



Mark Scheme (Results)

Summer 2017

Pearson Edexcel International A Level
in Further Pure Mathematics F1 (WFM01/01)

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Summer 2017

Publications Code WFM01_01_1706_MS

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL IAL MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 75
2. The Edexcel Mathematics mark schemes use the following types of marks:
 - **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
 - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - **B** marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod – benefit of doubt
- ft – follow through
- the symbol \surd will be used for correct ft
- cao – correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw – ignore subsequent working
- awrt – answers which round to
- SC: special case
- o.e. – or equivalent (and appropriate)
- d... or dep – dependent
- indep – independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper or ag- answer given
- \square or d... The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
7. Ignore wrong working or incorrect statements following a correct answer.

General Principles for Further Pure Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:**1. Factorisation**

$$(x^2 + bx + c) = (x + p)(x + q), \text{ where } |pq| = |c|, \text{ leading to } x = \dots$$

$$(ax^2 + bx + c) = (mx + p)(nx + q), \text{ where } |pq| = |c| \text{ and } |mn| = |a|, \text{ leading to } x = \dots$$

2. Formula

Attempt to use the correct formula (with values for a , b and c).

3. Completing the square

$$\text{Solving } x^2 + bx + c = 0: \left(x \pm \frac{b}{2}\right)^2 \pm q \pm c = 0, \quad q \neq 0, \text{ leading to } x = \dots$$

Method marks for differentiation and integration:**1. Differentiation**

Power of at least one term decreased by 1. ($x^n \rightarrow x^{n-1}$)

2. Integration

Power of at least one term increased by 1. ($x^n \rightarrow x^{n+1}$)

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

May 2017

WFM01 Further Pure Mathematics F1

Mark Scheme

Question Number	Scheme	Notes	Marks
1.	$3x^2 - 5x + 1 = 0$ has roots a, b		
	$a + b = \frac{5}{3}, ab = \frac{1}{3}$	Both $a + b = \frac{5}{3}$ and $ab = \frac{1}{3}$, seen or implied	B1
	$\frac{a}{b} + \frac{b}{a} = \frac{a^2 + b^2}{ab} = \dots$	Attempts to substitute at least one of their $(a^2 + b^2)$ or their ab into $\frac{a^2 + b^2}{ab}$	M1
	$a^2 + b^2 = (a + b)^2 - 2ab = \dots$	Use of a correct identity for $a^2 + b^2$ (May be implied by their work)	M1
	$\frac{a}{b} + \frac{b}{a} = \frac{\left(\frac{5}{3}\right)^2 - 2\left(\frac{1}{3}\right)}{\left(\frac{1}{3}\right)} = \frac{19}{9} = \frac{19}{3}$	dependent on ALL previous marks being awarded $\frac{19}{3}$ or $\frac{57}{9}$ or $6\frac{1}{3}$ or 6.3 o.e. from correct working	A1 cso
			(4)
			4
Question 1 Notes			
1.	Note	Finding $a + b = \frac{5}{3}, ab = \frac{1}{3}$ by writing down $a, b = \frac{5 + \sqrt{13}}{6}, \frac{5 - \sqrt{13}}{6}$ or by applying $a + b = \left(\frac{5 + \sqrt{13}}{6}\right) + \left(\frac{5 - \sqrt{13}}{6}\right) = \frac{5}{3}$ and $ab = \left(\frac{5 + \sqrt{13}}{6}\right)\left(\frac{5 - \sqrt{13}}{6}\right) = \frac{1}{3}$ scores B0.	
	Note	Those candidates who then apply $a + b = \frac{5}{3}, ab = \frac{1}{3}$ having written down/applied $a, b = \frac{5 + \sqrt{13}}{6}, \frac{5 - \sqrt{13}}{6}$ in part (a) can only score the M marks.	
	Note	Give M0M0A0 for $\frac{a}{b} + \frac{b}{a} = \frac{\left(\frac{5 + \sqrt{13}}{6}\right)}{\left(\frac{5 - \sqrt{13}}{6}\right)} + \frac{\left(\frac{5 - \sqrt{13}}{6}\right)}{\left(\frac{5 + \sqrt{13}}{6}\right)} = \frac{19}{3}$	
	Note	Give M0M0A0 for $\frac{a}{b} + \frac{b}{a} = \frac{a^2 + b^2}{ab} = \frac{\left(\frac{5 + \sqrt{13}}{6}\right)^2 + \left(\frac{5 - \sqrt{13}}{6}\right)^2}{\left(\frac{5 + \sqrt{13}}{6}\right)\left(\frac{5 - \sqrt{13}}{6}\right)} = \frac{19}{3}$	
	Note	Give M0M0A0 for $\frac{a}{b} + \frac{b}{a} = \frac{(a + b)^2 - 2ab}{ab} = \frac{\left(\left(\frac{5 + \sqrt{13}}{6}\right) + \left(\frac{5 - \sqrt{13}}{6}\right)\right)^2 - 2\left(\frac{5 + \sqrt{13}}{6}\right)\left(\frac{5 - \sqrt{13}}{6}\right)}{\left(\frac{5 + \sqrt{13}}{6}\right)\left(\frac{5 - \sqrt{13}}{6}\right)} = \frac{19}{3}$	
	Note	Allow B1 for both $S = \frac{5}{3}$ and $P = \frac{1}{3}$ or for $\hat{a} = \frac{5}{3}$ and $\tilde{O} = \frac{1}{3}$	
	Note	Give final A0 for 6.3 or 6.33 without reference to $\frac{19}{3}$ or $\frac{57}{9}$ or $6\frac{1}{3}$	

