Past Paper

This resource was created and owned by Pearson Edexcel

WFM01

Surname	Other nan	nes
Pearson Edexcel International Advanced Level	Centre Number	Candidate Number
Further Pu Mathema		
Advanced/Advance	d Subsidiary	
Thursday 14 May 2015 –		Paper Reference WFM01/01

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

#### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided - there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

#### Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each guestion.

#### **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶



■ Past Paper

This resource was created and owned by Pearson Edexcel

WFM01

Leave blank

1.	Given	that
1.	OIVCII	uiai

$$2z^3 - 5z^2 + 7z - 6 \equiv (2z - 3)(z^2 + az + b)$$

where a and b are real constants,

(a) find the value of a and the value of b.

**(2)** 

(b) Given that z is a complex number, find the three exact roots of the equation

$$2z^3 - 5z^2 + 7z - 6 = 0$$

(3)


_			
Sun	nmer	201	5

This resource was created and owned by Pearson Edexcei	V\
d	
u	
	Q
	d d l l l l l l l l l l l l l l l l l l

■ Past Paper

This resource was created and owned by Pearson Edexcel

WFM01

	7
Leave	
Louve	
hlank	

		n	n
2.	Use the standard results for	$\sum r$ and for	$\sum r^2$ to show that
		r=1	r=1

$$\sum_{r=1}^{n} (3r - 2)^{2} = \frac{n}{2} (an^{2} + bn + c)$$

where a, b and c are integers to be found.

1	_		
1	◂		
ı	J	,	

e.	ım	<u></u>	or	2	Λ4	E
.51	ım	m	er	_	UT	- 7

Question 2 continued	L
Ducetion 2 continued	h
Jungtion 2 continued	1 6
Jueshon 2 commucu	
	—
	Q

■ Past Paper

This resource was created and owned by Pearson Edexcel

NFM01

	Leave
	blank
It is given that $\alpha$ and $\beta$ are roots of the equation	

3. It is given that  $\alpha$  and  $\beta$  are roots of the equation

$$2x^2 - 7x + 4 = 0$$

(a) Find the exact value of  $\alpha^2 + \beta^2$ 

**(3)** 

(b) Find a quadratic equation which has roots  $\frac{\alpha}{\beta}$  and  $\frac{\beta}{\alpha}$ , giving your answer in the form  $ax^2 + bx + c = 0$ , where a, b and c are integers.

(3)

Su	 -	~=	2	$\Lambda A$	
311	ш	er	_	W I	-

Paper	This resource was created and owned by Pearson Edexcel	Wi
		L b
Question 3 continue	ed	
		Q.
	(Total 6 ma	

■ Past Paper

This resource was created and owned by Pearson Edexcel

WFM01

blank

4.

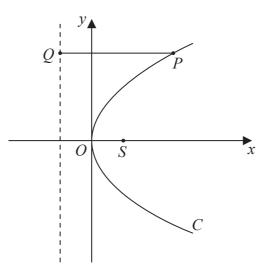


Figure 1

Figure 1 shows a sketch of the parabola C with equation  $y^2 = 4ax$ , where a is a positive constant. The point S is the focus of C and the point Q lies on the directrix of C. The point P lies on C where y > 0 and the line segment QP is parallel to the x-axis.

Given that the length of *PS* is 13

(a) write down the length of PQ.

**(1)** 

Given that the point P has x coordinate 9

find

(b) the value of a,

**(2)** 

(c) the area of triangle *PSQ*.

**(3)** 

e.	ım	<u></u>	or	2	Λ4	E
.51	ım	m	er	_	UT	- 7

Paper	This resource was created and owned by Pearson Edexcel	WF
		Le
<b>Question 4 continue</b>	d	bla
Question i continue	•	
		—
		Q4
	(Total 6 ma	,

■ Past Paper

This resource was created and owned by Pearson Edexcel

WFM01 Leave

blank

5. In the interval 2 < x < 3, the equation

$$6 - x^2 \cos\left(\frac{x}{5}\right) = 0$$
, where x is measured in radians

has exactly one root  $\alpha$ .

