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1. A curve C has the equation $y^2 - 3y = x^3 + 8$.

(a) Find $\frac{dy}{dx}$ in terms of x and y .

(4)

(b) Hence find the gradient of C at the point where $y = 3$.

(3)



**January 2009
6666 Core Mathematics C4
Mark Scheme**

Question Number	Scheme	Marks
1	<p>(a) C: $y^2 - 3y = x^3 + 8$</p> <p>$\frac{dy}{dx}$ $\left\{ \frac{dy}{dx} \right\} \times 2y \frac{dy}{dx} - 3 \frac{dy}{dx} = 3x^2$</p> <p>$(2y-3) \frac{dy}{dx} = 3x^2$</p> <p>$\frac{dy}{dx} = \frac{3x^2}{2y-3}$</p>	<p>Differentiates implicitly to include either $\pm ky \frac{dy}{dx}$ or $\pm 3 \frac{dy}{dx}$. (Ignore $\left(\frac{dy}{dx} = \right)$.) M1</p> <p>Correct equation. A1</p> <p>A correct (condoning sign error) attempt to combine or factorise their '$2y \frac{dy}{dx} - 3 \frac{dy}{dx}$'. M1</p> <p>Can be implied.</p> <p style="text-align: right;">$\frac{3x^2}{2y-3}$ A1 oe</p>
(b)	<p>$y = 3 \Rightarrow 9 - 3(3) = x^3 + 8$</p> <p>$x^3 = -8 \Rightarrow \underline{x = -2}$</p> <p>$(-2, 3) \Rightarrow \frac{dy}{dx} = \frac{3(4)}{6-3} \Rightarrow \frac{dy}{dx} = 4$</p>	<p>Substitutes $y = 3$ into C. M1</p> <p>Only $\underline{x = -2}$ A1</p> <p>$\frac{dy}{dx} = 4$ from correct working.</p> <p>Also can be ft using their 'x' value and $y = 3$ in the correct part (a) of $\frac{dy}{dx} = \frac{3x^2}{2y-3}$ A1 $\sqrt{\quad}$</p>
<p>1(b) final A1 $\sqrt{\quad}$. Note if the candidate inserts their x value and $y = 3$ into $\frac{dy}{dx} = \frac{3x^2}{2y-3}$, then an answer of $\frac{dy}{dx} =$ their x^2, may indicate a correct follow through.</p>		<p>(3)</p> <p>[7]</p>

2.

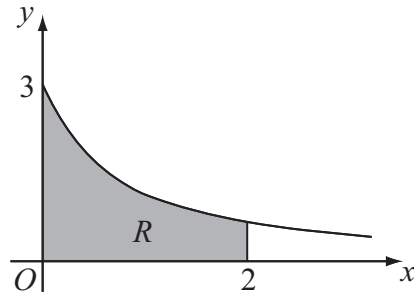


Figure 1

Figure 1 shows part of the curve $y = \frac{3}{\sqrt{1+4x}}$. The region R is bounded by the curve, the x -axis, and the lines $x = 0$ and $x = 2$, as shown shaded in Figure 1.

(a) Use integration to find the area of R . (4)

The region R is rotated 360° about the x -axis.

(b) Use integration to find the exact value of the volume of the solid formed. (5)