Question Number	Scheme		Notes	Marks
2. (a)	$\mathbf{AB} = \begin{pmatrix} 3 & 1 & -2 \\ -1 & 0 & 5 \end{pmatrix} \begin{pmatrix} 2 & 4 \\ -k & 2k \\ 3 & 0 \end{pmatrix}$			
	$= \begin{pmatrix} 6 - k - 6 & 12 + 2k - 0 \\ -2 + 0 + 15 & -4 + 0 + 0 \end{pmatrix}$		Obtains a 2×2 matrix consisting of 4 elements with at least two correct elements which can be simplified or un-simplified	M1
			Correct <i>un-simplified</i> matrix for AB	A1
	$= \begin{pmatrix} -k & 12 + 2k \\ 13 & -4 \end{pmatrix}$			(2)
(b)	$\{\det(\mathbf{AB}) = 0 \Rightarrow \}$			
	$(-k)(-4) - 13(12 + 2k) = 0$ $\Rightarrow 4k - 156 - 26k = 0$ $\Rightarrow -22k = 156$ $\Rightarrow k = -\frac{156}{22} \text{ or } -\frac{78}{11} \text{ or } -7\frac{1}{11}$		Applies " $ad - bc$ " = 0 on their 2×2 matrix for AB and solves the resulting equation to give $k = \dots$	M1
			$k = -\frac{156}{22} \text{ or } -\frac{78}{11} \text{ or } -7\frac{1}{11}$ Accept any exact equivalent form for k Condone - 7.09	A1
				(2)
			4	
	Question 2 Notes			
2. (a)	Note	Give A1 (ignore subsequent working) for a correct un-simplified answer which is later followed by an incorrect simplified answer.		
(b)	Note	Give M1A1 for sight of the correct answer in part (b).		
	Note	Condone the sign error in applying $\dots - 13(12 + 2k) = 0$ to give $\dots - 156 + 26k = 0$ (o.e.) E.g. Allow M1 for $\begin{vmatrix} -k & 12 + 2k \\ 13 & -4 \end{vmatrix} = 0 \Rightarrow 4k - 156 + 26k = 0 \Rightarrow k = \dots$		
	Note	Give final A0 for -7.0 or -7.1 or -7.09 without reference to $-\frac{156}{22}$ or $-\frac{78}{11}$ or $-7\frac{1}{11}$		

Question Number	Scheme	Notes	Marks
3.	Required to prove by induction the result $\sum_{r=1}^n \frac{2}{r(r+1)(r+2)} = \frac{1}{2} - \frac{1}{(n+1)(n+2)}, n \in \mathbb{N}$		
Way 1	$n = 1$: LHS = $\frac{1}{3}$, RHS = $\frac{1}{2} - \frac{1}{(2)(3)} = \frac{1}{3}$	Shows or states LHS = $\frac{1}{3}$ and shows either RHS = $\frac{1}{2} - \frac{1}{(1+1)(2+1)} = \frac{1}{3}$ or RHS = $\frac{1}{2} - \frac{1}{(2)(3)} = \frac{1}{3}$ or RHS = $\frac{1}{2} - \frac{1}{6} = \frac{1}{3}$	B1
	(Assume the result is true for $n = k$)		
	$\sum_{r=1}^{k+1} \frac{2}{r(r+1)(r+2)} = \frac{1}{2} - \frac{1}{(k+1)(k+2)} + \frac{2}{(k+1)(k+1+1)(k+1+2)}$	Adds the $(k+1)^{\text{th}}$ term to the sum of k terms	M1
	$= \frac{1}{2} - \frac{1}{(k+1)(k+2)} + \frac{2}{(k+1)(k+2)(k+3)}$		
	$= \frac{1}{2} - \frac{(k+3)}{(k+1)(k+2)(k+3)} + \frac{2}{(k+1)(k+2)(k+3)}$ or $= \frac{1}{2} - \left(\frac{(k+3) - 2}{(k+1)(k+2)(k+3)} \right)$	dependent on the previous M mark Makes $(k+1)(k+2)(k+3)$ a common denominator for their second and third fractions	dM1
	$= \frac{1}{2} - \frac{1}{(k+2)(k+3)}$	Obtains $\frac{1}{2} - \frac{1}{(k+2)(k+3)}$ or $\frac{1}{2} - \frac{1}{(k+1+1)(k+1+2)}$ by correct solution only	A1
	If the result is <u>true for $n = k$</u> , then it is <u>true for $n = k + 1$</u> . As the result has been shown to be <u>true for $n = 1$</u> , then the result is <u>true for all n</u> ($n \in \mathbb{N}$)		A1 cso
Final A1 is dependent on all previous marks being scored in that part. It is gained by candidates conveying the ideas of all four underlined points either at the end of their solution or as a narrative in their solution.		(5)	
			5
Way 2	The M1dM1A1 marks for Alternative Way 2		
	$\sum_{r=1}^{k+1} \frac{2}{r(r+1)(r+2)} = \frac{1}{2} - \frac{1}{(k+1)(k+2)} + \frac{2}{(k+1)(k+1+1)(k+1+2)}$	Adds the $(k+1)^{\text{th}}$ term to the sum of k terms	M1
	$= \frac{(k+1)(k+2)(k+3) - 2(k+3) + 2(2)}{2(k+1)(k+2)(k+3)}$	dependent on the previous M mark Makes $2(k+1)(k+2)(k+3)$ a common denominator for their three fractions	dM1
	$= \frac{k^3 + 6k^2 + 9k + 4}{2(k+1)(k+2)(k+3)} = \frac{(k+1)(k^2 + 5k + 4)}{2(k+1)(k+2)(k+3)} = \frac{k^2 + 5k + 4}{2(k+2)(k+3)} = \frac{(k+2)(k+3) - 2}{2(k+2)(k+3)}$		
	$= \frac{1}{2} - \frac{1}{(k+2)(k+3)}$	Obtains $\frac{1}{2} - \frac{1}{(k+2)(k+3)}$ or $\frac{1}{2} - \frac{1}{(k+1+1)(k+1+2)}$ by correct solution only	A1

