

Centre No.						Paper Reference							Surname	Initial(s)
Candidate No.						6	6	6	6	/	0	1	Signature	

Paper Reference(s)

6666/01

Edexcel GCE

Core Mathematics C4

Advanced

Monday 19 January 2009 – Afternoon

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

Materials required for examination

Mathematical Formulae (Green)

Items included with question papers

Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer for each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet ‘Mathematical Formulae and Statistical Tables’ is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 7 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.

You should show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

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- (a) Find $\frac{dy}{dx}$ in terms of x and y .

(4)

- (3)



January 2009
6666 Core Mathematics C4
Mark Scheme

Question Number	Scheme	Marks
1 (a)	<p>$C: y^2 - 3y = x^3 + 8$</p> <p>$\left\{ \frac{\cancel{dy}}{\cancel{dx}} \times \right\} 2y \frac{dy}{dx} - 3 \frac{dy}{dx} = 3x^2$</p> <p>$(2y-3) \frac{dy}{dx} = 3x^2$</p> <p>$\frac{dy}{dx} = \frac{3x^2}{2y-3}$</p>	<p>Differentiates implicitly to include either $\pm ky \frac{dy}{dx}$ or $\pm 3 \frac{dy}{dx}$. (Ignore $\left(\frac{dy}{dx} = \right)$.) M1</p> <p>Correct equation. A1</p> <p>A correct (condoning sign error) attempt to combine or factorise their '$2y \frac{dy}{dx} - 3 \frac{dy}{dx}$'. M1</p> <p>Can be implied.</p> <p>$\frac{3x^2}{2y-3}$ A1 oe</p>
(b)	<p>$y = 3 \Rightarrow 9 - 3(3) = x^3 + 8$</p> <p>$x^3 = -8 \Rightarrow \underline{x = -2}$</p> <p>$(-2, 3) \Rightarrow \frac{dy}{dx} = \frac{3(4)}{6-3} \Rightarrow \frac{dy}{dx} = 4$</p>	<p>Substitutes $y = 3$ into C. M1</p> <p>Only $\underline{x = -2}$ A1</p> <p>$\frac{dy}{dx} = 4$ from correct working.</p> <p>Also can be ft using their 'x' value and $y = 3$ in the correct part (a) of $\frac{dy}{dx} = \frac{3x^2}{2y-3}$ A1 \sqrt</p>
<p>1(b) final A1 \sqrt. Note if the candidate inserts their x value and $y = 3$ into $\frac{dy}{dx} = \frac{3x^2}{2y-3}$, then an answer of $\frac{dy}{dx} =$ their x^2, may indicate a correct follow through.</p>		(3)
		[7]

2.

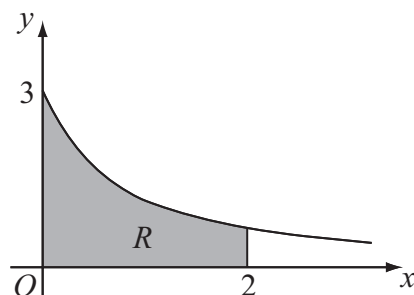


Figure 1

Figure 1 shows part of the curve $y = \frac{3}{\sqrt{1+4x}}$. The region R is bounded by the curve, the x -axis, and the lines $x = 0$ and $x = 2$, as shown shaded in Figure 1.

- (a) Use integration to find the area of R .

(4)

The region R is rotated 360° about the x -axis.

- (b) Use integration to find the exact value of the volume of the solid formed.