Question Number	Scheme	Marks
<p>2 (a)</p> <p>(b)</p>	<p> $\text{Area}(R) = \int_0^2 \frac{3}{\sqrt{1+4x}} dx = \int_0^2 3(1+4x)^{-\frac{1}{2}} dx$ $= \left[\frac{3(1+4x)^{\frac{1}{2}}}{\frac{1}{2} \cdot 4} \right]_0^2$ $= \left[\frac{3}{2}(1+4x)^{\frac{1}{2}} \right]_0^2$ $= \left(\frac{3}{2}\sqrt{9} \right) - \left(\frac{3}{2}(1) \right)$ $= \frac{9}{2} - \frac{3}{2} = \underline{3} \text{ (units)}^2$ <p>(Answer of 3 with no working scores M0A0M0A0.)</p> $\text{Volume} = \pi \int_0^2 \left(\frac{3}{\sqrt{1+4x}} \right)^2 dx$ $= (\pi) \int_0^2 \frac{9}{1+4x} dx$ $= (\pi) \left[\frac{9}{4} \ln 1+4x \right]_0^2$ $= (\pi) \left[\left(\frac{9}{4} \ln 9 \right) - \left(\frac{9}{4} \ln 1 \right) \right]$ <p>Note that $\ln 1$ can be implied as equal to 0.</p> <p>So Volume = $\frac{9}{4}\pi \ln 9$</p> <p>Note the answer must be a one term exact value. Note, also you can ignore subsequent working here.</p> </p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>(4)</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>dM1</p> <p>A1 oe isw</p> <p>(5)</p> <p>[9]</p>

3.

$$f(x) = \frac{27x^2 + 32x + 16}{(3x + 2)^2(1 - x)}, \quad |x| < \frac{2}{3}$$

Given that $f(x)$ can be expressed in the form

$$f(x) = \frac{A}{(3x + 2)} + \frac{B}{(3x + 2)^2} + \frac{C}{(1 - x)},$$

- (a) find the values of B and C and show that $A = 0$. (4)
- (b) Hence, or otherwise, find the series expansion of $f(x)$, in ascending powers of x , up to and including the term in x^2 . Simplify each term. (6)
- (c) Find the percentage error made in using the series expansion in part (b) to estimate the value of $f(0.2)$. Give your answer to 2 significant figures. (4)



Question Number	Scheme	Marks
<p>3 (a)</p>	$27x^2 + 32x + 16 \equiv A(3x + 2)(1 - x) + B(1 - x) + C(3x + 2)^2$ <p>$x = -\frac{2}{3}, \quad 12 - \frac{64}{3} + 16 = \left(\frac{5}{3}\right)B \Rightarrow \frac{20}{3} = \left(\frac{5}{3}\right)B \Rightarrow B = 4$</p> <p>$x = 1, \quad 27 + 32 + 16 = 25C \Rightarrow 75 = 25C \Rightarrow C = 3$</p> <p>Equate x^2: $27 = -3A + 9C \Rightarrow 27 = -3A + 27 \Rightarrow 0 = -3A \Rightarrow A = 0$</p> <p>$x = 0, \quad 16 = 2A + B + 4C \Rightarrow 16 = 2A + 4 + 12 \Rightarrow 0 = 2A \Rightarrow A = 0$</p>	<p>Forming this identity M1</p> <p>Substitutes either $x = -\frac{2}{3}$ or $x = 1$ into their identity or equates 3 terms or substitutes in values to write down three simultaneous equations. M1</p> <p>Both $B = 4$ and $C = 3$ A1</p> <p>(Note the A1 is dependent on both method marks in this part.)</p> <p>Compares coefficients or substitutes in a third x-value or uses simultaneous equations to show $A = 0$. B1</p> <p>(4)</p>
<p>(b)</p>	$f(x) = \frac{4}{(3x + 2)^2} + \frac{3}{(1 - x)}$ $= 4(3x + 2)^{-2} + 3(1 - x)^{-1}$ $= 4\left[2\left(1 + \frac{3}{2}x\right)^{-2}\right] + 3(1 - x)^{-1}$ $= 1\left(1 + \frac{3}{2}x\right)^{-2} + 3(1 - x)^{-1}$ $= 1\left\{1 + (-2)\left(\frac{3x}{2}\right) + \frac{(-2)(-3)}{2!}\left(\frac{3x}{2}\right)^2 + \dots\right\}$ $+ 3\left\{1 + (-1)(-x) + \frac{(-1)(-2)}{2!}(-x)^2 + \dots\right\}$ $= \left\{1 - 3x + \frac{27}{4}x^2 + \dots\right\} + 3\left\{1 + x + x^2 + \dots\right\}$ $= 4 + 0x + \frac{39}{4}x^2$	<p>Moving powers to top on any one of the two expressions M1</p> <p>Either $1 \pm (-2)\left(\frac{3x}{2}\right)$ or $1 \pm (-1)(-x)$ from either first or second expansions respectively dM1;</p> <p>Ignoring 1 and 3, any one correct {.....} expansion. A1</p> <p>Both {.....} correct. A1</p> <p>$4 + (0x) + \frac{39}{4}x^2$ A1; A1</p> <p>(6)</p>

