



# Mark Scheme (Results)

## Summer 2012

### GCE Further Pure FP2 (6668) Paper 1

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Summer 2012

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**Summer 2012**  
**6668 Further Pure 2**  
**FP2 Mark Scheme**

## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## EDEXCEL GCE MATHEMATICS

### General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.
3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod – benefit of doubt
  - ft – follow through
  - the symbol  $\checkmark$  will be used for correct ft
  - cao – correct answer only
  - cso – correct solution only. There must be no errors in this part of the question to obtain this mark
  - isw – ignore subsequent working
  - awrt – answers which round to
  - SC: special case
  - oe – or equivalent (and appropriate)
  - dep – dependent
  - indep – independent
  - dp decimal places
  - sf significant figures
  - \* The answer is printed on the paper
  - $\square$  The second mark is dependent on gaining the first mark
4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

## General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

### Method mark for solving 3 term quadratic:

#### 1. Factorisation

$(x^2 + bx + c) = (x + p)(x + q)$ , where  $|pq| = |c|$ , leading to  $x = \dots$

$(ax^2 + bx + c) = (mx + p)(nx + q)$ , where  $|pq| = |c|$  and  $|mn| = |a|$ , leading to  $x = \dots$

#### 2. Formula

Attempt to use correct formula (with values for  $a$ ,  $b$  and  $c$ ), leading to  $x = \dots$

#### 3. Completing the square

Solving  $x^2 + bx + c = 0$ :  $(x \pm \frac{b}{2})^2 \pm q \pm c$ ,  $q \neq 0$ , leading to  $x = \dots$

### Method marks for differentiation and integration:

#### 1. Differentiation

Power of at least one term decreased by 1. ( $x^n \rightarrow x^{n-1}$ )

#### 2. Integration

Power of at least one term increased by 1. ( $x^n \rightarrow x^{n+1}$ )

### Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

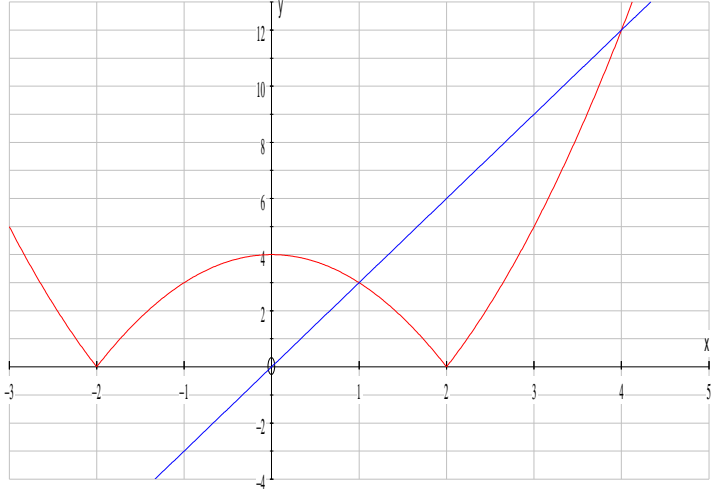
### Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

### Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

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6668 Further Pure Mathematics FP2  
Mark Scheme

Question Number	Scheme	Marks
1.	<p> <math>x^2 - 4 = 3x</math> and <math>x^2 - 4 = -3x</math>, or graphical method, or squaring both sides, leading to <math>x = \dots</math>  <math>(x = -4, x = -1)</math> <math>x = 1, x = 4</math> </p> <p style="text-align: right;">seen</p> <p>anywhere</p> <p>Using only 2 critical values to find an inequality</p> <p><math>x &lt; 1</math> <math>x &gt; 4</math></p> <p style="text-align: right;">both strict, ignore 'and'</p> <p><b>Notes</b></p>  <p> <math>1^{\text{st}}</math> M1 accept <math>\pm(x^2 - 4) &gt; 3x</math> or <math>\pm(x^2 - 4) = 3x</math> Require <b>modulus</b> of parabola and straight line with positive gradient through origin for graphical method.  <math>1^{\text{st}}</math> B1 for <math>x=1</math>, <math>2^{\text{nd}}</math> B1 for <math>x=4</math>  <math>2^{\text{nd}}</math> M1 dependent upon first M1                      A0 for error in solution of quadratic leading to correct answer.                 </p>	<p>M1</p> <p>B1 B1</p> <p>dM1</p> <p>A1</p> <p style="text-align: right;">(5) 5</p>

Question Number	Scheme	Marks
2.	$y = r \sin \theta = \sin \theta + 2 \sin \theta \cos \theta$ $\frac{dy}{d\theta} = \cos \theta + 2 \cos 2\theta$ $4 \cos^2 \theta + \cos \theta - 2 = 0$ $\cos \theta = \frac{-1 \pm \sqrt{1+32}}{8}$ $OP = r = 1 + \frac{-1 + \sqrt{1+32}}{4} = \frac{3 + \sqrt{33}}{4}$ <p>Notes                      B1 for <math>\sin \theta + 2 \sin \theta \cos \theta</math> or <math>\sin \theta (1 + 2 \cos \theta)</math>                      1<sup>st</sup> M1 for use of Product Rule or Chain Rule (require 2 or condone 1/2)                      1<sup>st</sup> A1 equation required                      2<sup>nd</sup> M1 Valid attempt at solving 3 term quadratic (usual rules) to give <math>\cos \theta = \dots</math>                      2<sup>nd</sup> A1 for exact or 3 dp or better (-0.843.....and 0.593....)                      3<sup>rd</sup> M1 for 1+2x 'their <math>\cos \theta</math>'                      3<sup>rd</sup> A1 for any form A0 if negative solution not discounted.</p>	B1 M1 A1oe M1 A1 M1 A1 (7) 7

Question Number	Scheme	Marks
<p><b>3.</b></p> <p><b>(a)</b></p>	$r = \sqrt{(-2)^2 + (2\sqrt{3})^2} = 4$ $\tan \theta = -\sqrt{3} \quad (\text{Also allow M mark for } \tan \theta = \sqrt{3})$ <p style="text-align: center;">M mark can be implied by <math>\theta = \pm \frac{2\pi}{3}</math> or <math>\theta = \pm \frac{\pi}{3}</math></p> $\theta = \frac{2\pi}{3}$	<p>B1</p> <p>M1</p>  <p>A1</p>
		(3)
<p><b>(b)</b></p>	<p>Finding the 4<sup>th</sup> root of their <math>r</math>: <math>r = 4^{\frac{1}{4}} (= \sqrt{2})</math></p> <p>For one root, dividing their <math>\theta</math> by 4: <math>\theta = \frac{2\pi}{3} \div 4 = \frac{\pi}{6}</math></p> <p>For another root, add or subtract a multiple of <math>2\pi</math> to their <math>\theta</math> <b>and</b> divide by 4 in correct order.</p> $\sqrt{2}(\cos \theta + i \sin \theta), \text{ where } \theta = -\frac{5\pi}{6}, -\frac{\pi}{6}, \frac{\pi}{6}, \frac{2\pi}{6}$	<p>M1</p> <p>M1</p> <p>M1</p>  <p>A1 A1</p>
		(5)
		<b>8</b>
<p><b>(a)</b></p>	<p>Notes</p> <p>M1 Accept <math>\pm\sqrt{3}</math> or <math>\pm \frac{1}{\sqrt{3}}</math></p> <p>A1 Accept awrt 2.1. A0 if in degrees.</p>	
<p><b>(b)</b></p>	<p>2<sup>nd</sup> M1 for awrt 0.52</p> <p>1<sup>st</sup> A1 for two correct values</p> <p>2<sup>nd</sup> A1 for all correct values values in correct form and no more</p>	

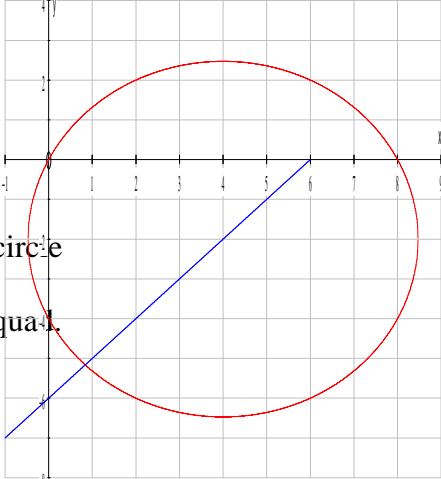


Question Number	Scheme	Marks
4.	$m^2 + 5m + 6 = 0 \quad m = -2, -3$ <p>C.F. <math>(x =) Ae^{-2t} + Be^{-3t}</math></p> <p>P.I. <math>x = P \cos t + Q \sin t</math></p> $\dot{x} = -P \sin t + Q \cos t$ $\ddot{x} = -P \cos t - Q \sin t$ $(-P \cos t - Q \sin t) + 5(-P \sin t + Q \cos t) + 6(P \cos t + Q \sin t) = 2 \cos t - \sin t$ $-P + 5Q + 6P = 2 \quad \text{and} \quad -Q - 5P + 6Q = -1, \text{ and solve for } P \text{ and } Q$ $P = \frac{3}{10} \quad \text{and} \quad Q = \frac{1}{10}$ $x = Ae^{-2t} + Be^{-3t} + \frac{3}{10} \cos t + \frac{1}{10} \sin t$ <p>Notes</p> <p>1<sup>st</sup> M1 form quadratic and attempt to solve (usual rules)</p> <p>1<sup>st</sup> B1 Accept negative signs for coefficients. Coefficients must be different.</p> <p>2<sup>nd</sup> M1 for differentiating their trig PI twice</p> <p>3<sup>rd</sup> M1 for substituting <math>x</math>, <math>\dot{x}</math> and <math>\ddot{x}</math> expressions</p> <p>4<sup>th</sup> M1 Form 2 equations in two unknowns and attempt to solve</p> <p>1<sup>st</sup> A1 for one correct, 2<sup>nd</sup> A1 for two correct</p> <p>2<sup>nd</sup> B1 for <math>x</math>=their CF + their PI as functions of <math>t</math></p> <p>Condone use of the wrong variable (e.g. <math>x</math> instead of <math>t</math>) for all marks except final B1.</p>	<p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1 A1</p> <p>B1 ft</p> <p>(9)</p> <p>9</p>

Question Number	Scheme	Marks
<p><b>5.</b></p> <p><b>(a)</b></p> <p><b>(b)</b></p>	$x \frac{d^2 y}{dx^2} + \frac{dy}{dx} = 3 + 2y \frac{dy}{dx}$ <p>(Using differentiation of product or quotient and also differentiation of implicit function)</p> $x \frac{d^2 y}{dx^2} + (1 - 2y) \frac{dy}{dx} = 3 \quad \text{**ag**}$ $\left( x \frac{d^3 y}{dx^3} + \frac{d^2 y}{dx^2} \right) + \dots$ $\dots \left[ (1 - 2y) \frac{d^2 y}{dx^2} - 2 \left( \frac{dy}{dx} \right)^2 \right] = 0$ <p>At <math>x = 1</math>: <math>\frac{dy}{dx} = 4</math></p> $\frac{d^2 y}{dx^2} = 7 \quad \frac{d^3 y}{dx^3} = 32$ $(y =) f(1) + f'(1)(x-1) + \frac{f''(1)(x-1)^2}{2} + \frac{f'''(1)(x-1)^3}{6} \dots$ $y = 1 + 4(x-1) + \frac{7}{2}(x-1)^2 + \frac{16}{3}(x-1)^3 \quad (\text{or equiv.})$ <p>Notes</p> <p><b>(a)</b> Finding second derivative and substituting into given answer acceptable</p> <p><b>(b)</b> 1<sup>st</sup> M1 for differentiating second term to obtain an expression involving</p> $\frac{d^2 y}{dx^2} \text{ and } \left( \frac{dy}{dx} \right)^2$ <p>B1B1B1 for 4,7,32 seen respectively</p> <p>2<sup>nd</sup> M1 require <math>f(1)</math> or 1, <math>f'(1)</math> etc and <math>x-1</math> and at least first 3 terms</p> <p>A1 for 4 terms following through their constants</p> <p>Condone <math>f(x)=</math> instead of <math>y=</math></p>	<p>M1</p> <p>A1 cso</p> <p>(2)</p> <p>B1</p> <p>M1 A1</p> <p>B1</p> <p>B1, B1</p> <p>M1</p> <p>A1 ft</p> <p>(8)</p> <p><b>10</b></p>

Question Number	Scheme	Marks
<p><b>6.</b></p> <p><b>(a)</b></p> <p><b>(b)</b></p> <p><b>(c)</b></p> <p><b>(a)</b></p> <p><b>(b)</b></p> <p><b>(c)</b></p>	$\frac{1}{r(r+2)} = \frac{1}{2} \left( \frac{1}{r} - \frac{1}{r+2} \right) = \frac{1}{2r} - \frac{1}{2r+4}$ <p> <math>r = 1: \frac{1}{2} \left( \frac{1}{1} - \frac{1}{3} \right)</math>  <math>r = 2: \frac{1}{2} \left( \frac{1}{2} - \frac{1}{4} \right)</math>  <math>r = 3: \frac{1}{2} \left( \frac{1}{3} - \frac{1}{5} \right)</math>  <math>r = n-1: \frac{1}{2} \left( \frac{1}{n-1} - \frac{1}{n+1} \right)</math>  <math>r = n: \frac{1}{2} \left( \frac{1}{n} - \frac{1}{n+2} \right)</math> </p> <p>Summing: <math>\sum_{r=1}^n \frac{1}{r(r+2)} = \frac{1}{2} \left( 1 + \frac{1}{2} - \frac{1}{n+1} - \frac{1}{n+2} \right)</math></p> $= \frac{1}{2} \left( \frac{3(n+1)(n+2) - 2(n+1) - 2(n+2)}{2(n+1)(n+2)} \right) = \frac{n(3n+5)}{4(n+1)(n+2)}$ <p> <math>\sum_{r=1}^{2n} \frac{1}{r(r+2)} = \frac{2n(6n+5)}{4(2n+1)(2n+2)}</math>  <math>S_{2n} - S_n = \frac{2n(6n+5)}{4(2n+1)(2n+2)} - \frac{n(3n+5)}{4(n+1)(n+2)}</math>  <math>= \frac{n(6n+5)(n+2) - n(3n+5)(2n+1)}{4(n+1)(n+2)(2n+1)}</math>  <math>= \frac{n(6n^2 + 17n + 10 - 6n^2 - 13n - 5)}{4(n+1)(n+2)(2n+1)} = \frac{n(4n+5)}{4(n+1)(n+2)(2n+1)}</math> </p> <p>(*ag*)</p> <p>1<sup>st</sup> and 2<sup>nd</sup> B1 Any form is acceptable</p> <p>1<sup>st</sup> M1 must include at least 4 out of 5 of (r=)1,2,3 and n-1, n</p> <p>1<sup>st</sup> A1 require all terms that do not cancel to be accurate</p> <p>2<sup>nd</sup> M1 Summed expression involving all terms that do not cancel</p> <p>2<sup>nd</sup> A1 Correct expression</p> <p>3<sup>rd</sup> M1 for attempt to find single fraction</p> <p>1<sup>st</sup> M1 for expression for <math>S_{2n} - S_n</math></p>	<p>B1,B1oe (2)</p> <p>M1</p> <p>A1</p> <p>M1 A1</p> <p>M1 A1cao (6)</p> <p>B1oe</p> <p>M1</p> <p>A1 cso (3)</p> <p><b>11</b></p>

Question Number	Scheme	Marks
<p>7.</p> <p>(a)</p> <p>(b)</p> <p>(c)</p>	<p>seen</p> $\frac{dy}{dx} = v + x \frac{dv}{dx}$ $3x^3 v^2 \left( v + x \frac{dv}{dx} \right) = x^3 + v^3 x^3 \quad \Rightarrow \quad 3v^2 x \frac{dv}{dx} = 1 - 2v^3$ <p>(**ag**)</p> $\int \frac{3v^2}{1-2v^3} dv = \int \frac{1}{x} dx$ $-\frac{1}{2} \ln(1-2v^3) = \ln x + C$ $-\ln(1-2v^3) = \ln x^2 + \ln A$ $Ax^2 = \frac{1}{1-2v^3}$ $1 - \frac{2y^3}{x^3} = \frac{1}{Ax^2}$ $y = \sqrt[3]{\frac{x^3 - Bx}{2}} \quad \text{or equivalent}$ <p>Using <math>y = 2</math> at <math>x = 1</math>: <math>12 \frac{dy}{dx} = 1 + 8</math></p> <p>At <math>x = 1</math>, <math>\frac{dy}{dx} = \frac{3}{4}</math></p> <p>Notes</p> <p>(a) M1 for substituting <math>y</math> and <math>\frac{dy}{dx}</math> obtaining an expression in <math>v</math> and <math>x</math> only</p> <p>(b) 1<sup>st</sup> M1 for separating variables                  2<sup>nd</sup> M1 for attempting to integrate both sides                  1<sup>st</sup> A1 both sides required or equivalent expressions. (Modulus not required.)                  3<sup>rd</sup> M1 Removing logs, dealing correctly with constant                  4<sup>th</sup> M1 dep on 1st M. Substitute <math>v = \frac{y}{x}</math> and rearranging to <math>y = f(x)</math></p> <p>(c) M1 for finding a numerical value for <math>\frac{dy}{dx}</math>                  A1 for correct numerical answer oe.</p>	<p>B1</p> <p>M1 A1 cso</p> <p>(3)</p> <p>M1</p> <p>M1 A1</p> <p>M1</p> <p>dM1 A1cso</p> <p>(6)</p> <p>M1</p> <p>A1</p> <p>(2)</p> <p><b>11</b></p>

Question Number	Scheme	Marks
<p><b>8.</b></p> <p><b>(a)</b></p>	$ x + iy - 6i  = 2 x + iy - 3 $ $x^2 + (y - 6)^2 = 4[(x - 3)^2 + y^2]$ $x^2 + y^2 - 12y + 36 = 4x^2 - 24x + 36 + 4y^2$ $3x^2 + 3y^2 - 24x + 12y = 0$ $(x - 4)^2 + (y + 2)^2 = 20$ <p>Centre (4, -2), Radius <math>\sqrt{20} = 2\sqrt{5} = \text{awrt } 4.47</math></p> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> <p>Centre in correct quad for their circle Passes through O centre in 4<sup>th</sup> quad.</p> <p>Half line with positive gradient</p> <p>Correct position, clearly through (6, 0)</p> </div> </div>	<p>M1</p> <p>M1 A1</p> <p>M1</p> <p>A1 A1</p> <p>(6)</p> <p>M1</p> <p>A1cao</p> <p>B1</p> <p>B1</p> <p>(4)</p>
<p><b>(b)</b></p>	<p>Equation of line <math>y = x - 6</math></p> <p>Attempting simultaneous solution of <math>(x - 4)^2 + (y + 2)^2 = 20</math> and <math>y = x - 6</math></p> $x = 4 \pm \sqrt{10}$ $(4 - \sqrt{10}) + i(-2 - \sqrt{10})$	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1cao</p> <p>(4)</p>
<p><b>(a)</b></p>	<p>Notes</p> <p>1<sup>st</sup> M Substituting <math>z = x + iy</math> oe</p> <p>2<sup>nd</sup> M implementing modulus of both sides and squaring. Require <b>Re<sup>2</sup> plus Im<sup>2</sup></b> on both sides &amp; no terms in i. Condone 2 instead of 4 here.</p> <p>3<sup>rd</sup> M1 for gathering terms and attempting to find centre and / or radius</p>	<p>(4)</p> <p><b>14</b></p>

Question Number	Scheme	Marks
Alt 8(c)	<p>2<sup>nd</sup> A1 for centre, 3<sup>rd</sup> A1 for radius</p> <p><b>For geometric approach in this part.</b></p> <p>Centre (4,-2) on line, can be implied.</p> <p>Use of Pythagoras or trigonometry to find lengths of isosceles triangle</p> $x = 4 - \sqrt{10}$ $(4 - \sqrt{10}) + i(-2 - \sqrt{10})$	B1 M1 A1 A1cao



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