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**Mathematics C1** 

Past Paper

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6663

Centre No.			Paper Reference			Surname	Initial(s)				
Candidate No.			6	6	6	3	/	0	1	Signature	

Paper Reference(s)

6663/01

# **Edexcel GCE**

# **Core Mathematics C1 Advanced Subsidiary**



Exam	Examiner's use only						
Team L	eader's u	ise only					

Question

Leave

Wednesday 10 January 2007 – Afternoon Time: 1 hour 30 minutes

Materials required for examination

Mathematical Formulae (Green)

Items included with question papers

Nil

Calculators may NOT be used in this examination.

1	
2	
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### **Instructions to Candidates**

In the boxes above, write your centre number, candidate number, your surname, initial(s) and signature.

Check that you have the correct question paper.

You must write your answer for each question in the space following the question.

### **Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 10 questions in this question paper. The total mark for this question paper is 75.

There are 20 pages in this question paper. Any blank pages are indicated.

### **Advice to Candidates**

You must ensure that your answers to parts of questions are clearly labelled.

You must show sufficient working to make your methods clear to the Examiner. Answers without working may gain no credit.

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Total



W850/R6663/57570 3/3/3/3/3/38,600

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1. Given that

$$y = 4x^3 - 1 + 2x^{\frac{1}{2}}, \quad x > 0,$$

find  $\frac{\mathrm{d}y}{\mathrm{d}x}$ .

**(4)** 

Q1

(Total 4 marks)

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## **Mathematics C1** edexcel

Past Paper (Mark Scheme)

### January 2007 6663 Core Mathematics C1 Mark Scheme

Question number	Scheme	Marks	
1.	$4x^3 \rightarrow kx^2$ or $2x^{\frac{1}{2}} \rightarrow kx^{-\frac{1}{2}}$ (k a non-zero constant) $12x^2, +x^{-\frac{1}{2}}$ , $(-1 \rightarrow 0)$	M1	
	$12x^2, +x^{-\frac{1}{2}}$ $(-1 \to 0)$	A1, A1, B1	(4) <b>4</b>
	Accept equivalent alternatives to $x^{-\frac{1}{2}}$ , e.g. $\frac{1}{x^{\frac{1}{2}}}$ , $\frac{1}{\sqrt{x}}$ , $x^{-0.5}$ .		
	M1: $4x^3$ 'differentiated' to give $kx^2$ , or		
	$2x^{\frac{1}{2}}$ 'differentiated' to give $kx^{-\frac{1}{2}}$ (but not for just $-1 \to 0$ ).		
	1 <sup>st</sup> A1: $12x^2$ (Do not allow just $3\times 4x^2$ )		
	$2^{\text{nd}}$ A1: $x^{-\frac{1}{2}}$ or equivalent. (Do not allow just $\frac{1}{2} \times 2x^{-\frac{1}{2}}$ , but allow $1x^{-\frac{1}{2}}$ or $\frac{2}{2}x^{-\frac{1}{2}}$ ).		
	B1: $-1$ differentiated to give zero (or 'disappearing'). Can be given provided that at least one of the other terms has been changed. Adding an extra term, e.g. $+ C$ , is B0.		

**C**1

Winter 2007	www.mystudybro.com	Mathematics C1
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(a) Express $\sqrt{108}$ in the form $a\sqrt{3}$ , where $a$ is an integer.	(1)
(b) Express $(2 - \sqrt{3})^2$ in the form $b + c\sqrt{3}$ , where b and c are integers to be found	d. <b>(3)</b>

**Mathematics C1** 

Past Paper (Mark Scheme)

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Question number	Scheme	Mar	Marks		
2.	(a) $6\sqrt{3}$	B1	(1)		
	(b) Expanding $(2 - \sqrt{3})^2$ to get 3 or 4 separate terms	M1			
	7, $-4\sqrt{3}$ $(b=7, c=-4)$	A1, A1	(3)		
			4		
	(a) $\pm 6\sqrt{3}$ also scores B1.				
	(b) M1: The 3 or 4 terms may be wrong.				
	$1^{st}$ A1 for 7, $2^{nd}$ A1 for $-4\sqrt{3}$ .				
	Correct answer $7 - 4\sqrt{3}$ with no working scores all 3 marks.				
	$7 + 4\sqrt{3}$ with or without working scores M1 A1 A0.				
	Other wrong answers with no working score no marks.				