Question Number	Scheme	Marks
(c)	<p>Actual = $f(0.2) = \frac{1.08 + 6.4 + 16}{(6.76)(0.8)}$ $= \frac{23.48}{5.408} = 4.341715976... = \frac{2935}{676}$</p> <p>Or</p> <p>Actual = $f(0.2) = \frac{4}{(3(0.2) + 2)^2} + \frac{3}{(1 - 0.2)}$ $= \frac{4}{6.76} + 3.75 = 4.341715976... = \frac{2935}{676}$</p> <p>Estimate = $f(0.2) = 4 + \frac{39}{4}(0.2)^2$ $= 4 + 0.39 = 4.39$</p> <p>%age error = $\frac{ 4.39 - 4.341715976... }{4.341715976...} \times 100$ $= 1.112095408... = 1.1\% (2sf)$</p>	<p>Attempt to find the actual value of $f(0.2)$ or seeing awrt 4.3 and believing it is candidate's actual $f(0.2)$.</p> <p>Candidates can also attempt to find the actual value by using $\frac{A}{(3x + 2)} + \frac{B}{(3x + 2)^2} + \frac{C}{(1 - x)}$ with their A, B and C.</p> <p>Attempt to find an estimate for $f(0.2)$ using their answer to (b)</p> <p>$\left \frac{\text{their estimate} - \text{actual}}{\text{actual}} \right \times 100$</p> <p>1.1%</p>
		<p>M1</p> <p>M1 $\sqrt{\quad}$</p> <p>M1</p> <p>A1 cao (4)</p> <p>[14]</p>

4. With respect to a fixed origin O the lines l_1 and l_2 are given by the equations

$$l_1: \mathbf{r} = \begin{pmatrix} 11 \\ 2 \\ 17 \end{pmatrix} + \lambda \begin{pmatrix} -2 \\ 1 \\ -4 \end{pmatrix} \quad l_2: \mathbf{r} = \begin{pmatrix} -5 \\ 11 \\ p \end{pmatrix} + \mu \begin{pmatrix} q \\ 2 \\ 2 \end{pmatrix}$$

where λ and μ are parameters and p and q are constants. Given that l_1 and l_2 are perpendicular,

(a) show that $q = -3$. (2)

Given further that l_1 and l_2 intersect, find

(b) the value of p , (6)

(c) the coordinates of the point of intersection. (2)

The point A lies on l_1 and has position vector $\begin{pmatrix} 9 \\ 3 \\ 13 \end{pmatrix}$. The point C lies on l_2 .

Given that a circle, with centre C , cuts the line l_1 at the points A and B ,

(d) find the position vector of B . (3)