		Question 3 Notes		
3.	Note	LHS = RHS by itself or $\text{LHS} = \text{RHS} = \frac{1}{3}$ is not sufficient for the 1 st B1 mark.		
	Note Way 2	The 1 st A1 can be obtained by e.g. using algebra to show that $\sum_{r=1}^{k+1} \frac{2}{r(r+1)(r+2)}$ gives $\frac{(k^2+5k+4)}{2(k+2)(k+3)}$ and by using algebra to show that $\frac{1}{2} - \frac{1}{(k+2)(k+3)}$ also gives $\frac{(k^2+5k+4)}{2(k+2)(k+3)}$		
	Note	Moving from $\frac{1}{2} - \frac{1}{(k+1)(k+2)} + \frac{2}{(k+1)(k+2)(k+3)}$ to $\frac{1}{2} - \frac{1}{(k+2)(k+3)}$ <i>with no intermediate working</i> is 2 nd M0 1 st A0 2 nd A0.		
Way 3	The M1dM1A1 marks for Alternative Way 3			
	$\sum_{r=1}^{k+1} \frac{2}{r(r+1)(r+2)} = \frac{1}{2} - \frac{1}{(k+1)(k+2)} + \frac{2}{(k+1)(k+1+1)(k+1+2)}$		Adds the $(k+1)^{\text{th}}$ term to the sum of k terms	M1
	$= \frac{1}{2} - \frac{1}{(k+1)(k+2)} + \frac{1}{(k+1)(k+2)} - \frac{1}{(k+2)(k+3)}$		dependent on the previous M mark This step must be seen in Way 3	dM1
	$= \frac{1}{2} - \frac{1}{(k+2)(k+3)}$	Obtains $\frac{1}{2} - \frac{1}{(k+2)(k+3)}$ or $\frac{1}{2} - \frac{1}{(k+1+1)(k+1+2)}$ by correct solution only		A1

Question Number	Scheme		Notes	Marks
4. (a) Way 1	$\left\{x = 4t, y = \frac{4}{t} \Rightarrow\right\} 3\left(\frac{4}{t}\right) - 2(4t) = 10$		Substitutes $x = 4t$ and $y = \frac{4}{t}$ into the printed equation to obtain an equation in t only	M1
	$8t^2 + 10t - 12 = 0$ or $4t^2 + 5t - 6 = 0$ (can be implied)		A correct 3 term quadratic Note: E.g. $12 - 8t^2 = 10t$, $8t^2 + 10t - 12 \{= 0\}$ or $8t^2 + 10t = 12$ are acceptable for this mark	A1
	$(8t - 6)(t + 2) = 0 \Rightarrow t = \dots$ or $(4t - 3)(2t + 4) = 0 \Rightarrow t = \dots$ or $(4t - 3)(t + 2) = 0 \Rightarrow t = \dots$		dependent on the previous M mark Correct method (e.g. factorising, completing the square or applying the quadratic formula) of solving a 3TQ to find $t = \dots$	dM1
	<ul style="list-style-type: none"> $x = 4\left(\frac{3}{4}\right) = 3$ and $y = \frac{4}{\left(\frac{3}{4}\right)} = \frac{16}{3}$ $x = 4(-2) = -8$ and $y = \frac{4}{(-2)} = -2$ 		dependent on both the previous M marks Correct substitution at least one of their values for t into the given parametric equations and obtains two sets of corresponding values for $x = \dots$ and $y = \dots$	ddM1
	$A\left(3, \frac{16}{3}\right), B(-8, -2)$ or $A: x = 3, y = \frac{16}{3}$ and $B: x = -8, y = -2$		Identifies the correct coordinates for A and B	A1 cao
				(5)
(a) Way 2	$x\left(\frac{10+2x}{3}\right) = 16$	$\left(\frac{3y-10}{2}\right)y = 16$	Either substitutes their rearranged $3y - 2x = 10$ into $xy = k$ or substitutes either $y = \frac{k}{x}$ or $x = \frac{k}{y}$, $k \neq 0$, into $3y - 2x = 10$ to form an equation in either x only or y only	M1
	$3\left(\frac{16}{x}\right) - 2x = 10$	$3y - 2\left(\frac{16}{y}\right) = 10$		
	$2x^2 + 10x - 48 = 0$ or $x^2 + 5x - 24 = 0$ or $\frac{2}{3}x^2 + \frac{10}{3}x - 16 = 0$ or $\frac{3}{2}y^2 - 5y - 16 = 0$ or $3y^2 - 10y - 32 = 0$ (can be implied)		A correct 3 term quadratic Note: $10x + 2x^2 = 48$, $3y^2 - 10y = 32$ or $x^2 + 5x - 24 \{= 0\}$ are acceptable for this mark	A1
	e.g. $(2x + 16)(x - 3) = 0 \Rightarrow x = \dots$ or $(x + 8)(x - 3) = 0 \Rightarrow x = \dots$ or $(3y - 16)(y + 2) = 0 \Rightarrow y = \dots$		dependent on the previous M mark Correct method (e.g. factorising, completing the square or applying the quadratic formula) of solving a 3TQ to find either $x = \dots$ or $y = \dots$	dM1
	E.g. $x = 3 \Rightarrow y = \frac{16}{3}$ $x = -8 \Rightarrow y = \frac{16}{-8} = -2$	dependent on both the previous M marks. Correct substitution of at least one of their values for x or y into either $3y - 2x = 10$ or their rearranged $3y - 2x = 10$ or $y = \frac{k}{x}$ or $x = \frac{k}{y}$, $k \neq 0$, and obtains two sets of corresponding values for $x = \dots$ and $y = \dots$		ddM1
	$A\left(3, \frac{16}{3}\right), B(-8, -2)$ or $A: x = 3, y = \frac{16}{3}$ and $B: x = -8, y = -2$		Identifies the correct coordinates for A and B	A1 cao
				(5)
(b)	$\left(\frac{3 + (-8)}{2}, \frac{\frac{16}{3} + (-2)}{2}\right); = \left(-\frac{5}{2}, \frac{5}{3}\right)$		Uses their (x_1, y_1) and (x_2, y_2) from part (a) to apply $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$ o.e.	M1;
			Correct answer	A1
				(2)
				7