(5)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question Number	Scheme	Marks
2 (a)	$\text{Area}(R) = \int_0^2 \frac{3}{\sqrt{1+4x}} dx = \int_0^2 3(1+4x)^{-\frac{1}{2}} dx$ $= \left[\frac{3(1+4x)^{\frac{1}{2}}}{\frac{1}{2} \cdot 4} \right]_0^2$ $= \left[\frac{3}{2}(1+4x)^{\frac{1}{2}} \right]_0^2$ $= \left(\frac{3}{2}\sqrt{9} \right) - \left(\frac{3}{2}(1) \right)$ $= \frac{9}{2} - \frac{3}{2} = \underline{3} \text{ (units)}^2$ <p>(Answer of 3 with no working scores M0A0M0A0.)</p>	<p><i>Integrating</i> $3(1+4x)^{-\frac{1}{2}}$ to give $\pm k(1+4x)^{\frac{1}{2}}$. M1</p> <p><u>Correct integration.</u> A1 Ignore limits.</p> <p>Substitutes limits of 2 and 0 into a changed function and subtracts the correct way round. M1</p> <p><u>3</u> A1</p> <p>(4)</p>
(b)	$\text{Volume} = \pi \int_0^2 \left(\frac{3}{\sqrt{1+4x}} \right)^2 dx$ $= (\pi) \int_0^2 \frac{9}{1+4x} dx$ $= (\pi) \left[\frac{9}{4} \ln 1+4x \right]_0^2$ $= (\pi) \left[\left(\frac{9}{4} \ln 9 \right) - \left(\frac{9}{4} \ln 1 \right) \right]$ <p>Note that $\ln 1$ can be implied as equal to 0.</p> <p>So Volume = $\frac{9}{4} \pi \ln 9$</p> <p>Note the answer must be a one term exact value. Note, also you can ignore subsequent working here.</p>	<p>Use of $V = \pi \int y^2 dx$. B1</p> <p>Can be implied. Ignore limits and dx.</p> <p>$\pm k \ln 1+4x$ M1 $\frac{9}{4} \ln 1+4x$ A1</p> <p>Substitutes limits of 2 and 0 and subtracts the correct way round. dM1</p> <p>$\frac{9}{4} \pi \ln 9$ or $\frac{9}{2} \pi \ln 3$ or $\frac{18}{4} \pi \ln 3$ A1 oe isw Note that = $\frac{9}{4} \pi \ln 9 + c$ (oe.) would be awarded the final A0. (5)</p> <p>[9]</p>

3.

$$f(x) = \frac{27x^2 + 32x + 16}{(3x + 2)^2(1 - x)}, \quad |x| < \frac{2}{3}$$

Given that $f(x)$ can be expressed in the form

$$f(x) = \frac{A}{(3x+2)} + \frac{B}{(3x+2)^2} + \frac{C}{(1-x)},$$

- (a) find the values of B and C and show that $A = 0$. (4)
- (b) Hence, or otherwise, find the series expansion of $f(x)$, in ascending powers of x , up to and including the term in x^2 . Simplify each term. (6)
- (c) Find the percentage error made in using the series expansion in part (b) to estimate the value of $f(0.2)$. Give your answer to 2 significant figures. (4)



Question Number	Scheme	Marks
3 (a)	$27x^2 + 32x + 16 \equiv A(3x+2)(1-x) + B(1-x) + C(3x+2)^2$ <p>Forming this identity</p> <p>Substitutes either $x = -\frac{2}{3}$ or $x = 1$ into their identity or equates 3 terms or substitutes in values to write down three simultaneous equations. Both $B = 4$ and $C = 3$ (Note the A1 is dependent on both method marks in this part.)</p> <p>Equate x^2: $27 = -3A + 9C \Rightarrow 27 = -3A + 27 \Rightarrow 0 = -3A \Rightarrow A = 0$</p> <p>$x = 0$, $16 = 2A + B + 4C \Rightarrow 16 = 2A + 4 + 12 \Rightarrow 0 = 2A \Rightarrow A = 0$</p> <p>Compares coefficients or substitutes in a third x-value or uses simultaneous equations to show $A = 0$.</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>(4)</p>
(b)	$f(x) = \frac{4}{(3x+2)^2} + \frac{3}{(1-x)}$ $= 4(3x+2)^{-2} + 3(1-x)^{-1}$ $= 4\left[2\left(1+\frac{3}{2}x\right)^{-2}\right] + 3(1-x)^{-1}$ $= 1\left(1+\frac{3}{2}x\right)^{-2} + 3(1-x)^{-1}$ $= 1\left\{1 + (-2)\left(\frac{3x}{2}\right) + \frac{(-2)(-3)}{2!}\left(\frac{3x}{2}\right)^2 + \dots\right\}$ $+ 3\left\{1 + (-1)(-x) + \frac{(-1)(-2)}{2!}(-x)^2 + \dots\right\}$ $= \left\{1 - 3x + \frac{27}{4}x^2 + \dots\right\} + 3\left\{1 + x + x^2 + \dots\right\}$ $= 4 + 0x + \frac{39}{4}x^2$ <p>Moving powers to top on any one of the two expressions</p> <p>Either $1 \pm (-2)\left(\frac{3x}{2}\right)$ or $1 \pm (-1)(-x)$ from either first or second expansions respectively Ignoring 1 and 3, any one correct $\{\dots\}$ expansion. Both $\{\dots\}$ correct.</p>	<p>M1</p> <p>dM1;</p> <p>A1</p> <p>A1</p> <p>A1; A1</p> <p>(6)</p>

