

Question Number	Scheme	Marks
1 (a)	$\frac{1}{(x^2+3x+5)} \times \dots = \frac{2x+3}{(x^2+3x+5)}$	M1,A1 (2)
1 (b)	<p>Applying $\frac{vu'-uv'}{v^2}$</p> $\frac{x^2 \times -\sin x - \cos x \times 2x}{(x^2)^2} = \frac{-x^2 \sin x - 2x \cos x}{x^4} = \frac{-x \sin x - 2 \cos x}{x^3} \text{ oe}$	M1, A2,1,0 (3) 5 Marks
2 (a)	$f(0.75) = -0.18\dots$ $f(0.85) = 0.17\dots\dots$ <p>Change of sign, hence root between $x=0.75$ and $x=0.85$</p>	M1 A1 (2)
2 (b)	<p>Sub $x_0=0.8$ into $x_{n+1} = [\arcsin(1 - 0.5x_n)]^{\frac{1}{2}}$ to obtain x_1</p> <p>Awrt $x_1=0.80219$ and $x_2=0.80133$</p> <p>Awrt $x_3 = 0.80167$</p>	M1 A1 A1 (3)
2 (c)	$f(0.801565) = -2.7\dots \times 10^{-5}$ $f(0.801575) = +8.6\dots \times 10^{-6}$ <p>Change of sign and conclusion</p> <p>See Notes for continued iteration method</p>	M1A1 A1 (3) 8 Marks

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2 (a)	$f(0.75) = -0.18\dots$ $f(0.85) = 0.17\dots\dots$ <p>Change of sign, hence root between $x=0.75$ and $x=0.85$</p>	M1 A1 (2)
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3.

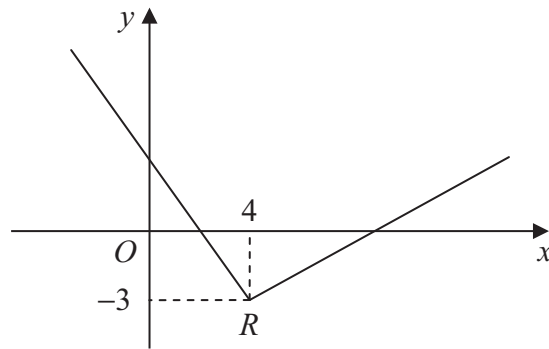


Figure 1

Figure 1 shows part of the graph of $y = f(x)$, $x \in \mathbb{R}$.

The graph consists of two line segments that meet at the point $R(4, -3)$, as shown in Figure 1.

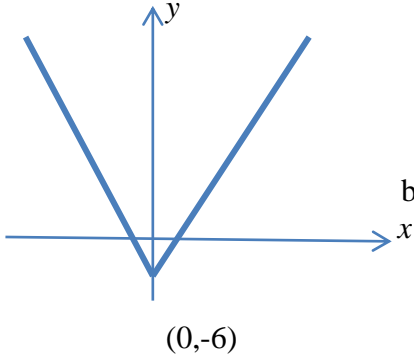
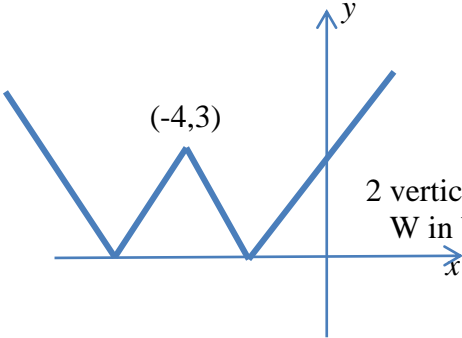
Sketch, on separate diagrams, the graphs of

(a) $y = 2f(x+4)$, (3)

(b) $y = |f(-x)|$. (3)

On each diagram, show the coordinates of the point corresponding to R .



Question Number	Scheme	Marks
3 (a)	 <p>V shape vertex on y axis & both branches of graph cross x axis 'y' co-ordinate of R is -6 (0,-6)</p>	<p>B1 B1 B1 (3)</p>
(b)	 <p>W shape 2 vertices on the negative x axis. W in both quad 1 & quad 2. $R' = (-4, 3)$</p>	<p>B1 B1dep B1 (3) 6 Marks</p>
4 (a)	$y = 4 - \ln(x + 2)$ $\ln(x + 2) = 4 - y$ $x + 2 = e^{4-y}$ $x = e^{4-y} - 2$ $f^{-1}(x) = e^{4-x} - 2$	<p>oe M1 M1A1 (3)</p>
(b)	$x \leq 4$	<p>B1 (1)</p>
(c)	$fg(x) = 4 - \ln(e^{x^2} - 2 + 2)$ $fg(x) = 4 - x^2$	<p>M1 dM1A1 (3)</p>
(d)	$fg(x) \leq 4$	<p>B1ft (1) 8 Marks</p>