Question 4 Notes		
4. (a)	SC	If the two previous M marks have been gained then award Special Case ddM1 for finding their correct points by writing either $x = 3, y = \frac{16}{3}$ or $x = -8, y = -2$ or $\left(3, \frac{16}{3}\right)$ or $(-8, -2)$
	Note	A decimal answer of e.g. $A(3, 5.33), B(-8, -2)$ (without a correct exact answer) is 2 nd A0
	Note	<u>Writing coordinates the wrong way round</u> E.g. writing $x = 3, y = \frac{16}{3}$ and $x = -8, y = -2$ followed by $A\left(\frac{16}{3}, 3\right), B(-8, -2)$ is 2 nd A0
	Note	Imply the dM1 mark for writing down the correct roots for their quadratic equation. E.g. <ul style="list-style-type: none"> $2x^2 + 10x - 48 = 0$ or $x^2 + 5x - 24 = 0$ or $\frac{2}{3}x^2 + \frac{10}{3}x = 16 \rightarrow x = 3, -8$ $\frac{3}{2}y^2 - 5y - 16 = 0$ or $3y^2 - 10y - 32 = 0 \rightarrow y = \frac{16}{3}, -2$ $8t^2 + 10t = 12$ or $4t^2 + 5t - 6 = 0 \rightarrow t = \frac{3}{4}, -2$
	Note	For example, give dM0 for <ul style="list-style-type: none"> $8t^2 + 10t = 12$ or $4t^2 + 5t - 6 = 0 \rightarrow t = \frac{1}{4}, -2$ [incorrect solution] with no intermediate working.
	Note	You can also imply the 1 st A1 dM1 marks for either <ul style="list-style-type: none"> $x\left(\frac{10+2x}{3}\right) = 16$ or $3\left(\frac{16}{x}\right) - 2x = 10 \rightarrow x = 3, -8$ $\left(\frac{3y-10}{2}\right)y = 16$ or $3y - 2\left(\frac{16}{y}\right) = 10 \rightarrow y = \frac{16}{3}, -2$ $3\left(\frac{4}{t}\right) - 2(4t) = 10 \rightarrow x = 3, -8$ $3\left(\frac{4}{t}\right) - 2(4t) = 10 \rightarrow y = \frac{16}{3}, -2$ with no intermediate working.
(b)	Note	You can imply the 1 st A1 dM1 ddM1 marks for either <ul style="list-style-type: none"> $x\left(\frac{10+2x}{3}\right) = 16$ or $3\left(\frac{16}{x}\right) - 2x = 10 \rightarrow x = 3, -8$ and $y = \frac{16}{3}, -2$ $3\left(\frac{4}{t}\right) - 2(4t) = 10 \rightarrow x = 3, -8$ and $y = \frac{16}{3}, -2$ with no intermediate working. You can then imply the final A1 mark if they correctly identify the correct pairs of values or coordinates which relate to the point A and the point B.
	Note	Give 2 nd A0 for a final answer of both $A\left(3, \frac{16}{3}\right), B(-8, -2)$ and $A(-8, -2), B\left(3, \frac{16}{3}\right)$,
	Note	Allow A1 for $\left(-\frac{5}{2}, \frac{10}{6}\right)$ or $\left(-2\frac{1}{2}, -1\frac{2}{3}\right)$ or exact equivalent.

Question Number	Scheme		Notes				Marks
5.	Given $f(x) = 30 - \frac{7}{\sqrt{x}} - x^5$, $x > 0$ and root of $f(x) = 0$ lies in the interval $[2, 2.1]$						
(a) Way 1	f(2) = 2.9497... or f(2.1) = - 6.0105...		Attempts to evaluate at least one of f(2) or f(2.1) and evaluates f(2.05)				M1
	f(2.05) = - 1.3160...		f(2) or f(2.1) correct awrt (or truncated) to 1 sf and f(2.05) correct awrt (or truncated) to 1 sf				A1
	f(2.025) = ...		dependent on the previous M mark Evaluates f(2.025) (and not f(2.075))				dM1
	f(2.025) = 0.86846... so interval is (2.025, 2.05) or (2.025, 2.050)	f(2.025) correct awrt (or truncated) to 1 sf and correct interval. Allow $2.025 \leq x \leq 2.05$ or $2.025 < x < 2.05$ or $2.025 \leq a \leq 2.05$ or $2.025 < a < 2.05$ or $[2.025, 2.05]$ or $(2.025, 2.05)$ equivalent in words. Condone 2.025 - 2.05 Allow a mixture of “ends”. Do not allow incorrect statements such as $2.05 < a < 2.025$ or (2.05, 2.025) or 2.05 - 2.025 unless they are recovered. Ignore the subsequent iteration of f(2.0375)					A1
	Note that some candidates only indicate the sign of f and not its value. In this case the M marks can still score as defined but not the A marks.						(4)
(a) Way 2	Common approach in the form of a table (use the mark scheme above)						
	a	f(a)	b	f(b)	$\frac{a+b}{2}$	$f\left(\frac{a+b}{2}\right)$	
	2	2.9497...	2.1	- 6.0105...	2.05	-1.3160...	
	2	2.9497...	2.05	-1.3160...	2.025	0.86846...	
	so interval is $2.025 < a < 2.05$ would score full marks in part (a)						
(b)	$f'(x) = -\frac{7}{2}x^{-\frac{3}{2}} - 5x^4$		At least one of either $-\frac{7}{\sqrt{x}} \rightarrow \pm Ax^{-\frac{3}{2}}$ or $-x^5 \rightarrow \pm Bx^4$ where A and B are non-zero constants.				M1
			At least one of either $-\frac{7}{2}x^{-\frac{3}{2}}$ or $-5x^4$ simplified or un-simplified				A1
			Correct differentiation simplified or un-simplified				A1
	$\left\{ \alpha \approx 2 - \frac{f(2)}{f'(2)} \right\} \Rightarrow \alpha \approx 2 - \frac{2.949747468...}{-81.23743687...}$			dependent on the previous M mark Valid attempt at Newton-Raphson using their values of f(2) and f'(2)		dM1	
	$\{a = 2.036310199...\} \supset a = 2.04$ (2 dp)			dependent on all 4 previous marks 2.04 on their first iteration (Ignore any subsequent iterations)		A1 cso cao	
	Correct differentiation followed by a correct answer of 2.04 scores full marks in part (b) Correct answer with no working scores no marks in part (b)						(5)
							9
	Question 5 Notes						
5. (a)	Note	Give 2 nd M0 for evaluating both f(2.025) and f(2.075)					
	Note	Do not allow “interval = f(2.025) to f(2.05)” unless recovered.					
	Note	A method of evaluating f(2.05) followed by f(2.025) with no evidence of evaluating at least one of either f(2) or f(2.1) is M0A0M0A0					