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**3.** Given that

$$f(x) = \frac{1}{x}, \quad x \neq 0,$$

(a) sketch the graph of y = f(x) + 3 and state the equations of the asymptotes.

**(4)** 

(b) Find the coordinates of the point where y = f(x) + 3 crosses a coordinate axis.

**(2)** 

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Past Paper (Mark Scheme)

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Question number	Scheme	Marks	
3.	(a) Shape of $f(x)$	B1	
	Moved up ↑	M1 B1	
	Asymptotes: $y = 3$ $x = 0 \text{ (Allow "y-axis")}$	В1	(4)
	$(y \neq 3 \text{ is B0}, x \neq 0 \text{ is B0}).$	Б1	(+)
	(b) $\frac{1}{x} + 3 = 0$ No variations accepted.	M1	
	$x = -\frac{1}{3}$ (or $-0.33$ ) Decimal answer requires at least 2 d.p.	A1	(2)
	J		6
	asymptotes (see below), but otherwise this mark is awarded generously. The curve may, e.g., bend away from the asymptote a little at the end. Sufficient curve must be seen to suggest the asymptotic behaviour, both horizontal and vertical.  M1: Evidence of an upward translation parallel to the <i>y</i> -axis. The shape of the graph can be wrong, but the complete graph (both branches if they have 2 branches) must be translated upwards. This mark can be awarded generously by implication where the graph drawn is an upward translation of another standard curve (but not a straight line).  The B marks for asymptote equations are independent of the graph. Ignore extra asymptote equations, if seen.		
	(b) Correct answer with no working scores both marks.  The answer may be seen on the sketch in part (a).  Ignore any attempts to find an intersection with the <i>y</i> -axis.		
	e.g.  (a) This scores B0 ( <u>clear</u> overlap with horiz. asymp.)  M1 (Upward translation bod that both branches have been translated).		
	B0 M1  B0 M1  No marks unless the original curve is seen, to show upward translation.		

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y=x-2	
y = x - 2, $y^2 + x^2 = 10$ .	
$y^2 + x^2 = 10.$	
	(7)

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Question number		Sche	me		Mark	S
4.	$(x-2)^2 = x^2 - 4x + 4$	or	$(y+2)^2 = y^2 + 4y + 4$	M: 3 or 4 terms	M1	
	$(x-2)^{2} + x^{2} = 10$ $2x^{2} - 4x - 6 = 0$	or	$y^2 + (y+2)^2 = 10$	M: Substitute	M1	
	$2x^2 - 4x - 6 = 0$	or	$2y^2 + 4y - 6 = 0$	Correct 3 terms	A1	
	$(x-3)(x+1) = 0,  x = \dots$	or	(y+3)(y-1) = 0, $y =appear as (2x-6)(x+1) or 6$		M1	
	x = 3 $x = -1$	or	y = -3  y = 1		A1	
	y = 1 $y = -3$ (Allow equivalent fractions s		x = -1 $x = 3: x = \frac{6}{2} for x = 3).$		M1 A1	7
	1 <sup>st</sup> M: 'Squaring a bracket', or $y^2$ term.	needs 3	or 4 terms, one of which mu	ast be an $x^2$		
	2 <sup>nd</sup> M: Substituting to get an equation in one variable (awarded generously).					
	1 <sup>st</sup> A: Accept equivalent form	ns, e.g.	$2x^2 - 4x = 6.$			
	3 <sup>rd</sup> M: Attempting to solve a	3-term	quadratic, to get 2 solutions			
	$4^{th}$ M: Attempting at least one y value (or x value).					
	If y solutions are given as x possible to score M1 M1A1		or vice-versa, penalise at the	e end, so that it is		

"Non-algebraic" solutions:

No working, and only one correct solution pair found (e.g. x = 3, y = 1):

Strict "pairing of values" at the end is <u>not</u> required.

