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Mathematics C4

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Question

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Centre No.					Pape	er Refer	ence			Surname	Initial(s)
Candidate No.			6	6	6	6	/	0	1	Signature	

Paper Reference(s)

6666/01

Edexcel GCE

Core Mathematics C4 Advanced

Wednesday 26 January 2011 – Afternoon

Time: 1 hour 30 minutes

Materials required for examination
Mathematical Formulae (Pink)Items included with question papers
Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer to each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 7 questions in this question paper. The total mark for this paper is 75.

There are 24 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

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$\int_0^{\frac{\pi}{2}} x \sin 2x \mathrm{d}x$	
	(6)

Past Paper (Mark Scheme)

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January 2011 Core Mathematics C4 6666 Mark Scheme

Question Number	Scheme	Marks
1.	$\int x \sin 2x dx = -\frac{x \cos 2x}{2} + \int \frac{\cos 2x}{2} dx$ $= \dots + \frac{\sin 2x}{4}$ $\left[\dots \right]_0^{\frac{\pi}{2}} = \frac{\pi}{4}$	M1 A1 A1 M1 M1 A1
		[6]
2.	$\frac{dI}{dt} = -16\ln(0.5)0.5^{t}$ At $t = 3$ $\frac{dI}{dt} = -16\ln(0.5)0.5^{3}$ $= -2\ln 0.5 = \ln 4$	M1 A1 M1 M1 A1
		[5]

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The current, I amps, in an electric circuit at time t seconds is given by	
$I = 16 - 16(0.5)^t, t \geqslant 0$	
Use differentiation to find the value of $\frac{dI}{dt}$ when $t = 3$.	
Give your answer in the form $\ln a$, where a is a constant.	
	(5)

Past Paper (Mark Scheme)

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January 2011 Core Mathematics C4 6666 Mark Scheme

Question Number	Scheme	Marks
1.	$\int x \sin 2x dx = -\frac{x \cos 2x}{2} + \int \frac{\cos 2x}{2} dx$ $= \dots + \frac{\sin 2x}{4}$ $\left[\dots \right]_0^{\frac{\pi}{2}} = \frac{\pi}{4}$	M1 A1 A1 M1 M1 A1
		[6]
2.	$\frac{dI}{dt} = -16\ln(0.5)0.5^{t}$ At $t = 3$ $\frac{dI}{dt} = -16\ln(0.5)0.5^{3}$ $= -2\ln 0.5 = \ln 4$	M1 A1 M1 M1 A1
		[5]

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3. (a) Express $\frac{5}{(x-1)(3x+2)}$ in partial fractions.

(3)

(b) Hence find $\int \frac{5}{(x-1)(3x+2)} dx$, where x > 1.

(3)

(c) Find the particular solution of the differential equation

$$(x-1)(3x+2)\frac{dy}{dx} = 5y, \quad x > 1,$$

for which y = 8 at x = 2. Give your answer in the form y = f(x).

(6)

Past Paper (Mark Scheme)

2	2	2	2
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Question Number	Scheme	Marks
3. (a)	$\frac{5}{(x-1)(3x+2)} = \frac{A}{x-1} + \frac{B}{3x+2}$ $5 = A(3x+2) + B(x-1)$	
	$x \to 1 \qquad 5 = 5A \implies A = 1$	M1 A1
	$(x + 1)(3x + 2) + x + 1 + 3x + 2$ $5 = A(3x + 2) + B(x - 1)$ $x \to 1$ $5 = 5A \implies A = 1$ $x \to -\frac{2}{3}$ $5 = -\frac{5}{3}B \implies B = -3$	A1 (3)
(b)	$\int \frac{5}{(x-1)(3x+2)} dx = \int \left(\frac{1}{x-1} - \frac{3}{3x+2}\right) dx$	
	$= \ln(x-1) - \ln(3x+2) (+C) $ ft constants	M1 A1ft A1ft
		(3)
(c)	$\int \frac{5}{(x-1)(3x+2)} dx = \int \left(\frac{1}{y}\right) dy$	M1
	$\ln(x-1) - \ln(3x+2) = \ln y (+C)$	M1 A1
	$y = \frac{K(x-1)}{3x+2}$ depends on first two Ms in (c)	M1 dep
	Using $(2, 8)$ $8 = \frac{K}{8}$ depends on first two Ms in (c)	M1 dep
	$y = \frac{64(x-1)}{3x+2}$	A1 (6)
		[12]