Question Number	Scheme	Marks
(c)	<p>Actual = $f(0.2) = \frac{1.08 + 6.4 + 16}{(6.76)(0.8)}$</p> <p>$= \frac{23.48}{5.408} = 4.341715976... = \frac{2935}{676}$</p> <p>Or</p> <p>Actual = $f(0.2) = \frac{4}{(3(0.2) + 2)^2} + \frac{3}{(1 - 0.2)}$</p> <p>$= \frac{4}{6.76} + 3.75 = 4.341715976... = \frac{2935}{676}$</p> <p>Estimate = $f(0.2) = 4 + \frac{39}{4}(0.2)^2$</p> <p>$= 4 + 0.39 = 4.39$</p> <p>%age error = $\frac{ 4.39 - 4.341715976... }{4.341715976...} \times 100$</p> <p>$= 1.112095408... = 1.1\%(2sf)$</p>	<p>Attempt to find the actual value of $f(0.2)$ or seeing awrt 4.3 and believing it is candidate's actual $f(0.2)$.</p> <p>Candidates can also attempt to find the actual value by using $\frac{A}{(3x + 2)} + \frac{B}{(3x + 2)^2} + \frac{C}{(1 - x)}$ with their A, B and C.</p> <p>Attempt to find an estimate for $f(0.2)$ using their answer to (b)</p> <p>$\left \frac{\text{their estimate} - \text{actual}}{\text{actual}} \right \times 100$</p> <p>1.1%</p> <p>M1</p> <p>M1 $\sqrt{}$</p> <p>M1</p> <p>A1 cao (4)</p> <p>[14]</p>

4. With respect to a fixed origin O the lines l_1 and l_2 are given by the equations

$$l_1: \quad \mathbf{r} = \begin{pmatrix} 11 \\ 2 \\ 17 \end{pmatrix} + \lambda \begin{pmatrix} -2 \\ 1 \\ -4 \end{pmatrix} \qquad l_2: \quad \mathbf{r} = \begin{pmatrix} -5 \\ 11 \\ p \end{pmatrix} + \mu \begin{pmatrix} q \\ 2 \\ 2 \end{pmatrix}$$

(a) show that $q = -3$.

(2)

Given further that l_1 and l_2 intersect, find

(b) the value of p ,

(6)

(c) the coordinates of the point of intersection.

(2)

The point A lies on l_1 and has position vector $\begin{pmatrix} 9 \\ 3 \\ 13 \end{pmatrix}$. The point C lies on l_2 .

Given that a circle, with centre C , cuts the line l_1 at the points A and B ,

(d) find the position vector of B .

(3)



Question Number	Scheme	Marks
4 (a)	$\mathbf{d}_1 = -2\mathbf{i} + \mathbf{j} - 4\mathbf{k}$, $\mathbf{d}_2 = q\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}$ As $\left\{ \mathbf{d}_1 \bullet \mathbf{d}_2 = \begin{pmatrix} -2 \\ 1 \\ -4 \end{pmatrix} \bullet \begin{pmatrix} q \\ 2 \\ 2 \end{pmatrix} \right\} = \underline{(-2 \times q) + (1 \times 2) + (-4 \times 2)}$ $\mathbf{d}_1 \bullet \mathbf{d}_2 = 0 \Rightarrow -2q + 2 - 8 = 0$ $-2q = 6 \Rightarrow \underline{q = -3}$ AG	M1 A1 cso (2)
(b)	Lines meet where: $\begin{pmatrix} 11 \\ 2 \\ 17 \end{pmatrix} + \lambda \begin{pmatrix} -2 \\ 1 \\ -4 \end{pmatrix} = \begin{pmatrix} -5 \\ 11 \\ p \end{pmatrix} + \mu \begin{pmatrix} q \\ 2 \\ 2 \end{pmatrix}$ $\mathbf{i}: 11 - 2\lambda = -5 + q\mu$ (1) First two of $\mathbf{j}: 2 + \lambda = 11 + 2\mu$ (2) $\mathbf{k}: 17 - 4\lambda = p + 2\mu$ (3)	M1 dM1 A1 A1
	$(1) + 2(2)$ gives: $15 = 17 + \mu \Rightarrow \mu = -2$ (2) gives: $2 + \lambda = 11 - 4 \Rightarrow \lambda = 5$	Attempts to solve (1) and (2) to find one of either λ or μ Any one of $\underline{\lambda = 5}$ or $\underline{\mu = -2}$ Both $\underline{\lambda = 5}$ and $\underline{\mu = -2}$
	$(3) \Rightarrow 17 - 4(5) = p + 2(-2)$ $\Rightarrow p = 17 - 20 + 4 \Rightarrow \underline{p = 1}$	Attempt to substitute their λ and μ into their \mathbf{k} component to give an equation in p alone. $\underline{p = 1}$ A1 cso (6)
(c)	$\mathbf{r} = \begin{pmatrix} 11 \\ 2 \\ 17 \end{pmatrix} + 5 \begin{pmatrix} -2 \\ 1 \\ -4 \end{pmatrix}$ or $\mathbf{r} = \begin{pmatrix} -5 \\ 11 \\ 1 \end{pmatrix} - 2 \begin{pmatrix} -3 \\ 2 \\ 2 \end{pmatrix}$ Intersect at $\mathbf{r} = \begin{pmatrix} 1 \\ 7 \\ -3 \end{pmatrix}$ or $\underline{(1, 7, -3)}$	M1 A1 (2)

