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Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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# Further Pure Mathematics F1

## Advanced/Advanced Subsidiary

Friday 20 May 2016 – Morning

**Time: 1 hour 30 minutes**

Paper Reference

**WFM01/01****You must have:**

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

### Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1. Use the standard results for  $\sum_{r=1}^n r$  and for  $\sum_{r=1}^n r^3$  to show that, for all positive integers  $n$ ,

$$\sum_{r=1}^n r(r^2 - 3) = \frac{n}{4}(n+a)(n+b)(n+c)$$

where  $a$ ,  $b$  and  $c$  are integers to be found.

(4)

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Question 1 continued

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(Total 4 marks)

Q1

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- Points  $A$  and  $B$  lie on the parabola  $P$ . The line  $AB$  is parallel to the directrix of  $P$  and cuts the  $x$ -axis at the midpoint of  $OS$ , where  $O$  is the origin.

- (b) Find the exact area of triangle  $ABS$ . (4)

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Question 2 continued

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3.

$$f(x) = x^2 + \frac{3}{x} - 1, \quad x < 0$$

The only real root,  $\alpha$ , of the equation  $f(x) = 0$  lies in the interval  $[-2, -1]$ .

- (a) Taking  $-1.5$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x)$  to find a second approximation to  $\alpha$ , giving your answer to 2 decimal places.

(5)

- (b) Show that your answer to part (a) gives  $\alpha$  correct to 2 decimal places.

(2)

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Question 3 continued

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(Total 7 marks)

Q3

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4. Given that

$$\mathbf{A} = \begin{pmatrix} k & 3 \\ -1 & k+2 \end{pmatrix}, \text{ where } k \text{ is a constant}$$

(a) show that  $\det(\mathbf{A}) > 0$  for all real values of  $k$ ,

(3)

(b) find  $\mathbf{A}^{-1}$  in terms of  $k$ .

(2)

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Question 4 continued

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Q4

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5.

$$2z + z^* = \frac{3 + 4i}{7 + i}$$

Find  $z$ , giving your answer in the form  $a + bi$ , where  $a$  and  $b$  are real constants. You must show all your working.

(5)

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Question 5 continued

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(Total 5 marks)

Q5

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- (c) Find the coordinates of  $B$ . **(4)**

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Question 6 continued

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Question 6 continued

Q6

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$$\mathbf{P} = \begin{pmatrix} \frac{5}{13} & -\frac{12}{13} \\ \frac{12}{13} & \frac{5}{13} \end{pmatrix}$$

- The transformation  $V$ , represented by the  $2 \times 2$  matrix  $\mathbf{Q}$ , is a reflection in the line with equation  $y = x$

- Given that the transformation  $V$  followed by the transformation  $U$  is the transformation  $T$ , which is represented by the matrix  $\mathbf{R}$ ,

- (d) Show that there is a value of  $k$  for which the transformation  $T$  maps each point on the straight line  $y = kx$  onto itself, and state the value of  $k$ . (4)



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Question 7 continued

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Question 7 continued

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Question 7 continued

Q7

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$$f(z) = z^4 + 6z^3 + 76z^2 + az + b$$

Given that  $-3 + 8i$  is a complex root of the equation  $f(z) = 0$

- (a) write down another complex root of this equation. (1)
- (b) Hence, or otherwise, find the other roots of the equation  $f(z) = 0$  (6)
- (c) Show on a single Argand diagram all four roots of the equation  $f(z) = 0$  (2)

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Question 8 continued

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Question 8 continued

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Question 9 continued

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Question 9 continued

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(Total 9 marks)

Q9



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10. (i) A sequence of positive numbers is defined by

$$u_1 = 5$$

$$u_{n+1} = 3u_n + 2, \quad n \geq 1$$

Prove by induction that, for  $n \in \mathbb{Z}^+$ ,

$$u_n = 2 \times (3)^n - 1 \quad (5)$$

(ii) Prove by induction that, for  $n \in \mathbb{Z}^+$ ,

$$\sum_{r=1}^n \frac{4r}{3^r} = 3 - \frac{(3+2n)}{3^n} \quad (6)$$

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Question 10 continued

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Question 10 continued

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**(Total 11 marks)**

**Q10**

**TOTAL FOR PAPER: 75 MARKS**

**END**

