WMA01



Mark Scheme (Results)

January 2016

International Advanced Level in Core Mathematics C12 (WMA01/01)

Winter 2016

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**Mathematics C12** 

Past Paper (Mark Scheme)

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# General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

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## **EDEXCEL GCE MATHEMATICS**

# **General Instructions for Marking**

- 1. The total number of marks for the paper is 125.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{\text{will}}$  be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the

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subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected. If you are using the annotation facility on ePEN, indicate this action by 'MR' in the body of the script.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.
- 8. Marks for each question are scored by clicking in the marking grids that appear below each student response on ePEN. The maximum mark allocation for each question/part question(item) is set out in the marking grid and you should allocate a score of '0' or '1' for each mark, or "trait", as shown:

|     | 0 | 1 |
|-----|---|---|
| аМ  |   | • |
| aA  | • |   |
| bM1 |   | • |
| bA1 | • |   |
| bB  | • |   |
| bM2 |   | • |
| bA2 |   | • |

9. Be careful when scoring a response that is either all correct or all incorrect. It is very easy to click down the '0' column when it was meant to be '1' and all correct.

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# General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

### Method mark for solving 3 term quadratic:

### 1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q)$$
, where  $|pq| = |c|$ , leading to  $x = \dots$   
 $(ax^2 + bx + c) = (mx + p)(nx + q)$ , where  $|pq| = |c|$  and  $|mn| = |a|$ , leading to  $x = \dots$ 

### 2. Formula

Attempt to use <u>correct</u> formula (with values for a, b and c).

## 3. Completing the square

Solving 
$$x^2 + bx + c = 0$$
:  $(x \pm \frac{b}{2})^2 \pm q \pm c$ ,  $q \neq 0$ , leading to  $x = ...$ 

### Method marks for differentiation and integration:

### 1. Differentiation

Power of at least one term decreased by 1.  $(x^n \rightarrow x^{n-1})$ 

### 2. Integration

Power of at least one term increased by 1.  $(x^n \rightarrow x^{n+1})$ 

### Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

**Method mark** for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

### **Exact answers**

Examiners' reports have emphasised that where, for example, an <u>exact</u> answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

### **Answers without working**

The rubric says that these <u>may</u> not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required. Most candidates do show working, but there are occasional awkward cases and if the mark scheme does <u>not</u> cover this, please contact your team leader for advice.

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# January 2016 **Core Mathematics C12 Mark Scheme**

| Question<br>Number | Scheme  | Marks       |  |  |  |
|--------------------|---|-------------|--|--|--|
| 1(a)               | $u_2 = 2 \times 2 - 6 = -2$ , $u_3 = 2 \times (-2) - 6 = -10$ or $u_3 = 2 \times (2 \times 2 - 6) - 6 = -10$                      | M1 A1       |  |  |  |
|                    |   | [2]         |  |  |  |
| (b)                | $\sum_{i=1}^{4} u_i = 2 + (-2) + (-10)$   | M1          |  |  |  |
|                    | +(-26)  | A1ft        |  |  |  |
|                    | = -36   | A1          |  |  |  |
|                    |   | [3]         |  |  |  |
|                    |   | 5 marks     |  |  |  |
|                    | Notes   | 1 0         |  |  |  |
| (a)                | M1: Attempt to use the given formula correctly at least once. This may be implied by a correct value for                          |             |  |  |  |
|                    | $u_2$ or a value for $u_3$ which follows through from their $u_2$ or implied by correct answer for $u_3$                          |             |  |  |  |
|                    | A1: $u_3$ correct and no incorrect work seen  |             |  |  |  |
|                    |   |             |  |  |  |
| (b)                | M1: Uses sum of the 3 numerical terms from part (a) (may be implied by correct answer for the Attempting to sum an AP here is M0. | eir terms). |  |  |  |
|                    | A1ft: obtains $u_4$ correctly (may be attempted in part (a)) and adds to sum of the first three terms from part                   |             |  |  |  |
|                    | (a) A1: -36 cao (-36 implies both A marks)  |             |  |  |  |
|                    | Special Cases:  |             |  |  |  |
|                    | Some candidates attempt $u_2 + u_3 + u_4 + u_5$ in part (b) – allow M1 only   |             |  |  |  |
|                    | Some candidates mis-copy one of their terms from part (a) into part (b) – allow M1 only   |             |  |  |  |

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| Question<br>Number |  | Sche   | me   |   | Marks                  |
|--------------------|--|--|--|---|------------------------|
|                    | Way 1:   | W  | ay 2:  | Way 3:  |                        |
| 2(i)               | $\frac{49}{\sqrt{7}} = \frac{7^2}{7^{\frac{1}{2}}} = 7^{2 - \frac{1}{2}}$  | 7√7  | $=7^{1+\frac{1}{2}}$   | $7^{a} = \frac{49}{\sqrt{7}} \Rightarrow a = \frac{\log \frac{49}{\sqrt{7}}}{\log 7}$ or $7^{a} = \frac{49}{\sqrt{7}} \Rightarrow a = \log_{7} \frac{49}{\sqrt{7}}$   | M1                     |
|                    | (a =   | $= 1\frac{1}{2}$ (oe) or   | see answer = $7^{1\frac{1}{2}}$  |   | A1                     |
|                    | · ·  | , , , , , , , , , , , , , , , , , , ,  |  |   | [2]                    |
| (ii)               | Way 1:   |  |  | <b>Way 2:</b>   | 1                      |
|                    | $\frac{10(\sqrt{18}+4)}{(\sqrt{18}-4)(\sqrt{18}+4)}$   | -  | (15√2  | $(2+20)(\sqrt{18}-4)$   | M1                     |
|                    | = \frac{\dots}{2}  |  | $=15\sqrt{36}$ -   | $60\sqrt{2} + 20\sqrt{18} - 80$   | B1                     |
|                    | $\frac{10}{\sqrt{18} - 4} = 5\left(3\sqrt{2} + 4\right) = 15\sqrt{2}$  | $\sqrt{2} + 20*$   |  | $\frac{10}{8} = 15\sqrt{2} + 80$ $\frac{10}{8} = 4$   | Alcso                  |
|                    |  |  |  |   | [3]                    |
|                    |  | Not  | 06   |   | 5 marks                |
| (i)                | Way 1:   |  | Vay 2:   | Way 3:  |                        |
|                    | 1  | and adds the A1: cao (ar low work with   | fraction to $7\sqrt{7}$<br>ir powers of 7<br>nswer only is 2 ma<br>inexact decimals f<br>$52 = 1.4999 \Rightarrow a$ |   | o obtain a             |
| (ii)               | Way 1:  M1: Multiply numerator and denoted $\sqrt{18} + 4$ or equivalent. The statem $\frac{10(\sqrt{18} + 4)}{(\sqrt{18} - 4)(\sqrt{18} + 4)}$ is sufficient $\frac{10(\sqrt{18} + 4)}{\sqrt{18} - 4(\sqrt{18} + 4)}$ unless respectively obtains $\pm 2$ in the definition of the follow M1 – i.e. treat as A implied by e.g. $\frac{10(\sqrt{18} + 4)}{18 - 16} = 5($ A1: Correct result with no errors so $\sqrt{18} = 3\sqrt{2}$ used before their fin Note that for Way 1, correct work $5\sqrt{18} + 20$ followed by $15\sqrt{2} + 20$ intermediate step would lose the finance of the statement of the finance of the statement of the stat | pominator by ment but do not missing at work. Enominator (1). May be $(\sqrt{18} + 4)$ seen and mal answer. It leading to 20 with no | M1: Attempts to at least 3 (not nee B1: All 4 terms of A1) A1: Obtains 10 v implied by e.g. 2                        | Way 2:<br>expand $(15\sqrt{2} + 20)(\sqrt{18} - 20)$<br>cessarily correct) terms<br>forrect ( <b>Must follow M1 – i.</b><br>with no errors and $\sqrt{18} = 3\sqrt{20}$<br>$20\sqrt{18} = 60\sqrt{2}$ and conclusinswer i.e. not just $10 = 10$ | e. treat as  2 seen or |