Question 5 Notes Continued		
5. (b)	Note	Incorrect differentiation followed by their estimate of α with no evidence of applying the NR formula is final dM0A0.
	Final dM1	This mark can be implied by applying at least one correct <i>value</i> of either $f(2)$ or $f'(2)$ in $2 - \frac{f(2)}{f'(2)}$. So just $2 - \frac{f(2)}{f'(2)}$ with an incorrect answer and no other evidence scores final dM0A0.
	Note	<p>You can imply the M1A1A1 marks for algebraic differentiation for either</p> <ul style="list-style-type: none"> $f'(2) = -\frac{7}{2}(2)^{-\frac{3}{2}} - 5(2)^4$ $f'(2)$ applied correctly in $\alpha \approx 2 - \frac{30 - 7(2)^{-\frac{1}{2}} - (2)^5}{-\frac{7}{2}(2)^{-\frac{3}{2}} - 5(2)^4}$
	Note	<p>Differentiating INCORRECTLY to give $f'(x) = -\frac{7}{2}x^{-2} - 5x^4$ leads to</p> $\alpha \approx 2 - \frac{2.949747468...}{-81.75} = 2.036082538... = 2.04 \text{ (2 dp)}$ <p>This response should be awarded M1A1A0M1A0</p>

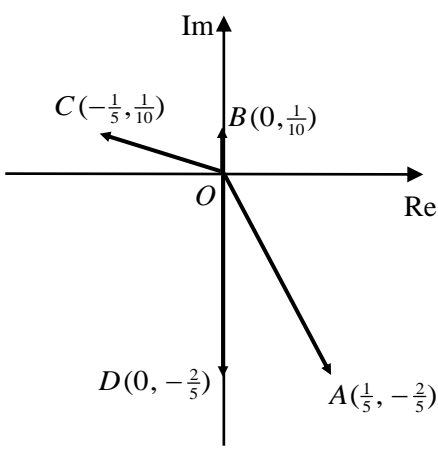
Question Number	Scheme	Notes	Marks
6. (a)	$\sum_{r=1}^n r^2(r+1) = \sum_{r=1}^n r^3 + \sum_{r=1}^n r^2$	{ Note: Let $f(n) = \frac{1}{12}n(n+1)(n+2)(3n+1)$ or their answer to part (a).}	
	$= \frac{1}{4}n^2(n+1)^2 + \frac{1}{6}n(n+1)(2n+1)$	Attempts to expand $r^2(r+1)$ and attempts to substitute at least one correct standard formula into their resulting expression.	M1
		Correct expression (or equivalent)	A1
	$= \frac{1}{12}n(n+1)[3n(n+1) + 2(2n+1)]$	dependent on the previous M mark Attempt to factorise at least $n(n+1)$ having attempted to substitute both standard formulae.	dM1
	$= \frac{1}{12}n(n+1)[3n^2 + 7n + 2]$	{this step does not have to be written}	
	$= \frac{1}{12}n(n+1)(n+2)(3n+1)$	Correct completion with no errors. Note: $a = 12, b = 1$	A1 cso
			(4)
(b) Way 1	$\left\{ \sum_{r=25}^{49} r^2(r+1) \right\}$	Attempts to find either $f(49) - f(24)$ or $f(49) - f(25)$. This mark can be implied.	M1
	$= \left(\frac{1}{12}(49)(50)(51)(148) \right) - \left(\frac{1}{12}(24)(25)(26)(73) \right)$ $\{ = 1541050 - 94900 = 1446150 \}$	Correct numerical expression for $f(49) - f(24)$ which can be simplified or un-simplified. Note: This mark can be implied by seeing 1446150	A1
	$\left\{ \sum_{r=25}^{49} (r^2(r+1) + 2) \right\}$ $= "1446150" + 25(2); = 1446200$	Adds 25(2) or equivalent to their $\sum_{r=25}^{49} r^2(r+1)$ or clear evidence that $\sum_{r=25}^{49} 2 = 2(49) - 2(24)$ or 50	M1
		1446200	A1 cao
			(4)
(b) Way 2	$\left\{ \sum_{r=25}^{49} (r^2(r+1) + 2) \right\} = \left(\frac{1}{12}(49)(50)(51)(148) + \underline{2(49)} \right) - \left(\frac{1}{12}(24)(25)(26)(73) + \underline{2(24)} \right)$ $= (\underline{1541050} + \underline{98}) - (\underline{94900} + \underline{48}) = 1541148 - 94948 = 1446200$		
		Attempts to find either $f(49) - f(24)$ or $f(49) - f(25)$	M1
	Correct numerical expression for $f(49) - f(24)$ which can be simplified or un-simplified. Note: This mark can be implied by $(\underline{1541050} + \underline{\dots}) - (\underline{94900} + \underline{\dots})$ or $1541148 - 94948$		A1
	Adds 50 or equivalent to their $\sum_{r=25}^{49} r^2(r+1)$ or clear evidence that $\sum_{r=25}^{49} 2 = 2(49) - 2(24)$ or 50 Note: This mark can be implied by $(\underline{\dots} + \underline{2(49)}) - (\underline{\dots} + \underline{2(24)})$ or $1541148 - 94948$		M1
		1446200	A1 cao
			(4)
			8

Question Number	Scheme	Notes	Marks
6. (b) Way 3	$\left\{ \sum_{r=25}^{49} (r^2(r+1) + 2) \right\} = \sum_{r=25}^{49} r^3 + \sum_{r=25}^{49} r^2 + \sum_{r=25}^{49} 2$ $= \left(\frac{1}{4}(49)^2(50)^2 - \frac{1}{4}(24)^2(25)^2 \right) + \left(\frac{1}{6}(49)(50)(99) - \frac{1}{6}(24)(25)(49) \right) + (98 - 48)$ $= (1500625 - 90000) + (40425 - 4900) + 50 = 1410625 + 35525 + 50 = 1446200$ or $\overset{49}{\underset{r=25}{\circlearrowleft}} (r^3 + r^2 + 2)$ $= \left(\frac{1}{4}(49)^2(50)^2 + \frac{1}{6}(49)(50)(99) + 2(49) \right) - \left(\frac{1}{4}(24)^2(25)^2 + \frac{1}{6}(24)(25)(49) + 2(24) \right)$ $= (1500625 + 40425 + 98) - (90000 + 4900 + 48) = 1541148 - 94948 = 1446200$		
	Attempts to find either $\overset{49}{\underset{r=25}{\circlearrowleft}} f(49) - f(24)$ or $\overset{49}{\underset{r=25}{\circlearrowleft}} f(49) - f(25)$		M1
	Correct numerical expression for $f(49) - f(24)$ which can be simplified or un-simplified.		A1
	Adds 50 or equivalent to their $\overset{49}{\underset{r=25}{\circlearrowleft}} r^2(r+1)$ or clear evidence that $\overset{49}{\underset{r=25}{\circlearrowleft}} 2 = 2(49) - 2(24)$ or 50		M1
	1446200		A1 cao
			(4)
Question 6 Notes			
6. (a)	Note	Applying e.g. $n = 1, n = 2$ to the printed equation without applying the standard formulae to give $a = 12, b = 1$ is M0A0M0A0	
	Alt 1 dM1 A1 cso	Alt Method 1: Using $\frac{1}{4}n^4 + \frac{5}{6}n^3 + \frac{3}{4}n^2 + \frac{1}{6}n \circ \frac{3}{a}n^4 + \frac{(9+b)}{a}n^3 + \frac{(6+3b)}{a}n^2 + \frac{2b}{a}n$ o.e. Equating coefficients to find both $a = \dots$ and $b = \dots$ and at least one of $a = 12, b = 1$ Finds $a = 12, b = 1$ and demonstrates the identity works for all of its terms.	
	Alt 2 dM1 A1	Alt Method 2: $\frac{1}{4}n^2(n+1)^2 + \frac{1}{6}n(n+1)(2n+1) \circ \frac{1}{a}n(n+1)(n+2)(3n+b)$ Substitutes $n = 1, n = 2$, into this identity o.e. to find both $a = \dots$ and $b = \dots$ and at least one of $a = 12, b = 1$ Finds $a = 12, b = 1$	
	Note	Allow final dM1A1 for $\frac{1}{4}n^4 + \frac{5}{6}n^3 + \frac{3}{4}n^2 + \frac{1}{6}n$ or $\frac{1}{12}n(3n^3 + 10n^2 + 9n + 2)$ or $\frac{1}{12}(3n^4 + 10n^3 + 9n^2 + 2n) \rightarrow \frac{1}{12}n(n+1)(n+2)(3n+1)$ from no incorrect working.	

Question 6 Notes Continued		
6. (b)	Note	Give 1 st M1 1 st A0 for applying $f(49) - f(25)$. i.e. $1541050 - 111150 \{ = 1429900 \}$
	Note	You cannot follow through their incorrect answer from part (a) for the 1 st A1 mark.
	Note	Give M1A0M1A0 for applying $[f(49) + 2(49)] - [f(25) + 2(24)]$ i.e. $1541148 - 111198 \{ = 1429950 \}$
	Note	Give M1A0M0A0 for applying $[f(49) + 2(49)] - [f(25) + 2(25)]$ i.e. $1541148 - 111200 \{ = 1429948 \}$
	Note	Give 1 st M0 1 st A0 for applying $(49)^2(50) - (24)^2(25) = 120050 - 14400 = 105650$
	Note	Give 1 st M0 1 st A0 for applying $(49)^2(50) - (25)^2(26) = 120050 - 16250 = 103800$
	Note	Give M0A0M0A0 for listing individual terms. e.g. $16250 + 18252 + \dots + 112896 + 120050 = 1446200$
	Note	Give 2 nd M0 for lack of bracketing in $\frac{1}{12}(49)(50)(51)(148) + 2(49) - \frac{1}{12}(24)(25)(26)(73) + 2(24)$ unless recovered
	Note	Give M0A0M0A0 for writing down 1446200 without any working.
	Note	Applying $f(49) - f(24)$ for $\frac{1}{4}n(n+1)(n+2)(3n+1)$ is $4623150 - 284\,700 = 4338450$ is 1 st M1 1 st A0

Question Number	Scheme	Notes	Marks
7.	$f(z) = z^4 + 4z^3 + 6z^2 + 4z + a$, a is a real constant. $z_1 = 1 + 2i$ satisfies $f(z) = 0$		
(a)	$\{z_2 = \} 1 - 2i$	$1 - 2i$	B1
			(1)
(b)(i)	$z^2 - 2z + 5$	Attempt to expand $(z - (1 + 2i))(z - (1 - 2i))$ or $(z - (1 + 2i))(z - (\text{their complex } z_2))$ or any valid method <i>to establish a quadratic factor</i> e.g. $z = 1 \pm 2i \Rightarrow z - 1 = \pm 2i \Rightarrow z^2 - 2z + 1 = -4$ or sum of roots 2, product of roots 5 to give $z^2 \pm (\text{their sum})z + (\text{their product})$	M1
		$z^2 - 2z + 5$	A1
	$f(x) = (z^2 - 2z + 5)(z^2 + 6z + 13)$	Attempts to find the other quadratic factor. e.g. using long division to obtain either $z^2 \pm kz + \dots$, $k \neq 0$ or $z^2 \pm az + b$, $b \neq 0$, a can be 0 or factorising e.g. $f(z) = (z^2 - 2z + 5)(z^2 \pm kz \pm c)$, $k \neq 0$ or $f(z) = (z^2 - 2z + 5)(z^2 \pm az \pm b)$, $b \neq 0$, a can be 0	M1
		$z^2 + 6z + 13$	A1
	$\{z^2 + 6z + 13 = 0 \Rightarrow\}$		
	Either <ul style="list-style-type: none"> $z = \frac{-6 \pm \sqrt{36 - 4(1)(13)}}{2(1)}$ $(z + 3)^2 - 9 + 13 = 0 \Rightarrow z = \dots$ 	dependent on only the previous M mark Correct method of applying the quadratic formula or completing the square for solving a 3TQ on their 2 nd quadratic factor	dM1
	$\{z = \} -3 + 2i, -3 - 2i$	$-3 + 2i$ and $-3 - 2i$	A1
			(6)
(ii)	$\{a = \} 65$	65 or $a = 65$ stated anywhere in (b)	B1
			(1)
			8
Question 7 Notes			
7. (b)(i)	Note	No working leading to $x = -3 + 2i, -3 - 2i$ is M0A0M0A0M0A0.	
	Note	You can assume $x \propto z$ for solutions in this question.	
	Note	Give dM1A1 for $z^2 + 6z + 13 = 0 \Rightarrow z = -3 + 2i, -3 - 2i$ with no intermediate working.	
	Note	Special Case: If their second 3 term quadratic factor can be factorised then give Special Case dM1 for correct factorisation leading to $z = \dots$	
	Note	Otherwise, give 3 rd dM0 for applying a method of factorising to solve their 3TQ.	
	Note	Reminder: Method Mark for solving a 3TQ, " $az^2 + bz + c = 0$ " Formula: Attempt to use the correct formula (with values for a, b and c) Completing the square $\left(z \pm \frac{b}{2}\right)^2 \pm q \pm c = 0, q \neq 0$, leading to $z = \dots$	

Question Number	Scheme	Notes	Marks
8.	$C: y^2 = 36x$, $P(9p^2, 18p)$ lies on C , where p is a constant.		
(a)	$y = 6x^{\frac{1}{2}} \Rightarrow \frac{dy}{dx} = \frac{1}{2}(6)x^{-\frac{1}{2}} = \frac{3}{\sqrt{x}}$	$\frac{dy}{dx} = \pm kx^{-\frac{1}{2}}$	M1
	$y^2 = 36x \Rightarrow 2y \frac{dy}{dx} = 36$	$py \frac{dy}{dx} = q$	
	$\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = 18\left(\frac{1}{18p}\right)$	their $\frac{dy}{dt} \cdot \frac{1}{\text{their } \frac{dx}{dt}}$	
	So at P , $m_T = \frac{1}{p}$	Correct calculus work leading to $m_T = \frac{1}{p}$	A1
	$y - 18p = \frac{1}{p}(x - 9p^2)$ or $y = \frac{1}{p}x + 9p$	Correct straight line method for an equation of a tangent where $m_T \left(\text{or } m_N \right)$ is found by using calculus. Note: m_T must be a function of p	M1
	leading to $py - x = 9p^2$ (*)	Correct solution only	A1 *
(b)	(Directrix: $x = -9 \Rightarrow a = 9$)	$a = 9$ or $a = 9$ stated anywhere in this question	B1
			(1)
(c)	Tangent goes through $(-a, 6) \Rightarrow$		
	$6p + 9 = 9p^2$	Substitutes their value $x = -"a"$ or their value $x = "a"$ and $y = 6$ into either $py - x = 9p^2$ or $py - x = -9p^2$	M1
	$9p^2 - 6p - 9 = 0$ or $3p^2 - 2p - 3 = 0$		
	E.g. $p = \frac{6 \pm \sqrt{36 - 4(9)(-9)}}{2(9)}$	dependent on the previous M mark Correct method of solving their 3TQ	dM1
	{as $p > 0$ } $p = \frac{1 + \sqrt{10}}{3}$	$p = \frac{1 + \sqrt{10}}{3}$ or $\frac{6 + \sqrt{360}}{18}$ or $\frac{6 + 6\sqrt{10}}{18}$ etc.	A1
	Note: Give A0 for giving two values for p as their answer to part (c)		(3)
(d)	$x = 9\left(\frac{1 + \sqrt{10}}{3}\right)^2$, $y = 18\left(\frac{1 + \sqrt{10}}{3}\right)$	Uses a real value of p , which is the result of substituting $(\pm a, 6)$ into $py - x = \pm 9p^2$, and substitutes p into at least one of either $x = 9p^2$ or $y = 18p$	M1
	$(11 + 2\sqrt{10}, 6 + 6\sqrt{10})$ or $(11 + 2\sqrt{10}, 6(1 + \sqrt{10}))$	Either $x = 11 + 2\sqrt{10}$ or $y = 6 + 6\sqrt{10}$ or $y = 6(1 + \sqrt{10})$	A1
		Correct coordinates of P . Condone $x = \dots, y = \dots$	A1
	Note: Give 2 nd A0 for two sets of coordinates for P		(3)
			11