Question Number	Scheme	Marks
(d)	<p>Let $\vec{OX} = \mathbf{i} + 7\mathbf{j} - 3\mathbf{k}$ be point of intersection</p> $\vec{AX} = \vec{OX} - \vec{OA} = \begin{pmatrix} 1 \\ 7 \\ -3 \end{pmatrix} - \begin{pmatrix} 9 \\ 3 \\ 13 \end{pmatrix} = \begin{pmatrix} -8 \\ 4 \\ -16 \end{pmatrix}$ <p>Finding vector \vec{AX} by finding the difference between \vec{OX} and \vec{OA}. Can be ft using candidate's \vec{OX}.</p> $\vec{OB} = \vec{OA} + \vec{AB} = \vec{OA} + 2\vec{AX}$ $\vec{OB} = \begin{pmatrix} 9 \\ 3 \\ 13 \end{pmatrix} + 2 \begin{pmatrix} -8 \\ 4 \\ -16 \end{pmatrix}$ $\text{Hence, } \vec{OB} = \begin{pmatrix} -7 \\ 11 \\ -19 \end{pmatrix} \text{ or } \vec{OB} = \underline{-7\mathbf{i} + 11\mathbf{j} - 19\mathbf{k}}$	<p>M1 $\sqrt{\pm}$</p> <p>dM1 $\sqrt{}$</p> <p>A1</p> <p>(3)</p> <p>[13]</p>

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The diagram shows an inverted cone with a smaller inverted cone inside it. The outer cone has a radius of 16 cm and a height of 24 cm. The inner cone has a radius labeled r and a height labeled h .

Figure 2

A container is made in the shape of a hollow inverted right circular cone. The height of the container is 24 cm and the radius is 16 cm, as shown in Figure 2. Water is flowing into the container. When the height of water is h cm, the surface of the water has radius r cm and the volume of water is V cm³.

(a) Show that $V = \frac{4\pi h^3}{27}$. (2)

[The volume V of a right circular cone with vertical height h and base radius r is given by the formula $V = \frac{1}{3}\pi r^2 h$.]

Water flows into the container at a rate of $8 \text{ cm}^3 \text{ s}^{-1}$.

(b) Find, in terms of π , the rate of change of h when $h = 12$. (5)

[illegible]

Question Number	Scheme	Marks
5	<p>(a) Similar triangles $\Rightarrow \frac{r}{h} = \frac{16}{24} \Rightarrow r = \frac{2h}{3}$</p> <p>$V = \frac{1}{3}\pi r^2 h = \frac{1}{3}\pi \left(\frac{2h}{3}\right)^2 h = \frac{4\pi h^3}{27}$ AG</p> <p>(b) From the question, $\frac{dV}{dt} = 8$</p> <p>$\frac{dV}{dh} = \frac{12\pi h^2}{27} = \frac{4\pi h^2}{9}$</p> <p>$\frac{dh}{dt} = \frac{dV}{dt} \div \frac{dV}{dh} = 8 \times \frac{9}{4\pi h^2} = \frac{18}{\pi h^2}$</p> <p>When $h = 12$, $\frac{dh}{dt} = \frac{18}{144\pi} = \frac{1}{8\pi}$</p> <p>Note the answer must be a one term exact value. Note, also you can ignore subsequent working after $\frac{18}{144\pi}$.</p>	<p>M1</p> <p>A1</p> <p>(2)</p> <p>B1</p> <p>B1</p> <p>M1;</p> <p>A1</p> <p>A1 oe isw</p> <p>(5)</p> <p>[7]</p>

6. (a) Find $\int \tan^2 x \, dx$. (2)

(b) Use integration by parts to find $\int \frac{1}{x^3} \ln x \, dx$.

