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Other names

Pearson Edexcel
International
Advanced Level

Centre Number

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Candidate Number

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Further Pure Mathematics F1

Advanced/Advanced Subsidiary

Monday 14 May 2018 – Afternoon

Time: 1 hour 30 minutes

Paper Reference

WFM01/01**You must have:**

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided – *there may be more space than you need*.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question*.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1. Use the standard results for $\sum_{r=1}^n r$ and for $\sum_{r=1}^n r^2$ to show that, for all positive integers n ,

$$\sum_{r=1}^n r(r+3) = \frac{n}{a}(n+1)(n+b)$$

where a and b are integers to be found.

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Question 1 continued

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Q1

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- (a) Write down the matrix \mathbf{P} , giving the exact numerical value of each element.

(1)

$$\mathbf{Q} = \begin{pmatrix} k\sqrt{2} & 0 \\ 0 & k\sqrt{2} \end{pmatrix}, \text{ where } k \text{ is a constant and } k > 0$$

- (b) Describe fully the single geometrical transformation represented by the matrix \mathbf{Q} .

(2)

The combined transformation represented by the matrix \mathbf{PQ} transforms the rhombus R_1 onto the rhombus R_3 .

The area of the rhombus R_1 is 6 and the area of the rhombus R_7 is 147

- (c) Find the value of the constant k .

(4)

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Question 2 continued

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A Cartesian coordinate system with x and y axes. The origin is labeled O . A parabola, labeled C , opens to the right with its vertex at O . The focus of the parabola is marked as point S on the positive x-axis. A vertical dashed line is drawn to the left of the y-axis, passing through a point Q on the y-axis. A point P is located on the upper branch of the parabola C .

Figure 1

(a) Find the coordinates of the point S . (1)

(b) State the distance SP . (1)

(c) find the exact coordinates of P .

(3)

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Question 3 continued

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Q3

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4.

$$\mathbf{A} = \begin{pmatrix} 2p & 3q \\ 3p & 5q \end{pmatrix}$$

where p and q are non-zero real constants.

(a) Find \mathbf{A}^{-1} in terms of p and q .

(3)

Given $\mathbf{XA} = \mathbf{B}$, where

$$\mathbf{B} = \begin{pmatrix} p & q \\ 6p & 11q \\ 5p & 8q \end{pmatrix}$$

(b) find the matrix \mathbf{X} , giving your answer in its simplest form.

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Question 4 continued

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(Total 7 marks)

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$$z^4 - 6z^3 + 34z^2 - 54z + 225 \equiv (z^2 + 9)(z^2 + az + b)$$

(a) find the value of a and the value of b .

(2)

(b) Hence find the exact roots of the equation

$$z^4 - 6z^3 + 34z^2 - 54z + 225 = 0$$

(4)

(c) Show your roots on a single Argand diagram.

(2)

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Question 5 continued

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Q5

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$$f(x) = \frac{2(x^3 + 3)}{\sqrt{x}} - 9, \quad x > 0$$

(5)

(4)

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Question 6 continued

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Question 6 continued

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Q6



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7. It is given that α and β are roots of the equation $5x^2 - 4x + 3 = 0$

Without solving the quadratic equation,

(a) find the exact value of $\frac{1}{\alpha^2} + \frac{1}{\beta^2}$ (5)

(b) find a quadratic equation which has roots $\frac{3}{\alpha^2}$ and $\frac{3}{\beta^2}$

giving your answer in the form $ax^2 + bx + c = 0$, where a , b and c are integers to be found.

(4)

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8. Prove by induction that, for $n \in \mathbb{Z}^+$

$$\begin{pmatrix} a & 0 \\ 1 & b \end{pmatrix}^n = \begin{pmatrix} a^n & 0 \\ \frac{a^n - b^n}{a - b} & b^n \end{pmatrix}$$

where a and b are constants and $a \neq b$.

(5)

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Question 8 continued

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$$\frac{z - ki}{z + 3i} = i, \text{ where } k \text{ is a positive real constant}$$

(b) Using the printed answer in part (a),

(i) find an exact simplified value for the modulus of z when $k = 4$

(4)



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Question 9 continued

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- (a) Show, by using calculus, that the normal to H at the point P has equation

$$y = p^2x + \frac{12}{p} - 12p^3 \quad (5)$$

(b) find the coordinates of Q and the coordinates of R , giving your answers in terms of p . (3)

- (c) Given also that the area of triangle OQR is 512, find the possible values of p . (5)

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Q10

TOTAL FOR PAPER: 75 MARKS

END