Question Number	Scheme	Marks
<p>4 (a)</p> <p>$\mathbf{d}_1 = -2\mathbf{i} + \mathbf{j} - 4\mathbf{k}$, $\mathbf{d}_2 = q\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}$</p> <p>As $\left\{ \mathbf{d}_1 \bullet \mathbf{d}_2 = \begin{pmatrix} -2 \\ 1 \\ -4 \end{pmatrix} \bullet \begin{pmatrix} q \\ 2 \\ 2 \end{pmatrix} \right\} = \frac{(-2 \times q) + (1 \times 2) + (-4 \times 2)}$</p> <p>$\mathbf{d}_1 \bullet \mathbf{d}_2 = 0 \Rightarrow -2q + 2 - 8 = 0$ $-2q = 6 \Rightarrow \underline{q = -3}$ AG</p> <p>(b) Lines meet where:</p> <p>$\begin{pmatrix} 11 \\ 2 \\ 17 \end{pmatrix} + \lambda \begin{pmatrix} -2 \\ 1 \\ -4 \end{pmatrix} = \begin{pmatrix} -5 \\ 11 \\ p \end{pmatrix} + \mu \begin{pmatrix} q \\ 2 \\ 2 \end{pmatrix}$</p> <p>$\mathbf{i}: 11 - 2\lambda = -5 + q\mu$ (1) First two of $\mathbf{j}: 2 + \lambda = 11 + 2\mu$ (2) $\mathbf{k}: 17 - 4\lambda = p + 2\mu$ (3)</p> <p>(1) + 2(2) gives: $15 = 17 + \mu \Rightarrow \mu = -2$</p> <p>(2) gives: $2 + \lambda = 11 - 4 \Rightarrow \lambda = 5$</p> <p>(3) $\Rightarrow 17 - 4(5) = p + 2(-2)$ $\Rightarrow p = 17 - 20 + 4 \Rightarrow \underline{p = 1}$</p> <p>(c) $\mathbf{r} = \begin{pmatrix} 11 \\ 2 \\ 17 \end{pmatrix} + 5 \begin{pmatrix} -2 \\ 1 \\ -4 \end{pmatrix}$ or $\mathbf{r} = \begin{pmatrix} -5 \\ 11 \\ 1 \end{pmatrix} - 2 \begin{pmatrix} -3 \\ 2 \\ 2 \end{pmatrix}$</p> <p>Intersect at $\mathbf{r} = \begin{pmatrix} 1 \\ 7 \\ -3 \end{pmatrix}$ or $\underline{(1, 7, -3)}$</p>	<p>Apply dot product calculation between two direction vectors, ie. $\underline{(-2 \times q) + (1 \times 2) + (-4 \times 2)}$</p> <p>Sets $\mathbf{d}_1 \bullet \mathbf{d}_2 = 0$ and solves to find $\underline{q = -3}$</p> <p>Need to see equations (1) and (2). Condone one slip. (Note that $q = -3$.)</p> <p>Attempts to solve (1) and (2) to find one of either λ or μ Any one of $\underline{\lambda = 5}$ or $\underline{\mu = -2}$ Both $\underline{\lambda = 5}$ and $\underline{\mu = -2}$</p> <p>Attempt to substitute their λ and μ into their \mathbf{k} component to give an equation in p alone.</p> <p>$\underline{p = 1}$</p> <p>Substitutes their value of λ or μ into the correct line l_1 or l_2.</p> <p>$\begin{pmatrix} 1 \\ 7 \\ -3 \end{pmatrix}$ or $\underline{(1, 7, -3)}$</p>	<p>M1</p> <p>A1 cso</p> <p>(2)</p> <p>M1</p> <p>dM1</p> <p>A1</p> <p>A1</p> <p>ddM1</p> <p>A1 cso</p> <p>(6)</p> <p>M1</p> <p>A1</p> <p>(2)</p>

Question Number	Scheme	Marks
(d)	<p>Let $\vec{OX} = \mathbf{i} + 7\mathbf{j} - 3\mathbf{k}$ be point of intersection</p> $\vec{AX} = \vec{OX} - \vec{OA} = \begin{pmatrix} 1 \\ 7 \\ -3 \end{pmatrix} - \begin{pmatrix} 9 \\ 3 \\ 13 \end{pmatrix} = \begin{pmatrix} -8 \\ 4 \\ -16 \end{pmatrix}$ <p>Finding vector \vec{AX} by finding the difference between \vec{OX} and \vec{OA}. Can be ft using candidate's \vec{OX}.</p> $\vec{OB} = \vec{OA} + \vec{AB} = \vec{OA} + 2\vec{AX}$ $\vec{OB} = \begin{pmatrix} 9 \\ 3 \\ 13 \end{pmatrix} + 2 \begin{pmatrix} -8 \\ 4 \\ -16 \end{pmatrix} \qquad \begin{pmatrix} 9 \\ 3 \\ 13 \end{pmatrix} + 2 \begin{pmatrix} \text{their } \vec{AX} \end{pmatrix}$ <p>Hence, $\vec{OB} = \begin{pmatrix} -7 \\ 11 \\ -19 \end{pmatrix}$ or $\vec{OB} = \underline{-7\mathbf{i} + 11\mathbf{j} - 19\mathbf{k}}$ $\begin{pmatrix} -7 \\ 11 \\ -19 \end{pmatrix}$ or $\underline{-7\mathbf{i} + 11\mathbf{j} - 19\mathbf{k}}$ or $\underline{(-7, 11, -19)}$</p>	<p>M1 $\sqrt{\pm}$</p> <p>dM1 $\sqrt{}$</p> <p>A1</p> <p>(3)</p> <p>[13]</p>