(c) Use the substitution $u = 1 + e^x$ to show that

$$\int \frac{e^{3x}}{1+e^x} dx = \frac{1}{2}e^{2x} - e^x + \ln(1+e^x) + k,$$

where k is a constant. (7)

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Question Number	Scheme	Marks
6	<p>(a) $\int \tan^2 x \, dx$</p> <p>$\left[NB: \underline{\sec^2 A = 1 + \tan^2 A} \text{ gives } \underline{\tan^2 A = \sec^2 A - 1} \right]$</p> <p>$= \int \sec^2 x - 1 \, dx$</p> <p>$= \underline{\tan x - x} (+ c)$</p> <p>(b) $\int \frac{1}{x^3} \ln x \, dx$</p> <p>$\left\{ \begin{array}{l} u = \ln x \Rightarrow \frac{du}{dx} = \frac{1}{x} \\ \frac{dv}{dx} = x^{-3} \Rightarrow v = \frac{x^{-2}}{-2} = \frac{-1}{2x^2} \end{array} \right\}$</p> <p>$= -\frac{1}{2x^2} \ln x - \int -\frac{1}{2x^2} \cdot \frac{1}{x} \, dx$</p> <p>$= -\frac{1}{2x^2} \ln x + \frac{1}{2} \int \frac{1}{x^3} \, dx$</p> <p>$= \underline{-\frac{1}{2x^2} \ln x + \frac{1}{2} \left(-\frac{1}{2x^2} \right)} (+ c)$</p>	<p>M1 oe</p> <p>A1</p> <p>(2)</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 oe</p> <p>(4)</p>

The correct underlined identity.

Correct integration with/without + c

Use of 'integration by parts' formula in the correct direction.
Correct direction means that $u = \ln x$.
Correct expression.

An attempt to multiply through $\frac{k}{x^n}, n \in \mathbb{Z}, n \neq 2$ by $\frac{1}{x}$ and an attempt to ...
... "integrate"(process the result);

correct solution with/without + c

Question Number	Scheme	Marks
(c)	$\int \frac{e^{3x}}{1+e^x} dx$ $\left\{ u = 1 + e^x \Rightarrow \frac{du}{dx} = e^x, \frac{dx}{du} = \frac{1}{e^x}, \frac{dx}{du} = \frac{1}{u-1} \right\}$ $= \int \frac{e^{2x} \cdot e^x}{1+e^x} dx = \int \frac{(u-1)^2 \cdot e^x}{u} \cdot \frac{1}{e^x} du$ <p>or $= \int \frac{(u-1)^3}{u} \cdot \frac{1}{(u-1)} du$</p> $= \int \frac{(u-1)^2}{u} du$ $= \int \frac{u^2 - 2u + 1}{u} du$ $= \int u - 2 + \frac{1}{u} du$ $= \frac{u^2}{2} - 2u + \ln u (+c)$ $= \frac{(1+e^x)^2}{2} - 2(1+e^x) + \ln(1+e^x) + c$ $= \frac{1}{2} + e^x + \frac{1}{2}e^{2x} - 2 - 2e^x + \ln(1+e^x) + c$ $= \frac{1}{2} + e^x + \frac{1}{2}e^{2x} - 2 - 2e^x + \ln(1+e^x) + c$ $= \frac{1}{2}e^{2x} - e^x + \ln(1+e^x) - \frac{3}{2} + c$ $= \frac{1}{2}e^{2x} - e^x + \ln(1+e^x) + k \quad \text{AG}$	<p>Differentiating to find any one of the <u>three underlined</u></p> <p>Attempt to substitute for $e^{2x} = f(u)$, their $\frac{dx}{du} = \frac{1}{e^x}$ and $u = 1 + e^x$ or $e^{3x} = f(u)$, their $\frac{dx}{du} = \frac{1}{u-1}$ and $u = 1 + e^x$.</p> <p>$\int \frac{(u-1)^2}{u} du$</p> <p>An attempt to multiply out their numerator to give at least three terms and divide through each term by u</p> <p>Correct integration with/without $+c$</p> <p>Substitutes $u = 1 + e^x$ back into their integrated expression with at least two terms.</p> <p>$\frac{1}{2}e^{2x} - e^x + \ln(1+e^x) + k$ must use a $+c$ and "$-\frac{3}{2}$" combined.</p> <p>B1</p> <p>M1*</p> <p>A1</p> <p>dM1*</p> <p>A1</p> <p>dM1*</p> <p>A1 cso (7)</p> <p>[13]</p>

7.

