

Mark Scheme (Results) January 2010

GCE

Mechanics M1 (6677)



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January 2010 6677 Mechanics M1 Mark Scheme

Scheme	Marks	
(a) $I = 2 \times 12 - 2 \times 3 = 18 \text{ (N s)}$	M1 A1	(2)
(b) LM $2 \times 12 - 8m = 2 \times 3 + 4m$ Solving to $m = 1.5$	M1 A1 DM1 A1	(4) [6]
Alternative to (b) I = m(4-(-8)) = 18 Solving to $m = 1.5$	M1 A1 DM1 A1	(4)
(a) s First two line segments Third line segment 8, 75 8 0 75 t	B1 B1 B1	(3)
(b) $\frac{1}{2} \times 8 \times (T+75) = 500$	M1 A2 (1,0)	
Solving to $T = 50$	DM1 A1	(5) [8]
	(a) $I = 2 \times 12 - 2 \times 3 = 18$ (N s) (b) LM $2 \times 12 - 8m = 2 \times 3 + 4m$ Solving to $m = 1.5$ Alternative to (b) $I = m(4 - (-8)) = 18$ Solving to $m = 1.5$ (a) First two line segments Third line segment $8, 75$ (b) $\frac{1}{2} \times 8 \times (T + 75) = 500$	(a) $I = 2 \times 12 - 2 \times 3 = 18$ (N s) (b) LM $2 \times 12 - 8m = 2 \times 3 + 4m$ Solving to $m = 1.5$ Alternative to (b) I = m(4 - (-8)) = 18 Solving to $m = 1.5$ (a) $I = m(4 - (-8)) = 18$ Solving to $m = 1.5$ (a) $I = m(4 - (-8)) = 18$ Solving to $m = 1.5$ (b) $I = m(4 - (-8)) = 18$ Solving to $m = 1.5$ (c) $I = m(4 - (-8)) = 18$ Solving to $m = 1.5$ (b) $I = m(4 - (-8)) = 18$ Solving to $m = 1.5$ (c) $I = m(4 - (-8)) = 18$ (c) $I = m(4 $

Question Number	Scheme	Marks
Q3.	$\begin{array}{c c} A & 30^{\circ} & 60^{\circ} & B \\ \hline 20 & T & T \\ C & mg \\ \end{array}$	
	(a) $R(\rightarrow)$ $20\cos 30^\circ = T\cos 60^\circ$ $T = 20\sqrt{3}, 34.6, 34.64,$	M1 A2 (1,0) A1 (4)
	(b) $R(\uparrow) \qquad mg = 20\sin 30^\circ + T\sin 60^\circ$ $m = \frac{40}{g} (\approx 4.1), 4.08$	M1 A2 (1,0) A1 (4) [8]
Q4.	(a) X A 1.8 m 1.5 m $W1.5 m$ 20	
	M (A) $W \times 1.5 + 20 \times 3 = Y \times 1.8$ $Y = \frac{5}{6}W + \frac{100}{3}$ * cso	M1 A2 (1, 0) A1 (4)
	(b) \uparrow $X + Y = W + 20$ or equivalent $X = \frac{1}{6}W - \frac{40}{3}$	M1 A1 A1 (3)
	(c) $\frac{5}{6}W + \frac{100}{3} = 8\left(\frac{1}{6}W - \frac{40}{3}\right)$ $W = 280$	M1 A1 ft A1 (3)
	Alternative to (b) M(C) $X \times 1.8 + 20 \times 1.2 = W \times 0.3$ $X = \frac{1}{6}W - \frac{40}{3}$	[10] M1 A1 A1

Question Number	Scheme	Marks
Q5.	(a) $s = ut + \frac{1}{2}at^{2} \implies 2.7 = \frac{1}{2}a \times 9$ $a = 0.6 (m s^{-2})$	M1 A1 A1 (3)
	(b)	
	$R = 0.8g \cos 30^{\circ} (\approx 6.79)$ Use of $F = \mu R$ $0.8g \sin 30^{\circ} - \mu R = 0.8 \times a$ $(0.8g \sin 30^{\circ} - \mu 0.8g \cos 30^{\circ} = 0.8 \times 0.6)$	B1 B1 M1 A1
	$\mu \approx 0.51$ accept 0.507	A1 (5)
	(c) $X = 0.8g$ 30°	
	$\uparrow \qquad R\cos 30^\circ = \mu R\cos 60^\circ + 0.8g$ $(R \approx 12.8)$	M1 A2 (1,0)
	$ \rightarrow X = R \sin 30^\circ + \mu R \sin 60^\circ $ Solving for X, X \approx 12 accept 12.0	M1 A1 DM1 A1 (7) [15]
	Alternative to (c)	
	$ℝ = X \sin 30^\circ + 0.8 \times 9.8 \sin 60^\circ$ $μR + 0.8g \cos 60^\circ = X \cos 30^\circ$	M1 A2 (1,0) M1 A1
	$X = \frac{\mu 0.8g \sin 60^\circ + 0.8g \cos 60^\circ}{\cos 30^\circ - \mu \sin 30^\circ}$ Solving for X, $X \approx 12$ accept 12.0	DM1 A1 (7)