M0 M0 A0 M0 A0 M1 A0

No working, and both correct solution pairs found, but not demonstrated:

M0 M0 A0 M1 A1 M1 A1

Both correct solution pairs found, and demonstrated, perhaps in a table of values:

Full marks

Squaring individual terms: e.g.

$y^2 = x^2 + 4$		M0	
$x^2 + 4 + x^2 = 10$		M1 A0	(Eqn. in one variable)
$x = \sqrt{3}$		M0 A0	(Not solving 3-term quad.)
$y^2 = x^2 + 4 = 7$	$y = \sqrt{7}$	M1 A0	(Attempting one y value)

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5. The equation $2x^2 - 3x - (k+1) = 0$ , where k is a constant, has no real roots.	
Find the set of possible values of $k$ .	(4)
/m . 1	4 marks)

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$b^2 - 4ac$ , perhaps implicit (e.g. in quadratic formula)	М1	
	M1	
$-4 \times 2 \times -(k+1) < 0$ $(9 + 8(k+1) < 0)$	A1	
8k < -17 (Manipulate to get $pk < q$ , or $pk > q$ , or $pk = q$ )	M1	
$k < -\frac{17}{8}$ (Or equiv: $k < -2\frac{1}{8}$ or $k < -2.125$ )	A1cso	(4)
		4
Must be considering the given quadratic equation.		
Condone sign or bracketing mistakes in manipulation.  Not dependent on 1 <sup>st</sup> M, but should not be given for irrelevant work.  M0 M1 could be scored:		
ere there are x terms in the discriminant expression, but then division by $x^2$		
	Could also be, for example, comparing or equating $b^2$ and $4ac$ . Must be considering the given quadratic equation. There must not be $x$ terms in the expression, but there must be a $k$ term. Correct expression (need not be simplified) and correct inequality sign. Allow also $-3^2 - 4 \times 2 \times -(k+1) < 0$ .  Condone sign or bracketing mistakes in manipulation. Not dependent on $1^{st}$ M, but should not be given for irrelevant work.	Could also be, for example, comparing or equating $b^2$ and $4ac$ . Must be considering the given quadratic equation. There must not be $x$ terms in the expression, but there must be a $x$ term. Correct expression (need not be simplified) and correct inequality sign. Allow also $-3^2 - 4 \times 2 \times -(k+1) < 0$ .  Condone sign or bracketing mistakes in manipulation.  Not dependent on $1^{st}$ M, but should not be given for irrelevant work. M0 M1 could be scored: e.g. where $b^2 + 4ac$ is used instead of $b^2 - 4ac$ .  Leases: There there are $x$ terms in the discriminant expression, but then division by $x^2$ is an inequality/equation in $x$ . (This could score M0 A0 M1 A1).  of $\le$ instead of $<$ loses one A mark only, at first occurrence, so an arwise correct solution leading to $x$ scores M1 A0 M1 A1.

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6	6	6	3

Leave blank (a) Show that  $(4+3\sqrt{x})^2$  can be written as  $16+k\sqrt{x}+9x$ , where k is a constant to be found. **(2)** (b) Find  $\int (4+3\sqrt{x})^2 dx$ . **(3) Q6** (Total 5 marks)

### **Mathematics C1**

Past Paper (Mark Scheme)

