+q) or ap + aq $x = apq$ $(R(apq, ap + aq))$ (a) (a) (a) (a) (a) (a) (a) (a) (b) (a) (a) (b) (a) (b) (c) | | $y = \frac{aq^2 - ap^2}{ap^2}$ | Attempt to isolate <i>x</i> or <i>y</i> | M1 |
| (d)'apq' = -aTheir x coordinate of $R = -a$ M1 $pq = -1$ Answer only: Scores 2/2 if x coordinate of R is apq otherwise 0/2.A1 | | y = a(p+q) or ap + aq x = apq | coordinate | A1,A1 |
| (d)' $apq' = -a$ Their x coordinate of $R = -a$ M1 $pq = -1$ Answer only: Scores 2/2 if x coordinate of R is apq otherwise 0/2.A1 | | (R(apq, ap + aq)) | | |
| pq = -1 Answer only: Scores 2/2 if x coordinate of R is apq otherwise 0/2. (2) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4 | (d) | | | |
| pq = -1 coordinate of <i>R</i> is <i>apq</i> otherwise 0/2. (2) | | apq' = -a | Their <i>x</i> coordinate of $R = -a$ | M1 |
| | | pq = -1 | • | A1 |
| | | | | (2 |

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| Question Number | Scheme | Notes | Marks |
|--------------------|--|---|----------|
| 7 | $z_1 = 2 + 3i$ | $z_1, z_2 = 3 + 2i$ | |
| (a) | $z_1 + z_2 = 5 + 5i \implies z_1 + z_2 = \sqrt{5^2 + 5^2}$ | Adds z_1 and z_2 and correct use of Pythagoras. i under square root award M0. | M1 |
| | $\sqrt{50} \ (= 5\sqrt{2})$ | | A1 cao |
| | | | (2) |
| (b) | $\frac{z_1 z_3}{z_2} = \frac{(2+3i)(a+bi)}{3+2i}$ | Substitutes for z_1, z_2 and z_3 and multiplies | |
| | $=\frac{(2+3i)(a+bi)(3-2i)}{(3+2i)(3-2i)}$ | by $\frac{3-2i}{3-2i}$ | M1 |
| | (3+2i)(3-2i) = 13 | 13 seen. | B1 |
| | $\frac{z_1 z_3}{z_2} = \frac{(12a - 5b) + (5a + 12b)i}{13}$ | M1: Obtains a numerator with 2 real and 2 imaginary parts. A1: As stated or $\frac{(12a-5b)}{13} + \frac{(5a+12b)}{13}i$ ONLY. | dM1A1 |
| | | | (4) |
| (c) | 12a - 5b = 17 5a + 12b = -7 | Compares real and imaginary parts to obtain 2 equations which both involve <i>a</i> and <i>b</i> . Condone sign errors only. | M1 |
| | $\begin{array}{c} 60a - 25b = 85\\ 60a + 144b = -84 \end{array} \implies b = -1 \end{array}$ | Solves as far as $a = \text{ or } b =$ | dM1 |
| | <i>a</i> = 1, <i>b</i> = -1 | Both correct | A1 |
| | | Correct answers with no working award 3/3. | |
| | | | (3) |
| (d) | $\arg(w) = -\tan^{-1}\left(\frac{7}{17}\right)$ | Accept use of $\pm \tan^{-1}$ or $\pm \tan$. awrt ± 0.391 or ± 5.89 implies M1. | M1 |
| | =awrt - 0.391 or awrt 5.89 | | A1 |
| | | | (2) |
| | | | Total 11 |