Question Number	Scheme	Marks	
Q6.	(a) N2L A: $5mg - T = 5m \times \frac{1}{4}g$	M1 A1	
	$T = \frac{15}{4}mg \bigstar \qquad $	A1	(3)
	(b) N2L B: $T - kmg = km \times \frac{1}{4}g$	M1 A1	
	<i>k</i> = 3	A1	(3)
	(c) The tensions in the two parts of the string are the same	B1	(1)
	(d) Distance of A above ground $s_1 = \frac{1}{2} \times \frac{1}{4} g \times 1.2^2 = 0.18g (\approx 1.764)$	M1 A1	
	Speed on reaching ground $v = \frac{1}{4}g \times 1.2 = 0.3g (\approx 2.94)$	M1 A1	
	For <i>B</i> under gravity $(0.3g)^2 = 2gs_2 \implies s_2 = \frac{(0.3)^2}{2}g (\approx 0.441)$	M1 A1	
	$S = 2s_1 + s_2 = 3.969 \approx 4.0$ (m)	A1	(7) [14]

Scheme	Mark	S
(a) $\mathbf{v} = \frac{21\mathbf{i} + 10\mathbf{j} - (9\mathbf{i} - 6\mathbf{j})}{2\mathbf{i} + 4\mathbf{i}}$	M1 A1	
speed is $\sqrt{(3^2 + 4^2)} = 5 (\text{km h}^{-1})$	M1 A1	(4)
(b) $\tan \theta = \frac{3}{4} (\Rightarrow \theta \approx 36.9^{\circ})$	M1	
bearing is 37, 36.9, 36.87,	A1	(2)
(c) $\mathbf{s} = 9\mathbf{i} - 6\mathbf{j} + t(3\mathbf{i} + 4\mathbf{j})$ = $(3t + 9)\mathbf{i} + (4t - 6)\mathbf{j} \mathbf{*}$ cso	M1 A1	(2)
(d) Position vector of S relative to L is $(3T+9)\mathbf{i} + (4T-6)\mathbf{j} - (18\mathbf{i}+6\mathbf{j}) = (3T-9)\mathbf{i} + (4T-12)\mathbf{j}$ $(3T-9)^2 + (4T-12)^2 = 100$ $25T^2 - 150T + 125 = 0$ or equivalent $(T^2 - 6T + 5 = 0)$ T = 1, 5	M1 A1 M1 DM1 A1 A1	(6) [14]
	(a) $\mathbf{v} = \frac{2\mathbf{l}\mathbf{i} + 10\mathbf{j} - (9\mathbf{i} - 6\mathbf{j})}{4} = 3\mathbf{i} + 4\mathbf{j}$ speed is $\sqrt{3^2 + 4^2} = 5$ (km h ⁻¹) (b) $\tan \theta = \frac{3}{4}$ ($\Rightarrow \theta \approx 36.9^\circ$) bearing is 37, 36.9, 36.87, (c) $\mathbf{s} = 9\mathbf{i} - 6\mathbf{j} + t(3\mathbf{i} + 4\mathbf{j})$ $= (3t + 9)\mathbf{i} + (4t - 6)\mathbf{j}$ * cso (d) Position vector of <i>S</i> relative to <i>L</i> is $(3T + 9)\mathbf{i} + (4T - 6)\mathbf{j} - (18\mathbf{i} + 6\mathbf{j}) = (3T - 9)\mathbf{i} + (4T - 12)\mathbf{j}$ $(3T - 9)^2 + (4T - 12)^2 = 100$ $25T^2 - 150T + 125 = 0$ or equivalent $(T^2 - 6T + 5 = 0)$	(a) $\mathbf{v} = \frac{21\mathbf{i} + 10\mathbf{j} - (9\mathbf{i} - 6\mathbf{j})}{4} = 3\mathbf{i} + 4\mathbf{j}$ M1 A1 M1 A1 (b) $\tan \theta = \frac{3}{4} (\Rightarrow \theta \approx 36.9^{\circ})$ M1 (c) $\mathbf{s} = 9\mathbf{i} - 6\mathbf{j} + t(3\mathbf{i} + 4\mathbf{j})$ $= (3t + 9)\mathbf{i} + (4t - 6)\mathbf{j} \\ (3T + 9)\mathbf{i} + (4T - 6)\mathbf{j} - (18\mathbf{i} + 6\mathbf{j}) = (3T - 9)\mathbf{i} + (4T - 12)\mathbf{j}$ M1 A1 (d) Position vector of S relative to L is $(3T + 9)\mathbf{i} + (4T - 6)\mathbf{j} - (18\mathbf{i} + 6\mathbf{j}) = (3T - 9)\mathbf{i} + (4T - 12)\mathbf{j}$ M1 A1 $(3T - 9)^{2} + (4T - 12)^{2} = 100$ $25T^{2} - 150T + 125 = 0$ or equivalent $(T^{2} - 6T + 5 = 0)$ M1 A1

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