 (b) Find a vector equation of <i>l</i>. (c) The point <i>C</i> has position vector 2i + pj - 4k with respect to <i>O</i>, where <i>p</i> is a constant. Given that <i>AC</i> is perpendicular to <i>l</i>, find (d) the distance <i>AC</i>. 	has
 (b) Find a vector equation of l. (c) The point C has position vector 2i + pj-4k with respect to O, where p is a constant. Given that AC is perpendicular to l, find (d) the distance AC. 	
 (b) Find a vector equation of l. (c) The point C has position vector 2i + pj-4k with respect to O, where p is a constant. Given that AC is perpendicular to l, find (d) the distance AC. 	
The point C has position vector $2\mathbf{i} + p\mathbf{j} - 4\mathbf{k}$ with respect to O, where p is a constant. Given that AC is perpendicular to l, find (c) the value of p, (d) the distance AC.	(2)
The point C has position vector $2\mathbf{i} + p\mathbf{j} - 4\mathbf{k}$ with respect to O, where p is a constant. Given that AC is perpendicular to l, find (c) the value of p, (d) the distance AC.	
Given that AC is perpendicular to l , find (c) the value of p , (d) the distance AC .	(2)
Given that AC is perpendicular to l , find (c) the value of p , (d) the distance AC .	
(d) the distance AC.	
(d) the distance AC.	
	(4)
	(2)

Mathematics C4

Past Paper (Mark Scheme)

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Question Number	Scheme		Marks	
4. (a)	$\overrightarrow{AB} = -2\mathbf{i} + 2\mathbf{j} - \mathbf{k} - (\mathbf{i} - 3\mathbf{j} + 2\mathbf{k}) = -3\mathbf{i} + 5\mathbf{j} - 3\mathbf{k}$		M1 A1	(2)
(b)	$\mathbf{r} = \mathbf{i} - 3\mathbf{j} + 2\mathbf{k} + \lambda \left(-3\mathbf{i} + 5\mathbf{j} - 3\mathbf{k} \right)$ or $\mathbf{r} = -2\mathbf{i} + 2\mathbf{j} - \mathbf{k} + \lambda \left(-3\mathbf{i} + 5\mathbf{j} - 3\mathbf{k} \right)$		M1 A1ft	(2)
(c)	$\overrightarrow{AC} = 2\mathbf{i} + p\mathbf{j} - 4\mathbf{k} - (\mathbf{i} - 3\mathbf{j} + 2\mathbf{k})$ $= \mathbf{i} + (p+3)\mathbf{j} - 6\mathbf{k}$	or \overrightarrow{CA}	B1	
	$\overrightarrow{AC}.\overrightarrow{AB} = \begin{pmatrix} 1 \\ p+3 \\ -6 \end{pmatrix} \cdot \begin{pmatrix} -3 \\ 5 \\ -3 \end{pmatrix} = 0$ $-3+5p+15+18=0$		M1	
	Leading to $p = -6$		M1 A1	(4)
(d)	$AC^{2} = (2-1)^{2} + (-6+3)^{2} + (-4-2)^{2} (=46)$ $AC = \sqrt{46}$	accept awrt 6.8	M1 A1	
				(2) [10]

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5. (a) Use the binomial theorem to expand

$$(2-3x)^{-2}$$
, $|x|<\frac{2}{3}$,

in ascending powers of x, up to and including the term in x^3 . Give each coefficient as a simplified fraction.

(5)

$$f(x) = \frac{a+bx}{(2-3x)^2}$$
, $|x| < \frac{2}{3}$, where a and b are constants.

In the binomial expansion of f(x), in ascending powers of x, the coefficient of x is 0 and the coefficient of x^2 is $\frac{9}{16}$. Find

(b) the value of a and the value of b,

(5)

(c	;) t	the coefficient	of x^3 ,	giving	your ans	swer as a	simplified	fraction.	

(3)

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Question Number	Scheme	Marks	;
5. (a)	$(2-3x)^{-2} = 2^{-2} \left(1 - \frac{3}{2}x\right)^{-2}$	B1	
	$\left(1 - \frac{3}{2}x\right)^{-2} = 1 + \left(-2\right)\left(-\frac{3}{2}x\right) + \frac{-2 3}{1.2}\left(-\frac{3}{2}x\right)^{2} + \frac{-2 3 4}{1.2.3}\left(-\frac{3}{2}x\right)^{3} + \dots$	M1 A1	
	$=1+3x+\frac{27}{4}x^2+\frac{27}{2}x^3+\dots$		
	$(2-3x)^{-2} = \frac{1}{4} + \frac{3}{4}x + \frac{27}{16}x^2 + \frac{27}{8}x^3 + \dots$	M1 A1	(5)
(b)	$f(x) = (a+bx)\left(\frac{1}{4} + \frac{3}{4}x + \frac{27}{16}x^2 + \frac{27}{8}x^3 + \dots\right)$ Coefficient of x; $\frac{3a}{4} + \frac{b}{4} = 0 \qquad (3a+b=0)$		
	Coefficient of x; $\frac{3a}{4} + \frac{b}{4} = 0 \qquad (3a+b=0)$	M1	
	Coefficient of x^2 ; $\frac{27a}{16} + \frac{3b}{4} = \frac{9}{16}$ $(9a + 4b = 3)$ A1 either correct	M1 A1	
	Leading to $a = -1, b = 3$	M1 A1	(5)
(c)	Coefficient of x^3 is $\frac{27a}{8} + \frac{27b}{16} = \frac{27}{8} \times (-1) + \frac{27}{16} \times 3$	M1 A1ft	
	$=\frac{27}{16}$ cao	A1	(3)
			[13]

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6. The curve C has parametric equations

$$x = \ln t$$
, $y = t^2 - 2$, $t > 0$

Find

(a) an equation of the normal to C at the point where t = 3,

(6)

(b) a cartesian equation of *C*.