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| Question<br>Number | Scheme   | Marks    |
|--------------------|--|----------|
| 3.                 | $\int \left(6x - 3 - \frac{2}{\sqrt{x}}\right) dx = \frac{6x^2}{2} - 3x - \frac{2x^{\frac{1}{2}}}{\frac{1}{2}} + (c)$  | M1 A1 A1 |
|                    | $\left[\frac{6x^2}{2} - 3x - \frac{2x^{\frac{1}{2}}}{\frac{1}{2}} + (c)\right]_1^4 = (28) - (-4) = 32$   | M1 A1    |
|                    |  | [5]      |
|                    |  | 5 marks  |
|                    | Notes  |          |
|                    | M1: Attempt to integrate original $f(x)$ – at least one power increased $x^n \to x^{n+1}$<br>A1: Two of the three terms correct un-simplified or simplified (Constant not required)<br>A1: All three terms correct un-simplified or simplified (Constant not required)<br>M1: Substitutes limits 4 and 1 into their 'changed' function and subtracts the right way round<br>A1: 32 cao (32 + c is A0)<br>The question requires the use of calculus so a correct answer only scores no marks) |          |

| Question<br>Number | Scheme   | Marks              |  |
|--------------------|--|--------------------|--|
| 4.                 | $a + 3d = 3$ <b>OR</b> $\frac{6}{2}(2a + 5d) = 27$   | M1 A1              |  |
|                    | $a + 3d = 3$ <b>OR</b> $\frac{6}{2}(2a + 5d) = 27$<br>$a + 3d = 3$ <b>AND</b> $\frac{6}{2}(2a + 5d) = 27$  | A1                 |  |
|                    | Eliminates one variable to find a or d from 2 equations in a and d   | dM1                |  |
|                    | Obtains $a = 12$ or $d = -3$   | A1                 |  |
|                    | Obtains $a = 12$ and $d = -3$  |                    |  |
|                    |  | [6] <b>6 marks</b> |  |
|                    | Notes  |                    |  |
|                    | <b>M1A1:</b> Writes down a correct (possibly un-simplified) equation for $4^{th}$ term <b>or</b> for sum of the first Allow the individual terms to be added for the sum e.g. $a + a + d + a + 2d + a + 3d + a + 4d + a + 4$ | 5d = 27 implified) |  |
|                    | Note that if both equations are correct and there is <b>no working</b> and the values of $a$ and $d$ are both this scores dM0. Also if either or both equations is/are incorrect and values of $a$ and $d$ are obtained <b>working</b> this also scores dM0.   |                    |  |

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| Question<br>number | Scheme   |                    |                                  |                        | Marks   |                           |
|--------------------|--|--------------------|----------------------------------|------------------------|---|---------------------------|
| 5(a)               | Sketch of a positive sine curve- passing through O with at least one complete cycle from O. Condone different amplitudes above and below the x-axis.   |                    |                                  | t one complete cycle   | B1  |                           |
|                    |  |                    | shown (                          | -                      | e and a half cycles as<br>and crossing the x- | B1                        |
|                    |  |                    |                                  |                        |   | [2]                       |
| (b)                | $\begin{bmatrix} x & 0 \\ y & 0 \end{bmatrix}$   |                    | $\frac{\pi}{12}$ 0.5             | $\frac{\pi}{6}$ 0.866  | $\frac{\pi}{4}$                               |                           |
|                    | , , ,  |                    |                                  |                        |   |                           |
|                    | Uses $\frac{1}{2} \times \frac{\pi}{12}$ May be implied by use of e.g. $\frac{1}{2}h = \frac{1}{2}\left(\frac{\pi}{6} - \frac{\pi}{12}\right) = \frac{1}{2}\left(0.261\right)$   |                    |                                  |                        | B1  |                           |
|                    | $\{(0+1)+2(0.5+0.866)\}$   |                    |                                  | M1                     |   |                           |
|                    | 0.4885176576 awrt 0.49   |                    |                                  | A1                     |   |                           |
|                    |  |                    | N                                |                        |   | [3] <b>5 marks</b>        |
| (a)                | Notes as above   |                    | IN                               | otes                   |   |                           |
| (4)                | Notes as above <b>B1</b> : Correct shape with positive gradient through $O$ <b>B1</b> : Need not see endpoints labelled. Ignore any part of the curve to the left of the origin but if the curve extends beyond $x = \frac{3\pi}{2}$ then then $x = \frac{3\pi}{2}$ must be labelled on the diagram. Labels for $\frac{\pi}{2}$ and $\pi$ may be on the diagram or in the text but not just in a table of values and must be in radians not degrees. (Allow awrt 1.57 and 3.14)  The amplitudes must not be significantly different above and below the $x$ -axis.   |                    |                                  |                        |   | s for $\frac{\pi}{2}$ and |
| (b)                | <b>B1:</b> Need ½ of $\frac{\pi}{12}$ or to see $\frac{\pi}{24}$   | or ½               | of 0.261                         |                        |   |                           |
|                    | M1: requires first bracket to contain additional values from the two in the stranger of the st | in firs the tab    | et plus las<br>ble.<br>astead of | t values <b>and</b> se | ores M0.                                      | e no                      |
|                    | Special Case: Bracketing mistake:  | i.e. $\frac{3}{2}$ | $\frac{\pi}{24} (0+1)$           | +2(0.5+0.86            | 66) (= 2.86)                                  |                           |
|                    | scores <b>B1 M1 A0</b> unless the final a full marks can be given).  Need to see trapezium rule used   | answe              | er implies                       | that the calcul        | ation has been done con                       | rectly (then              |