Question Number	Scheme	Marks
5 (a)	$p=7.5$	B1 (1)
(b)	$2.5 = 7.5e^{-4k}$ $e^{-4k} = \frac{1}{3}$ $-4k = \ln\left(\frac{1}{3}\right)$ $-4k = -\ln(3)$ $k = \frac{1}{4}\ln(3)$	M1 M1 dM1 A1*
	See notes for additional correct solutions and the last A1	(4)
(c)	$\frac{dm}{dt} = -kpe^{-kt}$ ft on their p and k $-\frac{1}{4}\ln 3 \times 7.5e^{-\frac{1}{4}(\ln 3)t} = -0.6\ln 3$ $e^{-\frac{1}{4}(\ln 3)t} = \frac{2.4}{7.5} = (0.32)$ $-\frac{1}{4}(\ln 3)t = \ln(0.32)$ $t=4.1486\dots$ 4.15 or awrt 4.1	M1A1ft M1A1 dM1 A1 (6)
		11Marks

Question Number	Scheme	Marks
6 (a)	$\frac{1}{\sin 2\theta} - \frac{\cos 2\theta}{\sin 2\theta} = \frac{1 - \cos 2\theta}{\sin 2\theta}$ $= \frac{2\sin^2 \theta}{2\sin \theta \cos \theta}$ $= \frac{\sin \theta}{\cos \theta} = \tan \theta$	M1 M1A1 A1* (4) cso
(b)(i)	$\tan 15^\circ = \frac{1}{\sin 30^\circ} - \frac{\cos 30^\circ}{\sin 30^\circ}$ $\tan 15^\circ = \frac{1}{\frac{1}{2}} - \frac{\frac{\sqrt{3}}{2}}{\frac{1}{2}} = 2 - \sqrt{3}$	M1 A1* (3) cso
(b)(ii)	$\tan 2x = 1$ $2x = 45^\circ$ $2x = 45^\circ + 180^\circ$ $x = 22.5^\circ, 112.5^\circ, 202.5^\circ, 292.5^\circ$	M1 A1 M1 A1 (any two) A1 (5)
	Alt for (b)(i) $\tan 15^\circ = \tan(60^\circ - 45^\circ) \text{ or } \tan(45^\circ - 30^\circ)$ $\tan 15^\circ = \frac{\tan 60^\circ - \tan 45^\circ}{1 + \tan 60^\circ \tan 45^\circ} \text{ or } \frac{\tan 45^\circ - \tan 30^\circ}{1 + \tan 45^\circ \tan 30^\circ}$ $\tan 15^\circ = \frac{\sqrt{3} - 1}{1 + \sqrt{3}} \text{ or } \frac{1 - \frac{\sqrt{3}}{3}}{1 + \frac{\sqrt{3}}{3}}$ Rationalises to produce $\tan 15^\circ = 2 - \sqrt{3}$	12 Marks M1 M1 A1*

Question Number	Scheme	Marks
7 (a)	$x^2 - 9 = (x + 3)(x - 3)$ $\frac{4x - 5}{(2x + 1)(x - 3)} - \frac{2x}{(x + 3)(x - 3)}$ $= \frac{(4x - 5)(x + 3)}{(2x + 1)(x - 3)(x + 3)} - \frac{2x(2x + 1)}{(2x + 1)(x + 3)(x - 3)}$ $= \frac{5x - 15}{(2x + 1)(x - 3)(x + 3)}$ $= \frac{5(x - 3)}{(2x + 1)(x - 3)(x + 3)} = \frac{5}{(2x + 1)(x + 3)}$	B1 M1 M1A1 A1* (5)
(b)	$f(x) = \frac{5}{2x^2 + 7x + 3}$ $f'(x) = \frac{-5(4x + 7)}{(2x^2 + 7x + 3)^2}$ $f'(-1) = -\frac{15}{4}$ <p>Uses $m_1 m_2 = -1$ to give gradient of normal = $\frac{4}{15}$</p> $\frac{y - (-\frac{5}{2})}{(x - -1)} = \text{their } \frac{4}{15}$ $y + \frac{5}{2} = \frac{4}{15}(x + 1) \text{ or any equivalent form}$	M1M1A1 M1A1 M1 M1 A1 (8) 13 Marks

Question Number	Scheme	Marks
<p>8</p> <p>(a)</p> <p>(b)</p> <p>(c)</p>	$R^2 = 2^2 + 3^2$ $R = \sqrt{13} \text{ or } 3.61 \dots$ $\tan \alpha = \frac{3}{2}$ $\alpha = 0.983 \dots$ $f'(x) = 2e^{2x} \cos 3x - 3e^{2x} \sin 3x$ $= e^{2x} (2 \cos 3x - 3 \sin 3x)$ $= e^{2x} (R \cos(3x + \alpha))$ $= R e^{2x} \cos(3x + \alpha)$ $f'(x) = 0 \Rightarrow \cos(3x + \alpha) = 0$ $3x + \alpha = \frac{\pi}{2}$ $x = 0.196 \dots \quad \text{awrt } 0.20$	<p>M1 A1</p> <p>M1 A1</p> <p>(4)</p> <p>M1A1A1 M1 A1* cso</p> <p>(5)</p> <p>M1 M1 A1</p> <p>(3)</p> <p>12 Marks</p>
	<p>Alternative to part (c) \Rightarrow</p> $f'(x) = 0 \Rightarrow 2 \cos 3x - 3 \sin 3x = 0$ $\tan 3x = \frac{2}{3}$ $x = 0.196 \dots \quad \text{awrt } 0.20$	<p>M1 M1 A1</p> <p>(3)</p>