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5.

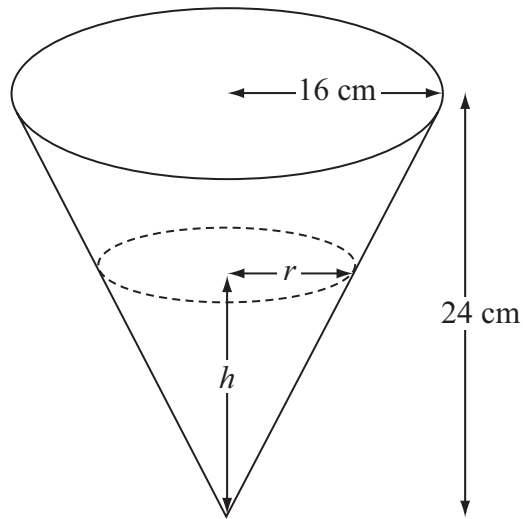


Figure 2

A container is made in the shape of a hollow inverted right circular cone. The height of the container is 24 cm and the radius is 16 cm, as shown in Figure 2. Water is flowing into the container. When the height of water is h cm, the surface of the water has radius r cm and the volume of water is V cm³.

(a) Show that $V = \frac{4\pi h^3}{27}$. (2)

[The volume V of a right circular cone with vertical height h and base radius r is given by the formula $V = \frac{1}{3}\pi r^2 h$.]

Water flows into the container at a rate of 8 cm³ s⁻¹.

(b) Find, in terms of π , the rate of change of h when $h = 12$. (5)



Question Number	Scheme	Marks
5	<p>(a) Similar triangles $\Rightarrow \frac{r}{h} = \frac{16}{24} \Rightarrow r = \frac{2h}{3}$</p> <p>$V = \frac{1}{3}\pi r^2 h = \frac{1}{3}\pi \left(\frac{2h}{3}\right)^2 h = \frac{4\pi h^3}{27}$ AG</p> <p>(b) From the question, $\frac{dV}{dt} = 8$</p> <p>$\frac{dV}{dh} = \frac{12\pi h^2}{27} = \frac{4\pi h^2}{9}$</p> <p>$\frac{dh}{dt} = \frac{dV}{dt} \div \frac{dV}{dh} = 8 \times \frac{9}{4\pi h^2} = \frac{18}{\pi h^2}$</p> <p>When $h = 12$, $\frac{dh}{dt} = \frac{18}{144\pi} = \frac{1}{8\pi}$</p> <p>Note the answer must be a one term exact value. Note, also you can ignore subsequent working after $\frac{18}{144\pi}$.</p>	<p>Uses similar triangles, ratios or trigonometry to find either one of these two expressions oe. M1</p> <p>Substitutes $r = \frac{2h}{3}$ into the formula for the volume of water V. A1</p> <p>(2)</p> <p>$\frac{dV}{dt} = 8$ B1</p> <p>$\frac{dV}{dh} = \frac{12\pi h^2}{27}$ or $\frac{4\pi h^2}{9}$ B1</p> <p>Candidate's $\frac{dV}{dt} \div \frac{dV}{dh}$; M1;</p> <p>$8 \div \left(\frac{12\pi h^2}{27}\right)$ or $8 \times \frac{9}{4\pi h^2}$ or $\frac{18}{\pi h^2}$ oe A1</p> <p>$\frac{18}{144\pi}$ or $\frac{1}{8\pi}$ A1 oe isw</p> <p>(5)</p> <p>[7]</p>