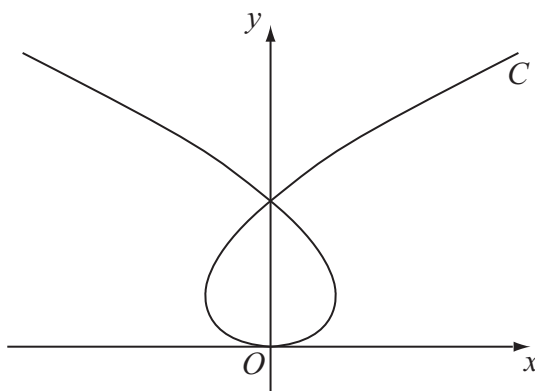


Figure 3

The curve C shown in Figure 3 has parametric equations

$$x = t^3 - 8t, \quad y = t^2$$

where t is a parameter. Given that the point A has parameter $t = -1$,

- (a) find the coordinates of A .

(1)

The line l is the tangent to C at A .

- (b) Show that an equation for l is $2x - 5y - 9 = 0$.

(5)

The line l also intersects the curve at the point B .

- (c) Find the coordinates of B .

(6)



Question Number	Scheme	Marks
7	<p>(a) At A, $x = -1 + 8 = 7$ & $y = (-1)^2 = 1 \Rightarrow A(7,1)$ $A(7,1)$</p> <p>(b) $x = t^3 - 8t$, $y = t^2$,</p> $\frac{dx}{dt} = 3t^2 - 8, \quad \frac{dy}{dt} = 2t$ $\therefore \frac{dy}{dx} = \frac{2t}{3t^2 - 8}$ <p style="text-align: right;">Their $\frac{dy}{dt}$ divided by their $\frac{dx}{dt}$ M1</p> <p style="text-align: right;">Correct $\frac{dy}{dx}$ A1</p> <p>At A, $m(T) = \frac{2(-1)}{3(-1)^2 - 8} = \frac{-2}{3 - 8} = \frac{-2}{-5} = \frac{2}{5}$ Substitutes for t to give any of the four underlined oe:</p> <p>T: $y - (\text{their } 1) = m_T(x - (\text{their } 7))$ Finding an equation of a tangent with their point and their tangent gradient or finds c and uses $y = (\text{their gradient})x + "c"$.</p> <p>or $1 = \frac{2}{5}(7) + c \Rightarrow c = 1 - \frac{14}{5} = -\frac{9}{5}$ dM1</p> <p>Hence T: $y = \frac{2}{5}x - \frac{9}{5}$</p> <p>gives T: $\underline{2x - 5y - 9 = 0}$ AG $\underline{2x - 5y - 9 = 0}$ A1 cso (5)</p> <p>(c) $2(t^3 - 8t) - 5t^2 - 9 = 0$ Substitution of both $x = t^3 - 8t$ and $y = t^2$ into T M1</p> $2t^3 - 5t^2 - 16t - 9 = 0$ <p>$(t+1)\{(2t^2 - 7t - 9) = 0\}$ A realisation that $(t+1)$ is a factor. dM1</p> <p>$(t+1)\{(t+1)(2t-9) = 0\}$</p> <p>$\{t = -1 \text{ (at A)}\} \quad t = \frac{9}{2} \text{ at B}$ $t = \frac{9}{2}$ A1</p> <p>$x = \left(\frac{9}{2}\right)^2 - 8\left(\frac{9}{2}\right) = \frac{729}{8} - 36 = \frac{441}{8} = 55.125$ or awrt 55.1 Candidate uses their value of t to find either the x or y coordinate ddM1</p> <p>$y = \left(\frac{9}{2}\right)^2 = \frac{81}{4} = 20.25$ or awrt 20.3 One of either x or y correct. A1</p> <p style="text-align: right;">Both x and y correct.</p> <p>Hence B $\left(\frac{441}{8}, \frac{81}{4}\right)$ awrt A1</p>	<p>B1</p> <p>(1)</p> <p>M1</p> <p>A1</p> <p>dM1</p> <p>A1 cso (5)</p> <p>M1</p> <p>dM1</p> <p>A1</p> <p>ddM1</p> <p>A1</p> <p>(6)</p> <p>[12]</p>