| Question Number | Scheme | Notes | Marks |
|--------------------|---|--|---------|
| 8(a) | $\mathbf{A}^{2} = \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} = \begin{pmatrix} 44 & -14 \\ -28 & 9 \end{pmatrix}$ | M1:Attempt both \mathbf{A}^2 and $7\mathbf{A} + 2\mathbf{I}$ | |
| | $7\mathbf{A} + 2\mathbf{I} = \begin{pmatrix} 42 & -14 \\ -28 & 7 \end{pmatrix} + \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} = \begin{pmatrix} 44 & -14 \\ -28 & 9 \end{pmatrix}$ | A1: Both matrices correct | M1A1 |
| | $OR \mathbf{A}^2 - 7\mathbf{A} = \mathbf{A} (\mathbf{A} - 7\mathbf{I})$ | M1 for expression and attempt to substitute and multiply (2x2)(2x2)=2x2 | |
| | $\mathbf{A}(\mathbf{A} - 7\mathbf{I}) = \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} -1 & -2 \\ -4 & -6 \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} = 2\mathbf{I}$ | A1 cso | |
| | | | (2) |
| (b) | $\mathbf{A}^2 = 7\mathbf{A} + 2\mathbf{I} \Longrightarrow \mathbf{A} = 7\mathbf{I} + 2\mathbf{A}^{-1}$ | Require one correct line using accurate expressions involving A^{-1} and identity matrix to be clearly stated as I. | M1 |
| | $\mathbf{A}^{-1} = \frac{1}{2} \left(\mathbf{A} - 7\mathbf{I} \right)^*$ | | A1* cso |
| | Numerical approach award 0/2. | | |
| | | | (2) |
| (c) | $\mathbf{A}^{-1} = \frac{1}{2} \begin{pmatrix} -1 & -2 \\ -4 & -6 \end{pmatrix}$ | Correct inverse matrix or equivalent | B1 |
| | $\frac{1}{2} \begin{pmatrix} -1 & -2 \\ -4 & -6 \end{pmatrix} \begin{pmatrix} 2k+8 \\ -2k-5 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} -2k-8+4k+10 \\ -8k-32+12k+30 \end{pmatrix}$ | Matrix multiplication involving their inverse and k: (2x2)(2x1)=2x1. N.B. $\begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} 2k+8 \\ -2k-5 \end{pmatrix}$ is M0 | M1 |
| | $\binom{k+1}{2k-1} \text{ or } (k+1, 2k-1)$ Or: | (k+1) first A1, $(2k-1)$ second A1 | A1,A1 |
| | | | |
| | $ \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 2k+8 \\ -2k-5 \end{pmatrix} $ | Correct matrix equation. | B1 |
| | 6x - 2y = 2k + 8 -4x + y = -2k - 5 \Rightarrow x = or y = | Multiply out and attempt to solve simultaneous equations for <i>x</i> or <i>y</i> in terms of <i>k</i> . | M1 |
| | $\binom{k+1}{2k-1} \text{ or } (k+1, 2k-1)$ | (k+1) first A1, $(2k-1)$ second A1 | A1,A1 |
| | | | (4) |
| | | | Total 8 |

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| - | _ | | |
|---|---|---|---|
| 6 | 6 | 6 | 7 |

| Question Number | Scheme | Notes | Marks |
|--------------------|--|---|-----------------|
| 9(a) | $u_1 = 8$ given $n = 1 \Longrightarrow u_1 = 4^1 + 3(1) + 1 = 8$ (: true for $n = 1$) | $4^1 + 3(1) + 1 = 8$ seen | B1 |
| - | Assume true for $n = k$ so that $u_k = 4^k + 3k + 1$ | | |
| | $u_{k+1} = 4(4^k + 3k + 1) - 9k$ | Substitute u_k into u_{k+1} as $u_{k+1} = 4u_k - 9k$ | M1 |
| | $= 4^{k+1} + 12k + 4 - 9k = 4^{k+1} + 3k + 4$ | Expression of the form $4^{k+1} + ak + b$ | A1 |
| | $=4^{k+1}+3(k+1)+1$ | Correct completion to an expression in terms of $k + 1$ | A1 |
| | If true for $n = k$ then true for $n = k + 1$ and as true for $n = 1$ true for all n | Conclusion with all 4 underlined elements that can be seen anywhere in the solution; <i>n</i> defined incorrectly award A0. | A1 cso |
| (b) | Condone use of <i>n</i> here. | | (5) |
| | $lhs = \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}^{1} = \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}$ $rhs = \begin{pmatrix} 2(1)+1 & -4(1) \\ 1 & 1-2(1) \end{pmatrix} = \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}$ | Shows true for $m = 1$ | B1 |
| | Assume $\begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}^{k} = \begin{pmatrix} 2k+1 & -4k \\ k & 1-2k \end{pmatrix}$ $\begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}^{k+1} = \begin{pmatrix} 2k+1 & -4k \\ k & 1-2k \end{pmatrix} \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}$ | $ \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} 2k+1 & -4k \\ k & 1-2k \end{pmatrix} $ award M1 | M1 |
| - | $= \begin{pmatrix} 6k+3-4k & -8k-4+4k \\ 3k+1-2k & -4k-1+2k \end{pmatrix}$ | Or equivalent 2x2 matrix. $\begin{pmatrix} 6k+3-4k & -12k-4+8k \\ 2k+1-k & -4k-1+2k \end{pmatrix}$ award A1from above. | A1 |
| | $= \left(\begin{pmatrix} 2k+3 & -4k-4\\ k+1 & -2k-1 \end{pmatrix} \right)$ | | |
| | $= \begin{pmatrix} 2(k+1)+1 & -4(k+1) \\ k+1 & 1-2(k+1) \end{pmatrix}$ | Correct completion to a matrix in terms of $k + 1$ | A1 |
| | If <u>true for $m = k$</u> then <u>true for $m = k + 1$</u> and as <u>true</u> for $m = 1$ true for all <u>m</u> | Conclusion with all 4 underlined elements that can be seen anywhere in the solution; <i>m</i> defined incorrectly award A0. | A1 cso |
| | | | (5) Total 10 |

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