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Question number	Scheme	Marks	
6.	(a) $(4+3\sqrt{x})(4+3\sqrt{x})$ seen, or a numerical value of $k$ seen, $(k \neq 0)$ . (The $k$ value need not be explicitly stated see below).	M1	
	$16 + 24\sqrt{x} + 9x$ , or $k = 24$	A1cso	(2)
	(b) $16 \rightarrow cx$ or $kx^{\frac{1}{2}} \rightarrow cx^{\frac{3}{2}}$ or $9x \rightarrow cx^2$	M1	
	$\int (16 + 24\sqrt{x} + 9x) dx = 16x + \frac{9x^2}{2} + C, + 16x^{3/2}$	A1, A1ft	(3)
			5
	(a) e.g. $(4+3\sqrt{x})(4+3\sqrt{x})$ alone scores M1 A0, (but <u>not</u> $(4+3\sqrt{x})^2$ alone). e.g $16+12\sqrt{x}+9x$ scores M1 A0.		
	$k = 24$ or $16 + 24\sqrt{x} + 9x$ , with no further evidence, scores full marks M1 A1.		
	Correct solution only (cso): any wrong working seen loses the A mark.		
	(b) A1: $16x + \frac{9x^2}{2} + C$ . Allow 4.5 or $4\frac{1}{2}$ as equivalent to $\frac{9}{2}$ .		
	A1ft: $\frac{2k}{3}x^{\frac{3}{2}}$ (candidate's value of k, or general k).		
	For this final mark, allow for example $\frac{48}{3}$ as equivalent to 16, but do		
	not allow unsimplified "double fractions" such as $\frac{24}{3/2}$ , and do		
	<u>not</u> allow unsimplified "products" such as $\frac{2}{3} \times 24$ .		
	A single term is required, e.g. $8x^{\frac{3}{2}} + 8x^{\frac{3}{2}}$ is not enough.		
	An otherwise correct solution with, say, $C$ missing, followed by an incorrect solution including $+ C$ can be awarded full marks (isw, but allowing the $C$ to appear at any stage).		

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The curve C has equation y = f(x),  $x \ne 0$ , and the point P(2, 1) lies on C. Given that

$$f'(x) = 3x^2 - 6 - \frac{8}{x^2} ,$$

(a) find f(x).

**(5)** 

(b) Find an equation for the tangent to C at the point P, giving your answer in the form y = mx + c, where m and c are integers.

**(4)** 

Past Paper (Mark Scheme)

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Question number	Scheme	Marks	
7.	(a) $3x^2 \to cx^3$ or $-6 \to cx$ or $-8x^{-2} \to cx^{-1}$	M1	
	$f(x) = \frac{3x^3}{3} - 6x - \frac{8x^{-1}}{-1} \qquad (+C) \qquad \left(x^3 - 6x + \frac{8}{x}\right)$	A1 A1	
	Substitute $x = 2$ and $y = 1$ into a 'changed function' to form an equation in $C$ .	M1	
	1 = 8 - 12 + 4 + C $C = 1$	A1cso	(5)
	(b) $3 \times 2^2 - 6 - \frac{8}{2^2}$	M1	
	= 4	A1	
	Eqn. of tangent: $y-1=4(x-2)$	M1	
	y = 4x - 7 (Must be in this form)	A1	(4)
			9
	(a) First 2 A marks: + <i>C</i> is not required, and coefficients need <u>not</u> be simplified, but powers must be simplified.  All 3 terms correct: A1 A1 Two terms correct: A1 A0 Only one term correct: A0 A0 Allow the M1 A1 for finding <i>C</i> to be scored either in part (a) or in part (b).  (b) 1 <sup>st</sup> M: Substituting <i>x</i> = 2 into 3 <i>x</i> <sup>2</sup> - 6 - $\frac{8}{x^2}$ (must be this function).  2 <sup>nd</sup> M: Awarded generously for attempting the equation of a straight line through (2, 1) or (1, 2) with any value of <i>m</i> , however found.  2 <sup>nd</sup> M: Alternative is to use (2, 1) or (1, 2) in $y = mx + c$ to <u>find a value</u> for <i>c</i> .  If calculation for the gradient value is seen in part (a), it must be <u>used</u> in part (b) to score the first M1 A1 in (b).  Using (1, 2) instead of (2, 1): Loses the 2 <sup>nd</sup> method mark in (a).  Gains the 2 <sup>nd</sup> method mark in (b).		