Question Number	Scheme			Notes	Marks	
9. (a)	$\left\{ z = \right\} \sqrt{\left(\frac{1}{5}\right)^2 + \left(-\frac{2}{5}\right)^2}; = \frac{\sqrt{5}}{5} \text{ or } \frac{1}{\sqrt{5}} \text{ or } \sqrt{\frac{1}{5}}$			$\sqrt{\left(\frac{1}{5}\right)^2 + \left(-\frac{2}{5}\right)^2} \text{ or } \sqrt{\left(\frac{1}{5}\right)^2 + \left(\frac{2}{5}\right)^2}$ which can be implied.	M1	
				Correct exact answer	A1	
	$\left\{ \arg z = \arctan(-2) = -1.107148718... \right\} = -1.11 \text{ (2 dp)}$		-1.11 cao or 5.18 cao	B1		
					(3)	
(b) Way 1	$w = \frac{/i}{z} = \frac{/i}{\left(\frac{1}{5} - \frac{2}{5}i\right)}$	or	$w = \frac{5/i}{5z} = \frac{5/i}{(1 - 2i)}$	Correct method of making w the subject and substituting for z	M1	
	$= \frac{/i\left(\frac{1}{5} + \frac{2}{5}i\right)}{\left(\frac{1}{5} - \frac{2}{5}i\right)\left(\frac{1}{5} + \frac{2}{5}i\right)}$		$= \frac{5/i(1 + 2i)}{(1 - 2i)(1 + 2i)}$	dependent on the previous M mark Multiplies numerator and denominator of right hand side by $\left(\frac{1}{5} + \frac{2}{5}i\right)$ or $(1 + 2i)$ to give an expression in terms of $/$ which contains a real denominator	dM1	
	$= \frac{-\frac{2}{5} + \frac{1}{5}/i}{\frac{1}{25} + \frac{4}{25}}$		$= \frac{-10/ + 5/i}{1 + 4}$			
	$= -2/ + /i$		$= -2/ + /i$	$-2/ + /i$ or $/i - 2/$	A1	
					(3)	
(b) Way 2	$\left(\frac{1}{5} - \frac{2}{5}i\right)(a + bi) = /i \Rightarrow \frac{1}{5}a + \frac{1}{5}bi - \frac{2}{5}ai + \frac{2}{5}b = /i$ $\frac{1}{5}a + \frac{2}{5}b = 0 \text{ or } -\frac{2}{5}a + \frac{1}{5}b = /$			Substitutes z and w into $zw = /i$, expands zw and attempts to equate either the real part of the imaginary part of the resulting equation.	M1	
	$\frac{1}{5}a + \frac{2}{5}b = 0, -\frac{2}{5}a + \frac{1}{5}b = /$ $\Rightarrow a = ... \text{ or } b = ...$		dependent on the previous M mark Obtains an equation in terms of a and b and obtains a second equation in terms of a, b and $/$ and solves them simultaneously to give at least one of $a = ... \text{ or } b = ...$		dM1	
	$\left\{ a = -2/ , b = / \Rightarrow \right\} w = -2/ + /i$			$-2/ + /i$ or $/i - 2/$	A1	
					(3)	
(c)	$\left\{ \frac{4}{3}(z + w) = \right\} \frac{4}{3}\left(\left(\frac{1}{5} - \frac{2}{5}i\right) + \left(-\frac{2}{10} + \frac{1}{10}i\right)\right); = -\frac{2}{5}i$			Substitutes $z, /$ and their w into $\frac{4}{3}(z + w)$	M1	
				$-\frac{2}{5}i$ or $-\frac{6}{15}i$ or $-0.4i$ o.e.	A1	
					(2)	
(d)				Criteria <ul style="list-style-type: none">plots $\left(\frac{1}{5}, -\frac{2}{5}\right)$ in quadrant 4plots $\left(0, \frac{1}{10}\right)$ on the positive imaginary axisplots $\left(-\frac{1}{5}, \frac{1}{10}\right)$ in quadrant 2plots $\left(0, -\frac{2}{5}\right)$ on the negative imaginary axis		
				Satisfies at least two of the four criteria		B1
				Satisfies all four criteria with some indication of scale or coordinates stated. All points (arrows) must be in the correct positions relative to each other.		B1
					10	

	Question 9 Notes	
9. (a)	Note	M1 can be implied by awrt 0.45 or a truncated 0.44
	Note	Give A0 for 0.4472... without reference to $\frac{\sqrt{5}}{5}$ or $\frac{1}{\sqrt{5}}$ or $\sqrt{\frac{1}{5}}$
	Note	Give B0 for -1.11 followed by a final answer of 1.11
(b)	Note	Be aware that $\frac{1}{(\frac{1}{5} - \frac{2}{5}i)} = 1 + 2i$

Question Number	Scheme	Notes	Marks
10. (a)	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$ or $\begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$	Correct matrix which is expressed in exact surds	B1
			(1)
(b)	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	Correct matrix which is expressed in exact surds	B1
			(1)
(c)	$\left\{ \begin{pmatrix} a & b \\ c & d \end{pmatrix} \right\} = \left\{ \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} = \dots \right.$	Multiplies their matrix from part (a) by their matrix from part (b) [either way round] and finds at least one element in the resulting matrix	M1
	$= \begin{pmatrix} \frac{\sqrt{2}-\sqrt{6}}{4} & \frac{-\sqrt{2}-\sqrt{6}}{4} \\ \frac{\sqrt{2}+\sqrt{6}}{4} & \frac{\sqrt{2}-\sqrt{6}}{4} \end{pmatrix}$ or $\begin{pmatrix} \frac{1-\sqrt{3}}{2\sqrt{2}} & \frac{-1-\sqrt{3}}{2\sqrt{2}} \\ \frac{\sqrt{3}+1}{2\sqrt{2}} & \frac{1-\sqrt{3}}{2\sqrt{2}} \end{pmatrix}$	At least 3 correct exact elements	A1
		Correct exact matrix Note: Allow multiplication either way round	A1
			(3)
(d)	Rotation about (0, 0)	Rotation (condone turn) and about (0, 0) or about <i>O</i> or about the origin	B1
	105 degrees (anticlockwise)	105 degrees or $\frac{7\pi}{12}$ (anticlockwise) or 255 degrees clockwise or $\frac{17\pi}{12}$ clockwise	B1 o.e.
	Note: Give 2 nd B0 for 105 degrees clockwise Note: Give B0B0 for combinations of transformations		(2)
(e)	Either	dependent on the 1st A mark in part (c) and states $\sin 75^\circ = \sin 105^\circ = \frac{\sqrt{3}+1}{2\sqrt{2}}$	dB1
	<ul style="list-style-type: none"> $\sin 75^\circ = \sin 105^\circ = \frac{\sqrt{3}+1}{2\sqrt{2}}$ $\sin 75^\circ = \sin 105^\circ = \frac{\sqrt{2}+\sqrt{6}}{4} = \frac{\sqrt{3}+1}{2\sqrt{2}}$ 		
	$\cos 75^\circ = -\cos 105^\circ = -\left(\frac{1-\sqrt{3}}{2\sqrt{2}}\right)$ or $\frac{\sqrt{3}-1}{2\sqrt{2}}$ or $\frac{\sqrt{6}-\sqrt{2}}{4}$	States $\cos 75^\circ = -\cos 105^\circ$ and deduces a correct exact value for $\cos 75^\circ$	B1
			(2)
			9
Question 10 Notes			
10. (e)	ALT 1	Comparing their matrix found in part (c) with a correct $\begin{pmatrix} -\cos 75 & -\sin 75 \\ \sin 75 & -\cos 75 \end{pmatrix}$ (representing a rotation 105° anti-clockwise about <i>O</i>) gives	
		$\sin 75^\circ = \frac{\sqrt{3}+1}{2\sqrt{2}}$ (with the 1 st A mark scored in part (c))	B1
		$\cos 75^\circ = -\left(\frac{1-\sqrt{3}}{2\sqrt{2}}\right)$ or $\frac{\sqrt{3}-1}{2\sqrt{2}}$ or $\frac{\sqrt{6}-\sqrt{2}}{4}$	B1
			(2)