(a) Starting with the interval [2, 3], use interval bisection twice to find an interval of width 0.25 which contains  $\alpha$ .

**(4)** 

(b) Use linear interpolation once on the interval [2, 3] to find an approximation to  $\alpha$ . Give your answer to 2 decimal places.

**(3)** 

_			
Sun	nmer	201	5

# **www.mystudybro.com**This resource was created and owned by Pearson Edexcel

**Mathematics F1** 

ast Paper	This resource was created and owned by Pearson Edexcel	WFM0
		Leave blank
Question 5 contin	ued	biank
<b>C</b>		
		Q5
	(Total 7 ma	arks)
	(=5002 / 200	

**(6)** 

■ Past Paper

This resource was created and owned by Pearson Edexcel

Leave blank

**6.** The rectangular hyperbola, H, has cartesian equation

$$xy = 36$$

The three points  $P\left(6p, \frac{6}{p}\right)$ ,  $Q\left(6q, \frac{6}{q}\right)$  and  $R\left(6r, \frac{6}{r}\right)$ , where p, q and r are distinct, non-zero values, lie on the hyperbola H.

(a) Show that an equation of the line PQ is

$$pqy + x = 6(p+q) \tag{4}$$

Given that PR is perpendicular to QR,

(b) show that the normal to the curve H at the point R is parallel to the line PQ.

Cun	nmer	204	_
Sun	nmer	<b>Z</b> U1	Э

nmer 2015	This resource was created and owned by Pearson Edexcel	Mathematics F
Paper	This resource was created and owned by Pearson Edexcel	WFM
		Leav
Overtion ( continue		blan
<b>Question 6 continue</b>	u	



Sı				00	١.	
.51	m	m	er	71	ľ	-0

Past Paper	This resource was created and owned by Pearson Edexcel	WFM0 <sup>2</sup>
		Leave blank
Question 6 co	ontinued	

Sum		204	_
Sum	mer	<b>Z</b> U1	Э

apei	This resource was created and owned by Fearson Edexcer	VVFIVIO
		Leave
		blank
Question 6 continued	1	
		Q6
	(Total 10 marks)	

Past Paper

This resource was created and owned by Pearson Edexcel

WFM01 Leave

blank

7.

z = -3k - 2ki, where k is a real, positive constant.

(a) Find the modulus and the argument of z, giving the argument in radians to 2 decimal places and giving the modulus as an exact answer in terms of k.

**(3)** 

- (b) Express in the form a + ib, where a and b are real and are given in terms of k where necessary,
  - (i)  $\frac{4}{z+3k}$
  - (ii)  $z^2$

**(5)** 

(c) Given that k = 1, plot the points A, B, C and D representing z,  $z^*$ ,  $\frac{4}{z + 3k}$  and  $z^2$  respectively on a single Argand diagram.

**(3)** 

16

Cun	nmer	204	_
Sun	nmer	<b>Z</b> U1	Э

Paper	This resource was created and owned by Pearson Edexcel	WFM01
		Leave
Question 7 continued	1	blank
Question / continue		
		1

Q.	ım	m	۵r	20	۱1	ľ
- 31	ши	m	er	ZL	, ,	-

summer 2015 ast Paper	www.mystudybro.com This resource was created and owned by Pearson Edexcel	Mathematics F <sup>2</sup> WFM0
αοι Γαμεί	This resource was created and owned by Fedison Edexcel	Leave
Question 7 contin	word	blank
Question 7 contin	ueu	

Sum		204	_
Sum	mer	<b>Z</b> U1	Э

apei	This resource was created and owned by Fearson Edexcei	VVI
		Le
		bl
Question 7 continued		
	(Total 11 marks)	

Past Paper

This resource was created and owned by Pearson Edexcel

VFM01 Leave

blank

8.

$$\mathbf{P} = \begin{pmatrix} 3a & -4a \\ 4a & 3a \end{pmatrix}, \text{ where } a \text{ is a constant and } a > 0$$

(a) Find the matrix  $P^{-1}$  in terms of a.

**(3)** 

The matrix  ${\bf P}$  represents the transformation U which transforms a triangle  $T_1$  onto the triangle  $T_2$ .

The triangle  $T_2$  has vertices at the points (-3a, -4a), (6a, 8a), and (-20a, 15a).

(b) Find the coordinates of the vertices of  $T_1$ 

**(3)** 

(c) Hence, or otherwise, find the area of triangle  $T_2$  in terms of a.

**(3)** 

The transformation V, represented by the 2  $\times$  2 matrix  $\mathbf{Q}$ , is a rotation through an angle  $\alpha$  clockwise about the origin, where  $\tan \alpha = \frac{4}{3}$  and  $0 < \alpha < \frac{\pi}{2}$ 

(d) Write down the matrix Q, giving each element as an exact value.

**(2)** 

The transformation U followed by the transformation V is the transformation W. The matrix  $\mathbf{R}$  represents the transformation W.

(e) Find the matrix  $\mathbf{R}$ .

**(2)** 

Sum	mar	204	E
Sum	mer	<b>Z</b> U1	Э

<b>nmer 2015</b> Paper	www.mystudybro.com This resource was created and owned by Pearson Edexcel	Mathematics F
•	,	Leave
Question 8 continued		blank

Q.	ım	m	۵r	20	۱1	ľ
- 31	ши	m	er	ZL	, ,	-

<b>summer 2015</b> ast Paper	www.mystudybro.com This resource was created and owned by Pearson Edexcel	Mathematics F <sup>2</sup> WFM0
αοι Γαμ <del>ε</del> ι	This resource was created and owned by Fearson Edexcer	Leave
Question 8 continu	and	blank
Question o continu	leu	

e.	ım	<u></u>	or	2	Λ4	E
.51	ım	m	er	_	UT	- 7

apei	This resource was created and owned by Fearson Edexcer	VVFIVI
		Leav
	•	blan
Question 8 continued	1	
		Q
	(Total 13 marks)	

**Mathematics F1** 

■ Past Paper

This resource was created and owned by Pearson Edexcel

WFM01

Leave blank

**9.** (i) Prove by induction that, for  $n \in \mathbb{Z}^+$ ,

$$\sum_{r=1}^{n} r^{2}(2r-1) = \frac{1}{6}n(n+1)(3n^{2}+n-1)$$

**(6)** 

(ii) Prove by induction that, for  $n \in \mathbb{Z}^+$ ,

$$\begin{pmatrix} 7 & -12 \\ 3 & -5 \end{pmatrix}^n = \begin{pmatrix} 6n+1 & -12n \\ 3n & 1-6n \end{pmatrix}$$

**(6)** 

Cun	nmer	204	_
Sun	nmer	<b>Z</b> U1	Э

Paper	This resource was created and owned by Pearson Edexcel	WFM0
		Leave blank
Question 9 continued		



C.	ım			20	1	
- 51	JM	m	er	ΖU	) [	:

st Paper	This resource was created and owned by Pearson Edexcel	WFM0
Question 9 continu	rod	Leave blank
Question 9 continu	leu	

C		204	E
Sum	mer	<b>Z</b> U1	Э

Paper	This resource was created and owned by Pearson Edexcel	WFM0
		Leave blank
Question 9 continued		

_					_	
c.	ım	-	^ r	വ	14	
.71	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		eı		, ,	Ξ

# **www.mystudybro.com**This resource was created and owned by Pearson Edexcel

Past Paper	This resource was created and owned by Pearson Edexcel	WFM01
		Leave blank
Question 9 co	ontinued	Ulalik
_		
		_
		_
		_
		_
		_
		_
		_
		_
		_
		_
		_
		_
		Q9
	(Total 12 mark	(s)
	TOTAL FOR PAPER: 75 MARI	KS
	END	
	444	