

Mark Scheme (Results)

January 2015

Pearson Edexcel International A Level in Further Pure Mathematics F1 (WFM01/01)

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Mathematics F1

Past Paper (Mark Scheme)

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WFM01

General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL IAL MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- · sf significant figures
- * The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark

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| Question Number | Scheme | Notes | Marks |
|--------------------|---|--|-------------|
| 1. | $f(x) = x^4 - x^3 - 9x^2 + 29x - 60$ | | |
| | 1 – 2i is also a root | Seen anywhere | B1 |
| | $x^2 - 2x + 5$ | M1: Attempt to expand $(x-(1+2i))(x-(1-2i))$ or any valid method to establish the quadratic factor A1: x^2-2x+5 | M1A1 |
| | $f(x) = (x^2 - 2x + 5)(x^2 + x - 12)$ | M1: Attempt other quadratic factor A1: $x^2 + x - 12$ | M1A1 |
| | $x^{2} + x - 12 = (x + 4)(x - 3) \Rightarrow x =$ | Attempt to solve their other quadratic factor. | M1 |
| | x = -4 and x = 3 | Both values correct | A1 |
| | | | (7) Total 7 |
| | Altornotivo usir | ng Factor Theorem | Total / |
| | f(3) = or $f(-4) =$ | M1: Attempts f(3) or f(-4) | M1 |
| | f(3) = 0 or $f(-4) = 0$ | A1: Shows or states $f(3) = 0$ or $f(-4) = 0$ | A1 |
| | f(3) = and $f(-4) =$ | M1: Attempts $f(3)$ and $f(-4)$ or $f(3)$ and $g(-4)$ where $g(x) = f(x)/(x-3)$ or $f(-4)$ and $h(3)$ where $h(x) = f(x)/(x+4)$ | M1 |
| | f(3) = 0 and $f(-4) = 0$ | A1: Shows or states $f(3) = 0$ and $f(-4) = 0$ or shows or states $f(3) = 0$ and $g(-4) = 0$ where $g(x) = f(x)/(x - 3)$ or shows or states $f(-4) = 0$ and $h(3) = 0$ where $h(x) = f(x)/(x + 4)$ | A1 |
| | NB $g(x) = x^3 + 2x^2 - 3x +$ | 20, $h(x) = x^3 - 5x^2 + 11x - 15$ | |
| | x = 3 or x = -4 One of $x = -4$ | 3 or x = -4 clearly stated as a root | M1 |
| | x = 3 and $x = -4$ | Both $x = 3$ and $x = -4$ clearly stated as roots | A1 |
| | x=1-2i | | B1 |

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| Question Number | Scheme | Notes | Marks |
|--------------------|---|--|---------|
| 2 | $f(x) = x^3 - 3x^2 + \frac{1}{2\sqrt{x^5}} + 2$ | | |
| (a) | f(2) = and $f(3) =$ | Attempts both f(2) and f(3) | M1 |
| | f(2) = -1.9116, $f(3) = 2.032Sign change (and f(x) is continuous) therefore a root \alpha exists between x = 2 and x = 3$ | Both values correct: $f(2) = -1.9116$ (awrt -1.9), and $f(3) = 2.032$ (awrt 2.0 or e.g. $2 + \frac{\sqrt{3}}{54}$), sign change (or equivalent) and conclusion | A1 |
| | | | (2) |
| (b) | $f'(x) = 3x^2 - 6x - \frac{5}{4}x^{-3.5}$ | M1: $x^n \to x^{n-1}$ A1: $3x^2 - 6x$ A1: $-\frac{5}{4}x^{-3.5}$ or equivalent un-simplified and no other terms (+ c loses this mark) | M1A1A1 |
| | $\alpha = 3 - \frac{2.032075015}{8.973270821}$ | Correct attempt at Newton-Raphson using their values of $f(3)$ and $f'(3)$. | M1 |
| | $\alpha = 2.774$ | Cao (Ignore any subsequent applications) | A1 |
| | Correct derivative followed by correct answer with <u>no</u> works | * / | |
| | Correct answer with <u>no</u> work | ing scores <u>no</u> marks in (D) | (5) |
| | NB if the answer is incorrect it must be clear | that both $f(3)$ and $f'(3)$ are being used in | (3) |
| | the Newton-Raphson process. So that just 3 | $-\frac{f(3)}{f'(3)}$ with an incorrect answer and no | |
| | other evidence | scores M0. | |
| | | | |
| | | | Total 7 |

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|----------------------------------|---|--|----------------|
| Past Paper Question Number | (Mark Scheme) This resource was created a Scheme | and owned by Pearson Edexcel Notes | WFM01 Marks |
| 3 | $(z-2i)(z^*-$ | -2i) = 21-12i | |
| | $z^* = x - iy$ | | B1 |
| | $(x+iy-2i)(x-iy-2i) = \dots$ | Substitutes for <i>z</i> and their <i>z</i> * and attempts to expand | M1 |
| | $= x^{2} - x(y+2)i + x(y-2)i + y^{2} - 4$ | | |
| | $=x^2+y^2-4-4xi$ | | |
| | $x^{2} + y^{2} - 4 = 21$ and $4x = 12$ | Compares real and imaginary parts (allow sign errors only) | M1 |
| | $4x = 12 \Rightarrow x = \dots$ | Solves real and imaginary parts to obtain at least one value of <i>x</i> or <i>y</i> | M1 |
| | $x = 3, \ y = \pm 4$ | $x = 3 \cos 0$ $y = \pm 4 \cos 0$ | A1, A1 |
| | | | (6) Total 6 |
| Way 2 | (z-2i)(z*-2i) = zz*-2i(z+z*)-4 | Attempt to expand | M1 |
| | =(x+iy)(x-iy)-2i(x+iy+x-iy)-4 | $z^* = x - iy$ (may be implied) | B1 |
| | $=x^2 + y^2 - 4xi - 4$ | | |
| | $x^{2} + y^{2} - 4 = 21$ and $4x = 12$ | Compares real and imaginary parts (allow sign errors only) | M1 |
| | $4x = 12 \Rightarrow x = \dots$ | Solves real and imaginary parts to obtain at least one value of x or y | M1 |
| | $x = 3, \ y = \pm 4$ | $x = 3 \cos 0$ $y = \pm 4 \cos 0$ | A1, A1 |
| | | | Total 6 |
| Way 2 | (2;)(* 2;) * 2;(*) 4 | | |
| Way 3 | (z-2i)(z*-2i) = zz*-2i(z+z*)-4 | Attempt to expand | M1 |
| | zz*-2i(z+z*)-4=21-12i | Compares real and imaginary parts | |
| | zz*-4 = 21, 2(z+z*) = 12 | (allow sign errors only) | M1 |
| | $z^{2}-6z+25=0\left(\operatorname{or}\left(z^{*}\right)^{2}-6z^{*}+25=0\right)$ | Correct quadratic | B1 |
| | $z^{2} - 6z + 25 = 0 \left(\text{or} \left(z^{*} \right)^{2} - 6z^{*} + 25 = 0 \right)$ $\Rightarrow z = \dots \text{ or } z^{*} = \dots$ | Solves to obtain at least one value of z or z^* | M1 |
| | $z = 3, \pm 4i$ | x = 3 cso | A 1 A 1 |
| | Z − J, ±41 | $y = \pm 4$ cso | A1, A1 |
| | | | Total 6 |

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| Question Number | Scheme | Notes | Marks |
|--------------------|--|---|-----------------|
| 4(a) | $y^{2} = 12x \Rightarrow y = \sqrt{12}x^{\frac{1}{2}} \Rightarrow \frac{dy}{dx} = \frac{1}{2}\sqrt{12}x^{-\frac{1}{2}}$ $y^{2} = 12x \Rightarrow 2y\frac{dy}{dx} = 12$ | $\frac{\mathrm{d}y}{\mathrm{d}x} = k x^{-\frac{1}{2}}$ $\alpha y \frac{\mathrm{d}y}{\mathrm{d}x} = \beta$ | - M1 |
| | $\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\mathrm{d}y}{\mathrm{d}p} \cdot \frac{\mathrm{d}p}{\mathrm{d}x} = 6 \cdot \frac{1}{6p}$ | their $\frac{\mathrm{d}y}{\mathrm{d}p} \times \left(\frac{1}{\mathrm{their}} \frac{\mathrm{d}x}{\mathrm{d}p}\right)$ | 1011 |
| | $\frac{dy}{dx} = \frac{1}{2}\sqrt{12}x^{-\frac{1}{2}} \text{ or } 2y\frac{dy}{dx} = 12 \text{ or } \frac{dy}{dx} = 6.\frac{1}{6p}$ or equivalent expressions | Correct differentiation | A1 |
| | $m_T = \frac{1}{p} \Rightarrow m_N = -p$ | Correct perpendicular gradient rule | M1 |
| | $y - 6p = -p(x - 3p^2)$ | $y-6p = \text{their } m_N \left(x-3p^2\right) \text{ or }$ $y=mx+c \text{ with their } m_N \text{ and } (3p^2,6p) \text{ in }$ an attempt to find 'c'. Their m_N must have come from calculus and should be a function of p which is not their tangent gradient. | M1 |
| | $y + px = 6p + 3p^3 *$ | Achieves printed answer with no errors | A1* |
| (b) | $p = 2 \Rightarrow y + 2x = 12 + 24$ | Substitutes the given value of <i>p</i> into the normal | M1 |
| | $y + \frac{y^2}{6} = 36$ | Substitutes to obtain an equation in one variable $(x, y \text{ or } "q")$ | M1 |
| | $y^2 + 6y - 216 = 0$ | | |
| | $(y+18)(y-12) = 0 \Rightarrow y =$ | Solves their 3TQ | M1 |
| | $y = -18 \Rightarrow x = 27$ | A1: One correct coordinate A1: Both coordinates correct | A1, A1 |
| | Forms is (2, 0) on a 2 on OS 2 | Must be seen an used in (s) | (5) |
| | Focus is (3, 0) or $a = 3$ or OS = 3 $y = 0 \Rightarrow x = 18$ | Must be seen or used in (c) | B1 |
| (c) | $A = \frac{1}{2}(18-3)(12) + \frac{1}{2}(18-3)(18)$ | M1: Correct attempt at area A1: Correct expression | M1A1 |
| | A = 225 | Correct area | A1 |
| | | | (4) Total 14 |
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| Question Number | Scheme | Notes | Marks |
|--------------------|---|---|---------|
| 5(a) | $\alpha + \beta = -\frac{3}{4}, \alpha\beta = \frac{1}{4}$ | | B1, B1 |
| | | | (2) |
| (b) | $\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta = \frac{9}{16} - \frac{1}{2} = \frac{1}{16}$ M1:Us | se of $\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$ | M1 A1 |
| - | 111. 16 | C50 (anow 0.0025) | (2) |
| (c) | Sum $4\alpha - \beta + 4\beta - \alpha = 3(\alpha + \beta) = -\frac{9}{4}$ | Attempt numerical sum | M1 |
| | Product $(4\alpha - \beta)(4\beta - \alpha) = 17\alpha\beta - 4(\alpha^2 + \beta^2)$ = $\frac{17}{4} - \frac{1}{4} = 4$ | Attempt numerical product | M1 |
| | $x^2 - \left(-\frac{9}{4}\right)x + 4\left(=0\right)$ | Uses $x^2 - (\text{sum})x + (\text{prod})$ with sum, prod numerical (= 0 not reqd.) | M1 |
| | $4x^2 + 9x + 16 = 0$ | Any multiple (including = 0) | A1 |
| | | | (4) |
| | | | Total 8 |
| (a) | Alternative: Finds roo | ts explicitly | |
| (a) | $x = -\frac{3}{8} \pm \frac{\sqrt{7}}{8}i$ | | |
| | $x = -\frac{3}{8} \pm \frac{\sqrt{7}}{8}i$ $\alpha + \beta = -\frac{3}{8} + \frac{\sqrt{7}}{8}i - \frac{3}{8} - \frac{\sqrt{7}}{8}i = -\frac{3}{4}$ | | B1 |
| | $\alpha\beta = \left(-\frac{3}{8} + \frac{\sqrt{7}}{8}i\right)\left(-\frac{3}{8} - \frac{\sqrt{7}}{8}i\right) = \frac{1}{4}$ | | B1 |
| | | | (2) |
| (b) | $\alpha^2 + \beta^2 = \left(-\frac{3}{8} + \frac{\sqrt{7}}{8}i\right)^2 + \left(-\frac{3}{8} - \frac{\sqrt{7}}{8}i\right)^2 = \frac{1}{16}$ | M1: Substitutes their α and β and attempt to square and add both brackets A1: $\frac{1}{16}$ cso (allow 0.0625) | M1 A1 |
| | | 10 , | (2) |
| (c) | $4\alpha - \beta = -\frac{9}{8} + \frac{5\sqrt{7}}{8}i, 4\beta - \alpha = -\frac{9}{8} - \frac{5\sqrt{7}}{8}i$ | | |
| | $f(x) = \left(x - \left(-\frac{9}{8} + \frac{5\sqrt{7}}{8}i\right)\right)\left(x - \left(-\frac{9}{8} - \frac{5\sqrt{7}}{8}i\right)\right)$ | Uses $(x-(4\alpha-\beta))(x-(4\beta-\alpha))$ With numerical values (May expand first) | M1 |
| | $f(x) = x^{2} + x \left(-\frac{9}{8} - \frac{5\sqrt{7}}{8}i\right) - x \left(-\frac{9}{8} + \frac{5\sqrt{7}}{8}i\right)$ | | M1 |
| | Attempt to expand (may occur in terms of α and β $= x^2 + \frac{9}{4}x + 4(=0)$ | | M1 |
| | 7 () | Collects terms (= 0 not reqd.) | |
| | $4x^2 + 9x + 16 = 0$ | Any multiple (including = 0) | A1 (4) |
| | | | Total 8 |

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| Question Number | Scheme | Notes | Marks | |
|--------------------|--|--|----------|--|
| 6(i)(a) | A : Stretch scale factor 3 parallel to the <i>x</i> -axis | B1: Stretch B1: SF 3 parallel to (or along) <i>x</i> -axis Allow e.g. horizontal stretch SF 3 (Ignore any reference to the origin) | B1B1 | |
| | | | (2) | |
| (b) | B : Rotation 210 degrees (anticlockwise) about (0, 0) or about O | B1: Rotation about (0, 0) B1: 210 degrees (anticlockwise) (or equivalent e.g150° or 150° clockwise). Allow equivalents in radians. | B1B1 | |
| | | | (2) | |
| (c) | $\mathbf{C} = \mathbf{B}\mathbf{A} = \begin{pmatrix} -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix} \begin{pmatrix} 3 & 0 \\ 0 & 1 \end{pmatrix}$ | Attempts BA (This statement is sufficient) | M1 | |
| | $= \begin{pmatrix} -\frac{3\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{3}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$ | Correct matrix | A1 | |
| | | | (2) | |
| (ii) | $\det \mathbf{M} = (2k+5).k-1 \times (-4)(=2k^2+5k+4)$ | M1: Correct attempt at determinant A1: Correct determinant (allow unsimplified) | M1A1 | |
| | $b^2 - 4ac = 25 - 32$ | Attempts discriminant or uses quadratic formula | M1 | |
| | $b^2 - 4ac < 0$ So no real roots so detM \neq 0 | Convincing explanation and conclusion with no previous errors | A1 | |
| | | | (4) | |
| | | | Total 10 | |
| (ii) Way 2 | $(2k+5).k-1\times(-4)(=2k^2+5k+4)$ | M1: Correct attempt at determinant A1: Correct determinant (allow unsimplified) | M1A1 | |
| | $=2\left(k+\frac{5}{4}\right)^2+\frac{7}{8}$ | Attempts to complete the square: | M1 | |
| | $ \frac{\text{detM} > 0 \ \forall \ k}{\text{Therefore detM} \neq 0} $ | Convincing explanation and conclusion with no previous errors | A1 | |
| (ii) Way 3 | $(2k+5).k-1\times(-4)(=2k^2+5k+4)$ | M1: Correct attempt at determinant A1: Correct determinant (allow unsimplified) | M1A1 | |
| | $\frac{d(det\mathbf{M})}{dk} = 4k + 5 = 0 \Longrightarrow k = -\frac{5}{4}$ | | | |
| | $k = -\frac{5}{4} \Rightarrow det \mathbf{M} = \frac{7}{8}$ | Attempts coordinates of turning point | M1 | |
| | Minimum $det\mathbf{M}$ is $\frac{7}{8}$ therefore $\mathbf{det}\mathbf{M} \neq 0$ | Convincing explanation and conclusion with no previous errors | A1 | |

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Mathematics F1

| Question Number | Scheme | Notes | Marks |
|--------------------|---|--|-----------------|
| 7 | $\sum_{r=1}^{n} (r+a)(r+b) =$ | $\frac{1}{6}n(2n+11)(n-1)$ | |
| (a) | $(r+a)(r+b) = r^2 + ra + rb + ab$ | | B1 |
| | $\sum_{r=1}^{n} (r+a)(r+b) = \frac{1}{6}n(n+1)(2$ | $(n+1)+(a+b)\frac{1}{2}n(n+1)+abn$ | M1A1B1 |
| | M1: Attempt to use one of the | e standard formulae correctly | |
| | A1: $\frac{1}{6}n(n+1)(2n+1)$ | $1)+(a+b)\frac{1}{2}n(n+1)$ | |
| | B1: | abn | |
| | $\frac{1}{6}n\Big[(n+1)(2n+1)+3(a+b)(n+1)\Big]$ | $+1)+6ab$ $=\frac{1}{6}n(2n+11)(n-1)$ | |
| | $(n+1)(2n+1)+3(a+b)(n+1)+6ab=2n^2+9n-11$ | | |
| | $2n^{2} + 3n + 1 + 3(a+b)(n+1) + 6ab = 2n^{2} + 9n - 11$ | | |
| | 3+3a+3b=9, $3a+3b+1+6ab=-11$ | M1: Compares coefficients to obtain at least one equation in <i>a</i> and <i>b</i> | 343434 |
| | (a+b=2, ab=-3) | M1: One correct equation | M1M1M1 |
| | | M1: Both equations correct Both values correct. This can be | |
| | b = -1, a = 3 | withheld if $b = 3$, $a = -1$ is not rejected. | A1 |
| | | | (8) |
| (b) | $\sum_{r=9}^{20} \left(r + \epsilon\right)$ | a)(r+b) | |
| | $\sum_{r=9}^{20} (r+a)(r+b) = f(20) - f(8 \text{ or } 9)$ | <u>Use</u> of f(20) – f(8 or 9) | M1 |
| | $=\frac{1}{6}(20)(51)(19)-\frac{1}{6}(8)(27)(7)$ | Correct (possibly un-simplified) numerical expression | A1 |
| | =3230 - 252 = 2978 | cao | A1 |
| | | | (3) Total 11 |
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| Question Number | Scheme | | Notes | Marks |
|--------------------|---|---------------|---|----------|
| 8(i) | When $n = 1$ $u_1 = 2^1 + 3^1 = 5$ When $n = 2$ $u_2 = 2^2 + 3^2 = 13$ | Both | | B1 |
| | True for $n = 1$ a | nd n = 1 | 2 | |
| | Assume $u_k = 2^k + 3^k$ and | $u_{k+1} = 1$ | $2^{k+1} + 3^{k+1}$ | |
| | $u_{k+2} = 5u_{k+1} - 6u_k = 5(2^{k+1} + 3^{k+1}) - 6(2^k + 3^k)$ | | M1: Attempts u_{k+2} in terms of u_{k+1} and u_k A1: Correct expression | M1A1 |
| | $=5.2^{k+1} + 5.3^{k+1} - 6.2^k - 6.3^k$ | | • | |
| | $=5.2^{k+1}-3.2^{k+1}+5.3^{k+1}-2.3^{k+1}$ | | Attempt u_{k+2} in terms of $2^{f(k)}$ and $3^{f(k)}$ only | M1 |
| | So $u_{k+2} = 2.2^{k+1} + 3.3^{k+1}$ | | | |
| | $=2^{(k+1)+1}+3^{(k+1)+1} \text{or} 2^{k+2}+3^{k+2}$ | | Correct expression with no errors | A1 |
| | If true for k and $k + 1$ then shown true for $k + 1$ as true for $n = 1$ and $n = 2$, true for $n \in \mathbb{Z}^d$ | | Full conclusion with all previous marks scored | A1 |
| | , | | | (6) |
| (ii) | $f(2) = 7^4 - 48(2) - 1 = 2304$ So true for $n = 2$ | | Shows true for $n = 2$ | B1 |
| | Assume | | | |
| | $f(k) = 7^{2k} - 48k - 1 = 2304p$ | | | |
| | for some integer p | | | |
| | $f(k+1)-f(k) = 7^{2k+2} - 48(k+1)-1-(7^{2k}-48)$ | (k-1) | Attempt $f(k+1) - f(k)$ | M1 |
| | $=7^{2k+2}-7^{2k}-48$ | | | |
| | $=7^{2k}(49-1)-48$ | | | |
| | 10f(L) + 10 ² L | | M1: Attempt rhs in terms of $f(k)$ or $7^{2k} - 48k - 1$ | - M1A1 |
| | $=48f(k)+48^2k$ | | A1: Correct expression which is a multiple of 2304 | WIIAI |
| | $= 48 \times 2304 p + 2304 k$ | | | |
| | $f(k+1) = 49 \times 2304 p + 2304 k$ | | Obtains $f(k+1)$ as a correct multiple of 2304 with no errors | A1 |
| | If true for k then shown true for $k + 1$ and as tr | ue for | Full conclusion with all | A1 |
| | $n = 2$, true for $n \ge 2$ $(n \in \mathbb{Z})$ | | previous marks scored | Λ1 |
| | | | | (6) |
| | | | | Total 12 |

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