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6. (a) Find $\int \tan^2 x \, dx$. (2)

(b) Use integration by parts to find $\int \frac{1}{x^3} \ln x \, dx$. (4)

(c) Use the substitution $u = 1 + e^x$ to show that

$$\int \frac{e^{3x}}{1+e^x} dx = \frac{1}{2}e^{2x} - e^x + \ln(1+e^x) + k,$$

where k is a constant. (7)



Question Number	Scheme	Marks
6	<p>(a) $\int \tan^2 x \, dx$</p> <p>[NB: <u>$\sec^2 A = 1 + \tan^2 A$</u> gives <u>$\tan^2 A = \sec^2 A - 1$</u>]</p> <p>$= \int \sec^2 x - 1 \, dx$</p> <p>$= \underline{\tan x - x} (+ c)$</p> <p>(b) $\int \frac{1}{x^3} \ln x \, dx$</p> <p>$\left\{ \begin{array}{l} u = \ln x \Rightarrow \frac{du}{dx} = \frac{1}{x} \\ \frac{dv}{dx} = x^{-3} \Rightarrow v = \frac{x^{-2}}{-2} = -\frac{1}{2x^2} \end{array} \right\}$</p> <p>$= -\frac{1}{2x^2} \ln x - \int -\frac{1}{2x^2} \cdot \frac{1}{x} \, dx$</p> <p>$= -\frac{1}{2x^2} \ln x + \frac{1}{2} \int \frac{1}{x^3} \, dx$</p> <p>$= \underline{-\frac{1}{2x^2} \ln x + \frac{1}{2} \left(-\frac{1}{2x^2} \right)} (+ c)$</p>	<p>The correct <u>identity</u>.</p> <p>M1 oe</p> <p>Correct integration with/without + c</p> <p>A1</p> <p>(2)</p> <p>Use of ‘integration by parts’ formula in the correct direction.</p> <p>M1</p> <p>Correct direction means that $u = \ln x$.</p> <p>Correct expression.</p> <p>A1</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>An attempt to multiply through $\frac{k}{x^n}, n \in \mathbb{Z}, n \neq 2$ by $\frac{1}{x}$ and an attempt to ...</p> <p>... “integrate”(process the result);</p> </div> <p>M1</p> <p><u>correct solution</u> with/without + c</p> <p>A1 oe</p> <p>(4)</p>