(3)

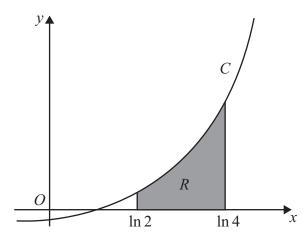


Figure 1

The finite area R, shown in Figure 1, is bounded by C, the x-axis, the line $x = \ln 2$ and the line $x = \ln 4$. The area R is rotated through 360° about the x-axis.

(c) Use calculus to find the exact volume of the solid generated.

(6)

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Question Number	Scheme	Marks
6. (a)	$\frac{\mathrm{d}x}{\mathrm{d}t} = \frac{1}{t}, \frac{\mathrm{d}y}{\mathrm{d}t} = 2t$	
	$\frac{\mathrm{d}y}{\mathrm{d}x} = 2t^2$ Using word 1 at t 2	M1 A1
	Using $mm' = -1$, at $t = 3$ $m' = -\frac{1}{18}$	M1 A1
	$y - 7 = -\frac{1}{18}(x - \ln 3)$	M1 A1 (6)
(b)	$x = \ln t \implies t = e^x$ $y = e^{2x} - 2$	B1 M1 A1 (3)
(c)	$V = \pi \int \left(e^{2x} - 2\right)^2 dx$	M1
	$\int (e^{2x} - 2)^2 dx = \int (e^{4x} - 4e^{2x} + 4) dx$	M1
	$=\frac{e^{4x}}{4} - \frac{4e^{2x}}{2} + 4x$	M1 A1
	$\pi \left[\frac{e^{4x}}{4} - \frac{4e^{2x}}{2} + 4x \right]_{\ln 2}^{\ln 4} = \pi \left[(64 - 32 + 4\ln 4) - (4 - 8 + 4\ln 2) \right]$	M1
	$=\pi\left(36+4\ln2\right)$	A1 (6) [15]
	Alternative to (c) using parameters	
	$V = \pi \int (t^2 - 2)^2 \frac{\mathrm{d}x}{\mathrm{d}t} \mathrm{d}t$	M1
	$\int \left(\left(t^2 - 2 \right)^2 \times \frac{1}{t} \right) dt = \int \left(t^3 - 4t + \frac{4}{t} \right) dt$	M1
	$=\frac{t^4}{4} - 2t^2 + 4\ln t$	M1 A1
	The limits are $t = 2$ and $t = 4$	
	$\pi \left[\frac{t^4}{4} - 2t^2 + 4\ln t \right]_2^4 = \pi \left[\left(64 - 32 + 4\ln 4 \right) - \left(4 - 8 + 4\ln 2 \right) \right]$	M1
	$=\pi(36+4\ln 2)$	A1 (6)

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7.

$$I = \int_{2}^{5} \frac{1}{4 + \sqrt{(x-1)}} \, \mathrm{d}x$$

(a) Given that $y = \frac{1}{4 + \sqrt{(x-1)}}$, complete the table below with values of y corresponding

to x = 3 and x = 5. Give your values to 4 decimal places.

x	2	3	4	5
y	0.2		0.1745	

(2)

(b) Use the trapezium rule, with all of the values of *y* in the completed table, to obtain an estimate of *I*, giving your answer to 3 decimal places.

(4)

(c) Using the substitution $x = (u-4)^2 + 1$, or otherwise, and integrating, find the exact value of I.

(8)

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Question Number	Scheme		Marks	
7. (a)	$x = 3 \implies y = 0.1847$ $x = 5 \implies y = 0.1667$	awrt awrt or $\frac{1}{6}$	B1 B1	(2)
(b)	$I \approx \frac{1}{2} \Big[0.2 + 0.1667 + 2(0.1847 + 0.1745) \Big]$ ≈ 0.543	0.542 or 0.543	<u>B1</u> M1 A1ft A1	(4)
(c)	$\frac{\mathrm{d}x}{\mathrm{d}u} = 2\left(u - 4\right)$		B1	
	$\int \frac{1}{4+\sqrt{(x-1)}} dx = \int \frac{1}{u} \times 2(u-4) du$		M1	
	$=\int \left(2-\frac{8}{u}\right) du$		A1	
	$= 2u - 8 \ln u$ $x = 2 \implies u = 5, x = 5 \implies u = 6$		M1 A1 B1	
	$[2u - 8\ln u]_5^6 = (12 - 8\ln 6) - (10 - 8\ln 5)$		M1	
	$=2+8\ln\left(\frac{5}{6}\right)$		A1	
			Г	(8) 14]