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**Mathematics C12** 

Question Scheme Marks Number  $f(x) = x^3 + x^2 - 12x - 18$ 6. (a) Attempts  $f(\pm 3)$ M1  $\{f(-3)=\}$ 0 so (x + 3) is a factor of f(x). **A**1 [2] **(b)**  $x^3 + x^2 - 12x - 18 = (x+3)(x^2 + ...$ M1 $x^3 + x^2 - 12x - 18 = (x+3)(x^2 - 2x - 6)$ **A**1 or  $x^3 + x^2 - 12x - 18 = (x+3)(x-1+\sqrt{7})(x-1-\sqrt{7})$  oe [2] (c) **B**1  $x = \frac{2 \pm \sqrt{4 + 24}}{2} = 1 \pm \sqrt{7}$  or by completion of square  $(x - 1)^2 = 7$  so  $x = 1 \pm \sqrt{7}$ M1 A1 or  $(x-1+\sqrt{7})(x-1-\sqrt{7})=0 \Rightarrow x=1\pm\sqrt{7}$ [3] 7 marks Notes M1: As on scheme – must use the factor theorem (a) A1: for seeing 0 and conclusion which may be in a preamble and may be minimal e.g. QED, proven, true, tick etc. There must be no obvious errors but need to see at least  $(-3)^3 + (-3)^2 - 12(-3) - 18 = 0$  for A1 but allow invisible brackets e.g.  $-3^3 + -3^2 - 12(-3) - 18 = 0$  provided there are no obvious errors. M1: Uses (x + 3) as a factor and obtains correct first term of quadratic factor by division or any other **(b)** method e.g. comparing coefficients or finding roots and factorising A1: Correct quadratic and writes  $(x+3)(x^2-2x-6)$  or  $(x+3)(x-1+\sqrt{7})(x-1-\sqrt{7})$  oe Note that this work may be done in part (a) and the result re-stated here. **(c) B1:** States -3M1: Method for finding their roots. Allow the usual rules applied to their quadratic. This mark is for finding the roots and not for just finding factors. You may need to check their roots if no working is shown e.g. if they give decimal answers (3.645..., -1.645...) A1: need both roots. Correct answer implies M mark. Allow  $x = \frac{2 \pm \sqrt{28}}{2}$ If they give extra roots e.g. x = -3, -1,  $\frac{2 \pm \sqrt{28}}{2}$ , lose the final A mark (B1M1A0)

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| Question<br>Number | Scheme  | Marks        |
|--------------------|---|--------------|
| 7(a)               | $(1+kx)^8 = 1 + \binom{8}{1}(kx) + \binom{8}{2}(kx)^2 + \binom{8}{3}(kx)^3 \dots$   | M1           |
|                    | $=1+8kx,+28k^2x^2,+56k^3x^3+$   | B1, A1, A1   |
| <b>a</b> >         |   | [4]          |
| (b)                | Sets " $56k^3$ " = 1512 and obtains $k^3 = \frac{1512}{56}$   | M1 A1        |
|                    | So $k = 3$  | A1           |
|                    |   | [3]          |
|                    |   | 7 marks      |
|                    | Notes   |              |
| (a)                | M1: The <b>method</b> mark is awarded for an attempt at the Binomial expansion to get the third at term. The <b>correct</b> binomial coefficient needs to be combined with the correct power of $x$ . Ign errors and omission of or incorrect powers of $k$ . Accept any notation for ${}^{8}C_{2}$ or ${}^{8}C_{3}$ , e.g. $\begin{pmatrix} 8 \\ 2 \end{pmatrix}$ 28 or 56 from Pascal's triangle. This mark may be given if no working is shown, but either or both of $28k^{2}x^{2}$ and $56k^{3}x^{3}$ is <b>B1:</b> This is for $1 + 8kx$ and not for just $1 + \begin{pmatrix} 8 \\ 1 \end{pmatrix}(kx)$ <b>A1:</b> is cao and is for $28k^{2}x^{2}$ or for $28(kx)^{2}$ <b>A1:</b> is cao and is for $56k^{3}x^{3}$ or for $56(kx)^{3}$ Any extra terms in higher powers of $x$ should be ignored. Allow terms separated by commas or given as a list for all the marks. | ore bracket  |
| (b)                | M1: Sets their coefficient of $x^3 = 1512$ and obtains $k^n =$ where $n$ is 1 or 3  A1: $k^3 = \frac{1512}{56}$ or equivalent e.g. 27 (May be implied by their final answer)  A1: $k = 3$ cao ( $\pm 3$ is A0)  Note (b) can be marked independently of part (a) so part (a) might be incorrect or not a they have $56k^3 = 1512$ etc. in (b)   | ttempted but |

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| Question<br>Number | Scheme  | Marks        |
|--------------------|---|--------------|
|                    | $7\sin x = 3\cos x$   |              |
| 8(a)               | $(\tan x =)\frac{3}{7}$   | B1           |
|                    |   | [1]          |
| <b>(b)</b>         | $\tan\left(2\theta+30\right)=\frac{3}{7}$   | B1ft         |
|                    | $\tan^{-1}$ " $\frac{3}{7}$ " $(\alpha)$  | M1           |
|                    | One of $\theta$ = awrt 87 or awrt 177 or awrt 267 or awrt 357   | A1           |
|                    | Follow through any of their final $\theta$ 's for $\theta \pm 90n$ within range   | A1ft         |
|                    | All of $\theta = 86.6$ , 176.6, 266.6, 356.6  | A1           |
|                    |   | [5]          |
|                    |   | 6 marks      |
|                    | Notes   |              |
| (a)                | <b>B1:</b> $(\tan x =)\frac{3}{7}$ or exact equivalent so accept recurring decimal (0.428571) but not roun                    | ided answer  |
| (b)                | <b>B1ft:</b> Correct equation as shown or follow through their value for tan x from part (a). Must be                         | be           |
|                    | $\tan(2\theta+30) = \dots$ but $2\theta+30$ may be implied later by an attempt to subtract 30 and then of                     | divide by 2. |
|                    | If the processing is unclear or incorrect and $2\theta + 30$ is never seen, score B0 here.                                    |              |
|                    | <b>M1:</b> Finds arctan of their $\frac{3}{7}$ . Could be implied by their value e.g. 23.19 or just $\tan^{-1} \frac{3}{7}$ . |              |
|                    | <b>A1:</b> For <b>one</b> of either $\theta$ = awrt 87 or awrt 177 or awrt 267 or awrt 357                                    |              |
|                    | A1ft: Follow through any of their final answers to which an integer multiple of 90 has been                                   | added or     |
|                    | subtracted to give another solution in range but not for adding a multiple of 90 to just $\alpha$ .                           |              |
|                    | A1: For all 4 correct answers to the required accuracy as stated in the scheme. Ignore e                                      | xtra answers |
|                    | outside range but lose last A mark for extra answers inside range.  |              |

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| Question<br>Number | Scheme   | Marks             |
|--------------------|--|-------------------|
| 9.(a)              | $130000 \times (1.02) = 132600 * \text{ or } 2\% = 2600 \text{ and } 130000 + 2600 = 132600 *$   | B1                |
| (b)                | (r =) 1.02   | [1]<br>B1         |
| (c)                | Uses $130000 \times (1.02)^{N-1} > 260000$ or $130000 \times (1.02)^{N-1} = 260000$  | [1]<br>M1         |
|                    | So $(1.02)^{N-1} > 2$  | A1                |
|                    | $(N-1)\log_{10}(1.02) > \log_{10} 2$ or $(N-1)\log_{10}(1.02) = \log_{10} 2$<br>or $(N-1) > \log_{1.02} 2$ or $(N-1) = \log_{1.02} 2$  | M1                |
|                    | $N > \frac{\log_{10} 2}{\log_{10} (1.02)} + 1*$  | Alcso             |
| (d)                | (N=) 37  | [4]<br>B1         |
|                    |  | [1] 7 marks       |
|                    | Notes  | 7 marks           |
| (a)                | <b>B1:</b> A reason must be provided for this mark as the answer is printed.<br><b>Allow both</b> $130000 \times (1+2\%)$ and $130000 \times (102\%)$ as both give the correct answer when ent   | ered this         |
| (b)                | way on a calculator. But not $130000 \times 1 + 2\%$ B1: For 1.02 oe e.g. allow $\frac{51}{50}$  |                   |
| (c)                | <b>M1:</b> Correct inequality or equality – may use $r$ or their $r$ or 1.02 and may use $N$ or $n$ .<br><b>A1:</b> $(1.02)^{N-1} > 2$ cao. Allow $(1.02)^{n-1} > 2$   | th .              |
|                    | M1: Correct use of logs power rule on their previous line which must have come from using the of a GP. Condone missing brackets for this mark e.g. $N - 1\log_{10}(1.02) > \log_{10} 2$ . (May follow u instead of > or use of r instead of 1.02 or use of N instead of $N - 1$ ). These cases can get M0A0M the base to be absent or just 'ln' for this mark. If the inequality sign is reversed at this point, still M1. | se of = 11. Allow |
|                    | A1*: Answer is <b>exactly</b> as printed ( <b>including the bases</b> ) and <b>all</b> inequality work should be corresprevious marks scored and <b>no missing brackets earlier</b> . Allow this mark to score from a correctine provided the power rule is used. So fully correct work leading to   |                   |
|                    | $(N-1)\log_{10}(1.02) > \log_{10}2 \Rightarrow N > \frac{\log_{10}2}{\log_{10}(1.02)} + 1$ scores the final M1A1 but   |                   |
| (d)                | $(1.02)^{N-1} > 2 \Rightarrow N > \frac{\log_{10} 2}{\log_{10} (1.02)} + 1$ scores M0A0 (no explicit use of power rule)  B1: Only need $N = 37$ – may follow trial and error or uses logs to a different base.   |                   |
|                    | Do not allow $N \ge 37$ or $N > 37$ or $N = 37.0$  |                   |

Winter 2016 www.mystudybro.com **Mathematics C12** This resource was created and owned by Pearson Edexcel Past Paper (Mark Scheme) WMA01 Question Scheme Marks Number  $y = 12x^{\frac{5}{4}} - \frac{5}{18}x^2 - 1000$  $\frac{dy}{dx} = 12 \times \frac{5}{4} x^{\frac{1}{4}} - \frac{10}{18} x$ 10.(a)M1 A1 [2] **(b)** Put  $12 \times \frac{5}{4} x^{\frac{1}{4}} - \frac{10}{18} x = 0$  so  $x^n = k \ (n \in \square, k \neq 0)$ M1dM1 **A**1 (Ignore x = 0 if given as a second solution) So  $y = 12(81)^{\frac{5}{4}} - \frac{5}{18}(81)^2 - 1000$  i.e. y = 93.5dM1A1 [5] (c)  $\frac{d^2y}{dx^2} = \frac{15}{4}x^{-\frac{3}{4}} - \frac{5}{9}$ B1ft Substitutes their non-zero x (positive or negative) into their second derivative. M1 Obtains maximum after correctly substituting 81 into correct second derivative to give correct negative quantity  $-\frac{15}{36}$  o.e. or decimal e.g. -0.4... (see note below) and considers negative sign deducing maximum. **A**1 Note that a correct second derivative followed by  $x = 81 \Rightarrow \frac{d^2y}{dx^2} = \frac{15}{4}81^{-\frac{3}{4}} - \frac{5}{9} = -\frac{5}{12}$  therefore maximum scores B1M1A0 here. [3] 10 marks **Notes M1:** Attempt to differentiate – power reduced by one  $x^n \to x^{n-1}$  (but not just  $1000 \to 0$ ) (a) **A1:** Two correct terms and no extra terms. Terms may be un-simplified. **(b)** M1: Puts derivative = 0 and attempts to solve to obtain an equation of the form  $x^n = k$  where n is real and *k* is non-zero **dM1:** Correct processing to obtain a value for x. (Dependent on the first method mark). This mark can only be awarded for processing an equation of the form  $ax^{\frac{1}{4}} - bx = 0$  i.e. their derivative must have the correct powers of x. E.g.  $ax^{\frac{1}{4}} - bx = 0 \Rightarrow x^{\frac{1}{4}} \left( a - bx^{\frac{3}{4}} \right) \Rightarrow x = k^{\frac{4}{3}}$  or  $ax^{\frac{1}{4}} - bx = 0 \Rightarrow ax^{\frac{1}{4}} = bx \Rightarrow px = qx^4 \Rightarrow x = \sqrt[3]{k}$ Do not allow incorrect squaring e.g.  $ax^{\frac{1}{4}} - bx = 0 \Rightarrow px - qx^{4} = 0$  etc. **dM1:** Substitutes their **positive** value for x into  $y = \dots$  and not into  $\frac{dy}{dx} = \dots$  (Dependent on the first method mark)

If x = 81 appears from **no working** following a correct derivative score M1M0A0 then allow full recovery. (c) **B1ft:** Correct **follow through** second derivative

M1: Substitutes their non-zero x (positive or negative) into their second derivative.

Note: Solving  $\frac{d^2y}{dx^2} = 0$  is M0

A1: cao

Alcso: Completely correct work  $\left(-\frac{5}{12}\right)$  o.e.). Note that o.e. could be  $=\frac{15}{4}\times\frac{1}{27}-\frac{5}{9}$  or  $\frac{15}{108}-\frac{5}{9}$  or  $\frac{5}{36}-\frac{5}{9}$ or -0.4....but it has to be correct for the final mark.

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| Question<br>Number | Scheme   | Marks                |
|--------------------|--|----------------------|
| 11(a)              | $16^2 = 10^2 + 12^2 - 2 \times 10 \times 12\cos \angle YXZ$  | M1                   |
|                    | $\cos \angle YXZ = \frac{10^2 + 12^2 - 16^2}{2 \times 10 \times 12} \text{ or } \frac{-12}{240} \text{ or } -0.05$   | A1                   |
|                    | $\angle BOC = 1.62(08)$ (N.B. 92.87 degrees is A0)   | A1                   |
| (b)                | Uses $s = 5\theta$ with their $\theta$ from part (a)   | [3]<br>M1            |
|                    | awrt 8.1   | A1                   |
|                    | Perimeter = $r\theta + 28$ , = 28 + their arc length   | M1                   |
|                    | awrt 36.1  | A1                   |
|                    |  | [4]                  |
| (c)                | area of sector = $\frac{1}{2}(5)^2 \theta$   | B1ft                 |
|                    | area of triangle = $\frac{1}{2}10 \times 12 \sin \theta$ (= 59.92 or 59.93)  | B1ft                 |
|                    | Area of shaded region = $\frac{1}{2} \times 10 \times 12 \sin \theta - \frac{1}{2} (5)^2 \theta = 59.9 20.2$<br>= 39.7 (cm <sup>2</sup> )  | M1<br>A1             |
|                    |  | [4]<br>(11<br>marks) |
|                    | Notes  |                      |
| (a)                | <ul> <li>M1: Uses cosine rule – must be a correct statement</li> <li>A1: Correct value or correct numerical expression for cos ∠YXZ</li> <li>A1: accept awrt 1.62 and must be seen in part (a) (answer in degrees is A0 (92.865))</li> </ul> |                      |
| (b)                | M1: Uses $s = 5\theta$ with their $\theta$ in radians, or correct formula for degrees if working in degrees  |                      |
|                    | A1: Accept awrt 8.1 (may be implied by their perimeter)  |                      |
|                    | M1: Adds their arc length to $28 \text{ or } (16 + 7 + 5)$   |                      |
| (c)                | A1: Accept awrt 36.1 do not need units (ignore any given)  B1ft: This formula used with their $\theta$ in radians or correct formula for degrees   |                      |
| (c)                | <b>B1ft:</b> Correct formula for area <b>used</b> – may use half base times height (may be implied by a cor (59.9))  | rect answer          |
|                    | M1: Subtracts their sector area from their triangle area this way round.   |                      |
|                    | A1: awrt 39.7 – do not need units (ignore any given)  Alternative approach to finding angle YXZ and area of triangle:  |                      |
|                    | Let foot of perpendicular from X to YZ be W and $XW = h$ and $YW = x$ so $WZ = 16 - x$ :   |                      |
|                    | $h^2 + x^2 = 100$ , $h^2 + (16 - x)^2 = 144 \Rightarrow x = \frac{53}{8}$ , $h = \frac{3\sqrt{399}}{8}$ M1: Correct work leading to values of  | x and $h$            |
|                    | $\angle YXZ = \sin^{-1}\left(\frac{53}{80}\right) + \sin^{-1}\left(\frac{25}{32}\right) = 1.62$ A1:Correct expression for $\angle YXZ$ , A1: awrt 1.62   |                      |
|                    | The B1 for the triangle area in (c) can then score for $\frac{1}{2} \times 16 \times "\frac{3\sqrt{399}}{8}"$ . Note this is $3\sqrt{399}$   |                      |

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| Question<br>Number | Scheme  | Marks                          |
|--------------------|---|--------------------------------|
| 1 (01110-01        | (a) and (b) can be marked together  |                                |
| 12(a)              | $f(x) = \frac{16 + 24\sqrt{x} + 9x}{x}$   | M1                             |
|                    | $f(x) = 16x^{-1} + 24x^{-\frac{1}{2}} + 9$  | M1A1A1                         |
|                    |   | [4]                            |
| <b>(b)</b>         | $f'(x) = -16x^{-2} - 12x^{-\frac{3}{2}}$  | M1 A1                          |
| (c)                | When $x = 4$ , $y = 25$   | [2]                            |
|                    | $f'(4) = -1 - \frac{12}{8} = -2\frac{1}{2}$<br>Equation of tangent is $y - 25 = -\frac{5}{2}(x - 4)$  | M1                             |
|                    | Equation of tangent is $y-25 = -\frac{5}{2}(x-4)$   | M1 A1                          |
|                    |   | [4]                            |
|                    |   | 10 marks                       |
|                    | Notes   |                                |
| (b)                | M1: Divides at least one term in numerator by $x$ correctly following an attempt at expansi $\frac{16}{x}$ .  A1: Two correct terms A1: All terms correct  M1: Evidence of differentiation $x^n \to x^{n-1}$ of an expression of the form $Ax^{-1}$ or $Bx^k$ so $x^k \to x^{k-1}$ $(k \ne 1)$ and not just $C \to 0$ . Differentiating top and bottom separately is M0 | $x^{-1} \rightarrow x^{-2}$ or |
|                    | Note this is a hence and so attempts at e.g. use of the quotient rule scores M0.  A1: cao and cso (May be un-simplified)  Note: An incorrect constant in part (a) (e.g. 3 instead of 9) will fortuitously give the s scores M1A0 if otherwise correct.  |                                |
| (c)                | <b>B1:</b> 25 only <b>M1:</b> Substitute $x = 4$ into their derived function <b>M1:</b> Uses their "25" and their "gradient" which has come from calculus ( <b>not the normal</b> $x = 4$ to give correct ft equation of line. If using $y = mx + c$ must at least obtain a value for <b>A1:</b> any correct form e.g.  |                                |
|                    | $y = -\frac{5}{2}x + 35, 	 5x + 2y - 70 = 0$ <b>BUT NOT JUST</b> $\frac{y - 25}{x - 4} = -\frac{5}{2}$ , this scores M1A0   |                                |
|                    | x-4 2<br>Note: An incorrect constant in part (a) (e.g. 3 instead of 9) will fortuitously give the c (c) and will lose the final A mark if otherwise correct.  | orrect answer in               |

# Past Paper (Mark Scheme)

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| Question<br>Number | Scheme   | Marks               |
|--------------------|--|---------------------|
| 13(a)              | $3kx^2 + (8k+6)x + 9k - 2 = 0$ or $3kx^2 + 8kx + 6x + 9k - 2 = 0$  | B1                  |
|                    | Uses $b^2 - 4ac$ with $a = 3k$ , $b = 8k \pm 6$ and $c = 9k \pm 2$   | M1                  |
|                    | $-44k^2 + 120k + 36 < 0$ or $36 < 44k^2 - 120k$ o.e.   | A1                  |
|                    | Reached with no errors   |                     |
|                    | $11k^2 - 30k - 9 > 0 *$  | A1*                 |
| (b)                | Attempts to solve $11k^2 - 30k - 9 = 0$ to give $k =$  | [4]<br>M1           |
|                    | $\Rightarrow$ Critical values, $k = 3, -\frac{3}{11}$  | A1                  |
|                    | $k > 3 \text{ (or) } k < -\frac{3}{11}$  | M1 A1cao            |
|                    |  | [4]                 |
|                    | N-4  | 8 marks             |
|                    | Notes  | 1: 1 1              |
| (a)                | <b>B1:</b> Multiplies by $k$ and collects terms to one side in any order. Allow the $x$ terms not to be conthe '= 0' may be implied by use of a <b>correct</b> discriminant.                   | nbined and          |
|                    | <b>M1:</b> Attempts $b^2 - 4ac$ with $a = 3k$ , $b = 8k \pm 6$ and $c = 9k \pm 2$ or uses quadratic formula with   | $b^2 - 4ac$         |
|                    | seen to solve their equation or uses $b^2 = 4ac$ or e.g. $b^2 < 4ac$ . There must be no x's.   |                     |
|                    | A1: Obtains a correct three term quadratic inequality that is not the printed answer with no A1: Correct answer with no errors   | errors seen.        |
| (b)                | M1: Uses factorisation, formula, or completion of square method to find <b>two values</b> for k or fit <b>correct</b> answers with no obvious method for <b>the given</b> three term quadratic | nds two             |
|                    | <b>A1:</b> Obtains $k = 3, -\frac{3}{11}$ accept awrt - 0.272  |                     |
|                    | <b>M1:</b> Chooses outside region ( $k <$ Their Lower Limit $k >$ Their Upper Limit ) for a 3 term of  | quadratic           |
|                    | inequality. Do not award simply for diagram or table.  |                     |
|                    | A1: $k > 3$ (or) $k < -\frac{3}{11}$ must be exact here but allow $-0.\dot{2}\dot{7}$ for $-\frac{3}{11}$ .  |                     |
|                    | Allow other notation such as $\left(-\infty, -\frac{3}{11}\right) \cup \left(3, \infty\right)$   |                     |
|                    | $k > 3$ and $k < -\frac{3}{11}$ and $-\frac{3}{11} > k > 3$ score M1A0   |                     |
|                    | ISW if possible e.g. $k > 3$ , $k < -\frac{3}{11}$ followed by $-\frac{3}{11} > k > 3$ can score M1A1  |                     |
|                    | $k > 3$ , $k > -\frac{3}{11}$ followed by $k > 3$ (or) $k < -\frac{3}{11}$ can score M1A1  |                     |
|                    | Allow (b) to be solved in terms of x for the first 3 marks but the final A mark needs the regions Fully correct answer with no working scores full marks.                                      | s in terms of $k$ . |
|                    | Answers that are otherwise correct but use $\leq$ , $\geq$ lose final mark.  |                     |

Past Paper (Mark Scheme)

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| Question<br>Number | Scheme  | Marks          |
|--------------------|---|----------------|
| 14(i)              | $\log_a x + \log_a 3 = \log_a 27 - 1$ so $\log_a \frac{3x}{27} = -1$<br>Or $\log_a x + \log_a 3 = \log_a 27 - \log_a a$ so $\log_a 3x = \log_a \frac{27}{a}$  | M1 A1          |
|                    | Or $\log_a x + 1 = \log_a 27 - \log_a 3 = \log_a 9$ so $\log_a ax = \log_a 9$   |                |
|                    | $\frac{3x}{27} = a^{-1}$  | M1             |
|                    | $x = 9a^{-1} \text{ or } \frac{9}{a}$   | A1 [4]         |
| (ii)               | $x^2 - 7x + 12 = 0$ and attempt to solve to give $x =$ or $\log_5 y =$ (implied by correct answers)   | M1             |
|                    | $x 	(or log_5 y) = 3 	 and 4$   | A1             |
|                    | $y = 5^3$ or $5^4$  | dM1            |
|                    | y = 125 and $625$   | A1             |
|                    |   | [4]<br>8 marks |
|                    | Notes   | o marks        |
| (i)                | M1: Uses sum or difference of logs correctly e.g.   | •              |
|                    | $\log x + \log 3 = \log 3x$ or $\log 27 - \log 3 = \log 9$ or $\log 27 - \log x = \log \frac{27}{x}$ etc.   |                |
|                    | or writes 1 as $\log_a a$   |                |
|                    | <ul> <li>A1: Uses two rules correctly to obtain correct log equation</li> <li>M1: Removes logs correctly to obtain an equation connecting x and a</li> <li>A1: Correct simplified answer</li> </ul> |                |
|                    | Note that some candidates interpret $\log_a 27 - 1$ as $\log_a (27 - 1)$ . This can score a maximum of $\Omega$   | out of 4 if    |
|                    | they have $\log x + \log 3 = \log 3x$   |                |
|                    | Note that $\log_a x + \log_a 3 = \log_a 27 - 1$ so $\frac{\log_a 3x}{\log_a 27} = -1 \Rightarrow \frac{3x}{27} = a^{-1}$ etc. scores <b>M1A0M0A0</b>  |                |
|                    | Note that $\log_a x + \log_a 3 = \log_a 27 - 1$ so $\frac{\log_a x \log_a 3}{\log_a 27} = -1 \Rightarrow \frac{3x}{27} = a^{-1}$ etc. scores <b>no mar</b>  | ks             |
| (ii)               | M1: Recognise and attempt to solve quadratic A1: Obtain both 3 and 4 (Both correct implies M1A1) dM1: Uses powers correctly to find a value for y (Dependent on first method mark)                  |                |
|                    | A1: Both values correct   |                |

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Past Paper (Mark Scheme)

| Question<br>Number | Scheme  | Marks                       |  |
|--------------------|---|-----------------------------|--|
| 15 (a)             | Mid-point of $AB = (2, -3)$   | M1 A1                       |  |
|                    | $(r^2) = (12 - "2")^2 + (2 - "-3")^2$ or $(r^2) = (-8 - "2")^2 + (-8 - "-3")^2$ or $(d^2) = (-8 - 12)^2 + (-8 - 2)^2$   | M1                          |  |
|                    | $r^2 = 125$   | A1                          |  |
|                    | "125" = $(x \pm "2")^2 + (y \pm "-3")^2$  | M1                          |  |
|                    | $125 = (x-2)^2 + (y+3)^2$   | A1                          |  |
|                    |   | [6]                         |  |
| (b)                | gradient from "(2, -3)" to (4, 8) = $\frac{8 - "-3"}{4 - "2"}$ , $\left(=\frac{11}{2}\right)$   | M1                          |  |
|                    | $ZM$ has gradient $-\frac{1}{m}$ $\left(=-\frac{2}{11}\right)$  | M1                          |  |
|                    | Either: $y - 8 = "-\frac{2}{11}"(x - 4)$ or: $y = "-\frac{2}{11}"x + c$ and $8 = "-\frac{2}{11}"(4) + c \implies c = "8\frac{8}{11}"$   | ddM1                        |  |
|                    | 2x + 11y - 96 = 0   | A1                          |  |
|                    |   | [4]                         |  |
|                    |   | (10marks)                   |  |
|                    | Notes   | (= = =====)                 |  |
| (a)                | M1: Uses midpoint formula, or implied by $y$ coordinate of -3 or $x$ coordinate of 2<br>A1: cao<br>M1: Finds radius or radius <sup>2</sup> , diameter or diameter <sup>2</sup> using any valid method – probably distance from to one of the points. Need not state $r =$ so ignore lhs – you are just looking for correct use of Pythagoras with or without the square root so ignore how they reference it for this mark.<br>A1: for any equivalent $r^2 = 125$ or $r = \sqrt{125}$ (11.18) etc. Their numeric answer must be identified either $r$ or $r^2$ (may be implied by their equation). If they halve it or double it, this is M1 A0.<br>M1: Attempt to use a true equation for circle with their centre and radius or the letter $r$ , allow sign so brackets but do not allow use or $r$ instead of $r^2$ in the equation.<br>So must be using $r^2 = (x \pm)^2 + (y \pm)^2$ |                             |  |
|                    | <b>A1:</b> correct answer only (Allow $(5\sqrt{5})^2$ instead of 125 but not $5\sqrt{5}^2$ )  |                             |  |
| (b)                | M1: States or uses gradient equation correctly with their centre and (4, 8). Must be using the (4, 8). If no method is shown and gradient incorrect for their values score M0.  M1: Finds negative reciprocal. Follow through their gradient ddM1: Correct straight line method with (4, 8) and perpendicular gradient. Dependent on both method marks having been scored.  A1: cao – accept multiples of this equation (Note integer coefficients not required) A common error here is to use the diameter to find the gradient. This usually scores M0M1ddl just one mark for the perpendicular gradient rule.  (b) Alternative uses implicit differentiation: e.g.   | ent on <b>both</b> previous |  |
|                    |   |                             |  |
|                    | $125 = (x-2)^2 + (y+3)^2 \Rightarrow 2(x-2) + 2(y+3)\frac{dy}{dx} = 0  M1(correct implicit differentiation)$ $\Rightarrow \frac{dy}{dx} = \frac{2-x}{y+3} = \frac{2-4}{8+3}  M1(Substitution)$ Then follow the scheme.  | n) oe                       |  |

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**Mathematics C12** 

| Question<br>Number | Scheme  | Marks        |
|--------------------|---|--------------|
| 16(a)              | $\frac{1}{2}x + 1 = x^2 - 4x + 3$   | M1           |
|                    | $2x^2 - 9x + 4 = 0 \Rightarrow x = \frac{1}{2} \text{ or } x = 4$   | dM1 A1       |
| <br>               | y = 5/4  or  y = 3  | dM1 A1       |
| (b)                | Curve meets x-axis at $x = 3$ and at $x = 1$ (No need to see $y = 0$ )  | [5]<br>M1 A1 |
| (b)                | Curve meets x-axis at $x = 3$ and at $x = 1$ (140 need to see $y = 0$ )   | [2]          |
|                    | NOTE that the subscripted A's refer to areas on the diagram given at the end of the   |              |
|                    | scheme. All the method marks are for their $x = 1/2$ , 4, 1 and 3   |              |
| (c)<br>Way 1       | $\int x^2 - 4x + 3  \mathrm{d}x = \frac{1}{3}x^3 - 2x^2 + 3x$   | M1 A1        |
|                    | Use limits 1 and $\frac{1}{2} \left[ \left( \frac{1}{3} (1)^3 - 2(1)^2 + 3 \times 1 \right) - \left( \frac{1}{3} \left( \frac{1}{2} \right)^3 - 2 \cdot \left( \frac{1}{2} \right)^2 + 3 \times \left( \frac{1}{2} \right) \right) \right] A_1$                       | M1           |
| <br>               | Use limits 4 and 3 $\left[ \left( \frac{1}{3} (4)^3 - 2(4)^2 + 3 \times (4) \right) - \left( \frac{1}{3} (3)^3 - 2 \cdot (3)^2 + 3 \times (3) \right) \right] A_2$  | M1           |
| <br>               | Area of trapezium =   |              |
|                    | $\frac{1}{2}(a+b) \times h = \frac{1}{2}(\frac{5}{4}+3) \times (4-\frac{1}{2}) = \dots \text{ or } \int_{\frac{1}{2}}^{4} (\frac{1}{2}x+1) dx = \left[\frac{1}{4}x^2 + x\right]_{\frac{1}{2}}^{4} = (4+4) - \left(\frac{1}{16} + \frac{1}{2}\right) = \dots$          | M1           |
| <b>-</b>           | 7.4375 $\left(7\frac{7}{16}\right) \left(\frac{119}{16}\right)$ (may be implied by correct final answer)  | A1           |
| -                  | Uses correct combination of correct areas. Area of region = Area of trapezium $-A_1 - A_2$  | ddddM1       |
| <br> -             | Dependent on all previous method marks  | addalvi i    |
| <br> -             | $= 7.4375 - \frac{7}{24} - \frac{4}{3} = \frac{93}{16} \text{ or } 5.8125$  | A1           |
| (c)                | Alternative method using "line – curve" and subtracting area below x- axis  | [8]          |
| Way 2              | $\int -x^2 + \frac{9}{2}x - 2dx = -\frac{x^3}{3} + \frac{9}{4}x^2 - 2x \text{ or } \int x^2 - \frac{9}{2}x + 2dx = \frac{x^3}{3} - \frac{9}{4}x^2 + 2x$   | M1A1         |
| -                  | Use limits $\frac{1}{2}$ and 4 on this <i>subtracted</i> integration $\left(A_3 + A_4 + A_5 + A_6\right) = 6\frac{2}{3} + \frac{23}{48} = \dots$  | M1           |
|                    | $\pm \int x^2 - 4x + 3 dx = \pm \left(\frac{1}{3}x^3 - 2x^2 + 3x\right)$  | M1           |
|                    | Use limits 1 and 3 on their integrated curve to obtain $A_6 = \pm \frac{4}{3}$  | M1A1         |
|                    | Uses correct combination of correct areas. Area of region = $(A_3 + A_4 + A_5 + A_6) - A_6$<br><b>Dependent on all previous method marks</b>  | ddddM1       |
| <u> </u>           | $6\frac{2}{3} + \frac{23}{48} - \frac{4}{3} = \frac{93}{16}$  | A1           |
|                    |   | [8]          |
| (c)<br>Way 3       | Alternative method using "line – curve" for areas $A_3$ and $A_4$ and adding smaller trapezium  |              |
| way 3              | $\int -x^2 + \frac{9}{2}x - 2dx = -\frac{x^3}{3} + \frac{9}{4}x^2 - 2x \text{ or } \int x^2 - \frac{9}{2}x + 2dx = \frac{x^3}{3} - \frac{9}{4}x^2 + 2x$   | M1A1         |
|                    | Use limits 1 and $\frac{1}{2} \left[ \left( -\frac{1}{3}(1)^3 + \frac{9}{4}(1)^2 - 2 \times 1 \right) - \left( -\frac{1}{3}(\frac{1}{2})^3 + \frac{9}{4}(\frac{1}{2})^2 - 2 \times \frac{1}{2} \right] A_3$   | M1           |
|                    | Use limits 4 and 3 $\left[ \left( -\frac{1}{3}(4)^3 + \frac{9}{4}(4)^2 - 2 \times 4 \right) - \left( -\frac{1}{3}(3)^3 + \frac{9}{4}(3)^2 - 2 \times 3 \right] A_4$   | M1           |
|                    | Area of trapezium =   |              |
|                    | $\frac{1}{2}(a+b) \times h = \frac{1}{2}(\frac{3}{2} + \frac{5}{2}) \times (3-1) = \dots \text{ or } \int_{1}^{3} \left(\frac{1}{2}x + 1\right) dx = \left[\frac{1}{4}x^{2} + x\right]_{1}^{3} = \left(\frac{9}{4} + 3\right) - \left(\frac{1}{4} + 1\right) = \dots$ | M1           |
| <u> </u>           | = 4   | A1           |
|                    | Uses correct combination of correct areas. Area of region = $A_3 + A_4 + A_5$   | ddddM1       |
|                    | Dependent on all previous method marks $\frac{19}{48} + \frac{17}{12} + 4 = \frac{93}{16}$  | A1           |
|                    | 48 12 1 1 16  | [8]          |
|                    |   | <u> </u>     |

Winter 2016 **Mathematics C12** This resource was created and owned by Pearson Edexcel Past Paper (Mark Scheme) **WMA01** Alternative method: Finds area of larger trapezium and subtracts  $A_1 + A_2$  which is found (c) by integrating quadratic between  $\frac{1}{2}$  and 4 and adding area below x-axis Way 4  $\int x^2 - 4x + 3 \, dx = \frac{1}{3}x^3 - 2x^2 + 3x$ M1 A1 Use limits 4 and  $\frac{1}{2} \left[ \left( \frac{1}{3} (4)^3 - 2(4)^2 + 3 \times 4 \right) - \left( \frac{1}{3} \left( \frac{1}{2} \right)^3 - 2 \cdot \left( \frac{1}{2} \right)^2 + 3 \times \left( \frac{1}{2} \right) \right) \right] A_1 + A_2 - A_6$ M2**AND** Use limits 3 and 1  $\pm \left[ \left( \frac{1}{3}(3)^3 - 2(3)^2 + 3 \times 3 \right) - \left( \frac{1}{3}(1)^3 - 2(1)^2 + 3 \times (1) \right) \right] \pm A_6$ Area of transzium =  $\frac{1}{2}(a+b) \times h = \frac{1}{2}(\frac{5}{4}+3) \times (4-\frac{1}{2}) = \dots \text{ or } \int_{1}^{\infty} (\frac{1}{2}x+1) dx = \left[\frac{1}{4}x^2 + x\right]_{\frac{1}{2}}^{4} = (4+4) - (\frac{1}{16} + \frac{1}{2}) = \dots$ M1 7.4375  $(7\frac{7}{16})$  (may be implied by correct final answer) **A**1 Uses correct combination of correct areas. Area of region =  $7.4375 - (A_1 + A_2 - A_4 + A_4)$ ddddM1 Dependent on all previous method marks  $=7.4375 - \left(\frac{7}{24} + \frac{4}{3}\right) = \frac{93}{16}$ **A**1 [8] 15 marks **Notes** M1: Puts equations equal or finds x in terms of y and substitutes or substitutes for x (a) **dM1:** Solves three term quadratic in x to obtain  $x = \dots$  or in y to obtain  $y = \dots$  (Dependent on first M) A1: Both answers correct **dM1:** Obtains at least one value for y or x (Dependent on **first** M) A1: Both correct **Note:** Allow candidates to obtain  $x^2 - \frac{9}{2}x + 2 = 0$  and solve as  $(2x-1)(x-4) = 0 \Rightarrow x = \frac{1}{2}$ ,4 The coordinates do not need to be 'paired' **M1:** Attempts to solve  $0 = x^2 - 4x + 3$  according to the usual rules **(b)** Attempts by T&I can score both marks for x = 1 and x = 3. If one solution is obtained by this, score M1A0 For (c) do not allow 'mixed' methods. For their strategy, they must be finding the appropriate areas but apply the method for the scheme that gives the most credit for the candidate. (c) M1: Attempt at integration of the given quadratic expression  $(x^n \to x^{n+1})$  at least once Way 1 A1: Correct integration of the given quadratic expression **M1:** Finds area of  $A_1$ **M1:** Finds area of  $A_2$ M1: Finds area of appropriate trapezium **A1:** Correct area of trapezium 7.4375  $(7\frac{7}{16})$ ddddM1: correct final combination **A1:** any correct form of this exact answer M1: Attempt at integration of  $\pm$  (the given quadratic expression – the given line)  $(x^n \to x^{n+1})$  at least once (c) Way 2 A1: Correct integration as shown in the mark scheme. Allow correct answer even if terms not collected nor simplified. If there are sign errors when subtracting before valid attempt at integration, score M1A0 M1: Uses the limits  $\frac{1}{2}$  and 4 on their subtracted integration **M1:** Attempts to integrate curve **M1:** Uses the limits 1 and 3 on the integrated curve C A1: Obtains  $A_6 = \pm \frac{4}{3}$ 

Note: A common error with this method is to use the limits ½ and 4 on their subtracted integration and then

stop (this should give an area of  $\frac{343}{48}$ ). This will usually score 3/8 in (c)

ddddM1: correct final combination **A1:** any correct form of this exact answer

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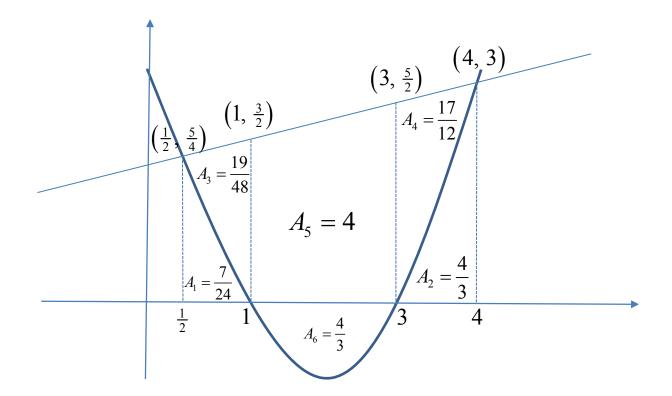
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WMA01

| (c)<br>Way 3 | <b>M1:</b> Attempt at integration of $\pm$ (the given quadratic expression – the given line) $(x^n \to x^{n+1})$ at least once         |  |
|--------------|--|--|
| way 3        | A1: Correct integration as shown in the mark scheme. Allow correct answer even if terms not collected nor                              |  |
|              | simplified. If there are sign errors when subtracting before valid attempt at integration, score M1A0                                  |  |
|              | M1: Uses the limits ½ and 1 on their <i>subtracted</i> integration   |  |
|              | M1: Uses the limits 4 and 3 on their <i>subtracted</i> integration   |  |
|              | M1: Finds area of appropriate trapezium  |  |
|              | A1: Correct area of trapezium 4  |  |
|              | ddddM1: correct final combination  |  |
|              | A1: any correct form of this exact answer  |  |
| (c)<br>Way 4 | <b>M1:</b> Attempt at integration of the given quadratic expression $(x^n \to x^{n+1})$ at least once                                  |  |
|              | A1: Correct integration of the given quadratic expression  |  |
|              | <b>M2:</b> Finds area of $A_1 + A_2 - A_6$ by using the limits $\frac{1}{2}$ and 4 and finds area of $A_6$ by using the limits 1 and 3 |  |
|              | M1: Finds area of appropriate trapezium  |  |
|              | A1: Correct area of trapezium 7.4375 $(7\frac{7}{16})$   |  |
|              | ddddM1: correct final combination  |  |
|              | A1: any correct form of this exact answer  |  |

# **Diagram for Question 16**



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