Question Number	Scheme	Marks
(c)	$\int \frac{e^{3x}}{1+e^x} dx$ $\left\{ u = 1 + e^x \Rightarrow \frac{du}{dx} = e^x, \frac{dx}{du} = \frac{1}{e^x}, \frac{dx}{du} = \frac{1}{u-1} \right\}$ $= \int \frac{e^{2x} \cdot e^x}{1+e^x} dx = \int \frac{(u-1)^2 \cdot e^x}{u} \cdot \frac{1}{e^x} du$ <p>or $= \int \frac{(u-1)^3}{u} \cdot \frac{1}{(u-1)} du$</p> $= \int \frac{(u-1)^2}{u} du$ $= \int \frac{u^2 - 2u + 1}{u} du$ $= \int u - 2 + \frac{1}{u} du$ $= \frac{u^2}{2} - 2u + \ln u (+c)$ $= \frac{(1+e^x)^2}{2} - 2(1+e^x) + \ln(1+e^x) + c$ $= \frac{1}{2} + e^x + \frac{1}{2}e^{2x} - 2 - 2e^x + \ln(1+e^x) + c$ $= \frac{1}{2} + e^x + \frac{1}{2}e^{2x} - 2 - 2e^x + \ln(1+e^x) + c$ $= \frac{1}{2}e^{2x} - e^x + \ln(1+e^x) - \frac{3}{2} + c$ $= \frac{1}{2}e^{2x} - e^x + \ln(1+e^x) + k \quad \mathbf{AG}$	<p>Differentiating to find any one of the <u>three underlined</u></p> <p>Attempt to substitute for $e^{2x} = f(u)$, their $\frac{dx}{du} = \frac{1}{e^x}$ and $u = 1 + e^x$</p> <p>or $e^{3x} = f(u)$, their $\frac{dx}{du} = \frac{1}{u-1}$ and $u = 1 + e^x$.</p> <p>$\int \frac{(u-1)^2}{u} du$</p> <p>An attempt to multiply out their numerator to give at least three terms and divide through each term by u</p> <p>Correct integration with/without $+c$</p> <p>Substitutes $u = 1 + e^x$ back into their integrated expression with at least two terms.</p> <p>$\frac{1}{2}e^{2x} - e^x + \ln(1+e^x) + k$ must use a $+c$ and "$-\frac{3}{2}$" combined.</p> <p>B1</p> <p>M1*</p> <p>A1</p> <p>dM1*</p> <p>A1</p> <p>dM1*</p> <p>A1 cso</p> <p>(7)</p> <p>[13]</p>

Question Number	Scheme	Marks
<p>7 (a)</p> <p>(b)</p>	<p>At A, $x = -1 + 8 = 7$ & $y = (-1)^2 = 1 \Rightarrow A(7,1)$</p>	<p>B1</p>
	<p>$x = t^3 - 8t$, $y = t^2$,</p> <p>$\frac{dx}{dt} = 3t^2 - 8$, $\frac{dy}{dt} = 2t$</p> <p>$\therefore \frac{dy}{dx} = \frac{2t}{3t^2 - 8}$</p> <p>At A, $m(T) = \frac{2(-1)}{3(-1)^2 - 8} = \frac{-2}{3 - 8} = \frac{-2}{-5} = \frac{2}{5}$</p> <p>T: $y - (\text{their } 1) = m_T(x - (\text{their } 7))$</p> <p>or $1 = \frac{2}{5}(7) + c \Rightarrow c = 1 - \frac{14}{5} = -\frac{9}{5}$</p> <p>Hence T: $y = \frac{2}{5}x - \frac{9}{5}$</p> <p>gives T: $2x - 5y - 9 = 0$ AG</p>	<p>(1)</p> <p>M1</p> <p>A1</p> <p>Substitutes for t to give any of the four underlined oe:</p> <p>Finding an equation of a tangent with their point and their tangent gradient or finds c and uses $y = (\text{their gradient})x + "c"$.</p> <p>dM1</p> <p>A1 cso</p> <p>(5)</p>
<p>(c)</p>	<p>$2(t^3 - 8t) - 5t^2 - 9 = 0$</p> <p>$2t^3 - 5t^2 - 16t - 9 = 0$</p> <p>$(t + 1)\{(2t^2 - 7t - 9) = 0\}$</p> <p>$(t + 1)\{(t + 1)(2t - 9) = 0\}$</p> <p>$\{t = -1 \text{ (at A)}\} t = \frac{9}{2} \text{ at B}$</p> <p>$x = (\frac{9}{2})^2 - 8(\frac{9}{2}) = \frac{729}{8} - 36 = \frac{441}{8} = 55.125$ or awrt 55.1</p> <p>$y = (\frac{9}{2})^2 = \frac{81}{4} = 20.25$ or awrt 20.3</p> <p>Hence B($\frac{441}{8}, \frac{81}{4}$)</p>	<p>M1</p> <p>A1</p> <p>A realisation that $(t + 1)$ is a factor.</p> <p>$t = \frac{9}{2}$</p> <p>A1</p> <p>Candidate uses their value of t to find either the x or y coordinate</p> <p>One of either x or y correct.</p> <p>Both x and y correct.</p> <p>awrt</p> <p>(6)</p>

[12]