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- The curve *C* has equation  $y = 4x + 3x^{\frac{3}{2}} 2x^2$ , x > 0.
  - (a) Find an expression for  $\frac{dy}{dx}$ .

**(3)** 

(b) Show that the point P(4, 8) lies on C.

**(1)** 

(c) Show that an equation of the normal to C at the point P is

$$3y = x + 20$$
.

**(4)** 

The normal to C at P cuts the x-axis at the point Q.

(d) Find the length PQ, giving your answer in a simplified surd form.

**(3)** 

Past Paper (Mark Scheme)

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Question number	Scheme	Marks	
8.	(a) $4x \to k$ or $3x^{\frac{3}{2}} \to kx^{\frac{1}{2}}$ or $-2x^2 \to kx$	M1	
	$\frac{dy}{dx} = 4 + \frac{9}{2}x^{1/2} - 4x$	A1 A1	(3)
	(b) For $x = 4$ , $y = (4 \times 4) + (3 \times 4\sqrt{4}) - (2 \times 16) = 16 + 24 - 32 = 8$ (*)	B1	(1)
	(c) $\frac{dy}{dx} = 4 + 9 - 16 = -3$ M: Evaluate their $\frac{dy}{dx}$ at $x = 4$	M1	
	Gradient of normal = $\frac{1}{3}$	A1ft	
	Equation of normal: $y - 8 = \frac{1}{3}(x - 4)$ , $3y = x + 20$ (*)	M1, A1	(4)
	(d) $y = 0$ : $x = (-20)$ and use $(x_2 - x_1)^2 + (y_2 - y_1)^2$	M1	
	$PQ = \sqrt{24^2 + 8^2}$ or $PQ^2 = 24^2 + 8^2$ Follow through from $(k, 0)$	A1ft	
	May also be scored with $(-24)^2$ and $(-8)^2$ .		
	$=8\sqrt{10}$	A1	(3)
			11
	(a) For the 2 A marks coefficients need <u>not</u> be simplified, but powers must be simplified. For example, $\frac{3}{2} \times 3x^{\frac{1}{2}}$ is acceptable.		
	All 3 terms correct: A1 A1		
	Two terms correct: A1 A0		
	Only one term correct: A0 A0		
	(b) There must be some evidence of the "24" value.		
	(c) In this part, beware 'working backwards' from the given answer.		
	A1ft: Follow through is just from the candidate's <u>value</u> of $\frac{dy}{dx}$ .		
	$2^{\text{nd}}$ M: Is not given if an $m$ value appears "from nowhere". $2^{\text{nd}}$ M: Must be an attempt at a <u>normal</u> equation, not a tangent.		
	$2^{\text{nd}}$ M: Alternative is to use (4, 8) in $y = mx + c$ to <u>find a value</u> for c.		
	(d) M: Using the normal equation to attempt coordinates of $Q$ , (even if using		
	$x = 0$ instead of $y = 0$ ), and using Pythagoras to attempt $PQ$ or $PQ^2$ . Follow through from $(k, 0)$ , but not from $(0, k)$		
	A common wrong answer is to use $x = 0$ to give $\frac{20}{3}$ . This scores M1 A0 A0.		
	For final answer, accept other simplifications of $\sqrt{640}$ , e.g. $2\sqrt{160}$ or $4\sqrt{40}$ .		

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	ome sticks that are all of the same length. She arranges them in squares and has following 3 rows of patterns:
Row 1	
Row 2	
Row 3	
	es that 4 sticks are required to make the single square in the first row, 7 sticks to quares in the second row and in the third row she needs 10 sticks to make 3
	an expression, in terms of $n$ , for the number of sticks required to make a similar gement of $n$ squares in the $n$ th row.  (3)
	inues to make squares following the same pattern. She makes 4 squares in the nd so on until she has completed 10 rows.
(b) Find	the total number of sticks Ann uses in making these 10 rows.  (3)
	ed with 1750 sticks. