

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Pearson Edexcel
International
Advanced Level

Centre Number

--	--	--	--	--

Candidate Number

--	--	--	--	--

Monday 14 January 2019

Afternoon (Time: 1 hour 30 minutes)

Paper Reference **WFM01/01**

Further Pure Mathematics F1
Advanced/Advanced Subsidiary

You must have:

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

P54951A

©2019 Pearson Education Ltd.

1/1/1/1/



Pearson

Leave
blank

1. The point $A(12, 12)$ lies on the parabola with equation $y^2 = 12x$. The point S is the focus of this parabola. The line l passes through A and S .

(a) Find an equation of the line l .

(3)

The line l meets the directrix of the parabola at the point B .

(b) Find the coordinates of B .

(3)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 1 continued

Handwriting practice area with horizontal lines.

(Total 6 marks)

Q1

Mark box for Q1



P 5 4 9 5 1 A 0 3 3 2

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Leave
blank

2.

$$f(z) = z^3 - 2z^2 + 16z - 32$$

(a) Show that $f(2) = 0$ (1)

(b) Use algebra to solve $f(z) = 0$ completely. (3)

(c) Show, on a single Argand diagram, all three roots of the equation $f(z) = 0$ (2)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 2 continued

Handwriting practice area with horizontal lines.

(Total 6 marks)

Q2



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Leave
blank

3. (a) Use the standard results for $\sum_{r=1}^n r$ and $\sum_{r=1}^n r^2$ to show that, for all positive integers n ,

$$\sum_{r=1}^n (2r + 5)^2 = \frac{n}{3}[(an + b)^2 + c]$$

where a , b and c are integers to be found.

(5)

- (b) Use the answer to part (a) to evaluate $\sum_{r=0}^{100} (2r + 5)^2$

(2)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 3 continued

Handwriting practice area with horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 3 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 3 continued

Handwriting practice area with horizontal lines.

(Total 7 marks)

Q3

Mark box



P 5 4 9 5 1 A 0 9 3 2

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

$$f(x) = 2x^3 - \frac{7}{x^2} + 16, \quad x \neq 0$$

(a) Starting with the interval $[-2, -1]$, use interval bisection twice to find an interval of width 0.25 that contains α .

(3)

(b) Taking 0.65 as a first approximation to β , apply the Newton-Raphson procedure once to $f(x)$ to obtain a second approximation to β , giving your answer to 4 decimal places.

(4)



Leave
blank

Question 4 continued

Handwriting practice area with horizontal lines.

(Total 7 marks)

Q4

Mark box

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 5 4 9 5 1 A 0 1 1 3 2

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- The point P , on H , has coordinates $\left(4p, \frac{4}{p}\right)$ where p is a non-zero constant.

- $$x + p^2 y = 8p \quad (4)$$

(b) use algebra to find the coordinates of the two possible positions of P . (4)

[illegible]

Leave
blank

Question 5 continued

Handwriting practice area with horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 5 4 9 5 1 A 0 1 3 3 2

Leave
blank

Question 5 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 5 continued

Q5

(Total 8 marks)



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- $$12x^2 - 3x + 4 = 0$$

(a) find the exact value of $\frac{2}{\alpha} + \frac{2}{\beta}$ **(3)**

- (b) find a quadratic equation that has roots $\frac{2}{\alpha} - \beta$ and $\frac{2}{\beta} - \alpha$ giving your answer in the form $ax^2 + bx + c = 0$, where a, b and c are integers to be found. (6)

Leave
blank

Question 6 continued

Handwriting practice area with horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 5 4 9 5 1 A 0 1 7 3 2

Leave
blank

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 6 continued

Handwriting practice area with horizontal lines.

(Total 9 marks)

Q6

Mark box

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 5 4 9 5 1 A 0 1 9 3 2

Leave
blank

$$\mathbf{P} = \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix}$$

- (a) Show that $\mathbf{P}^3 = 8\mathbf{I}$, where \mathbf{I} is the 2×2 identity matrix. (3)
- (b) Describe fully the transformation represented by the matrix \mathbf{P} as a combination of two simple geometrical transformations. (4)
- (c) Find the matrix \mathbf{P}^{35} , giving your answer in the form

$$\mathbf{P}^{35} = 2^k \begin{pmatrix} -1 & a \\ b & -1 \end{pmatrix}$$

where k is an integer and a and b are surds to be found.

(2)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

[illegible]

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 7 continued

Handwriting practice area with horizontal lines.

(Total 9 marks)

Q7

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 5 4 9 5 1 A 0 2 3 3 2

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- $$\begin{pmatrix} 5 & -8 \\ 2 & -3 \end{pmatrix}^n = \begin{pmatrix} 1+4n & -8n \\ 2n & 1-4n \end{pmatrix} \quad (5)$$

- $$\begin{aligned} u_1 &= 8, \quad u_2 = 40 \\ u_{n+2} &= 8u_{n+1} - 12u_n \quad n \geq 1 \end{aligned}$$

$$u_n = 6^n + 2^n \quad (5)$$

Leave
blank

Question 8 continued

Lined area for writing the answer to Question 8 continued.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 5 4 9 5 1 A 0 2 5 3 2

Leave
blank

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 8 continued

Q8

(Total 10 marks)



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- (5)

Leave
blank

Question 9 continued

Handwriting practice area with horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 5 4 9 5 1 A 0 2 9 3 2

Leave
blank

Question 9 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Leave
blank

Question 9 continued

Handwriting practice area with horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 5 4 9 5 1 A 0 3 1 3 2

Leave
blank

Question 9 continued

Handwriting practice area with horizontal lines.

(Total 13 marks)

TOTAL FOR PAPER: 75 MARKS

END

Q9

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

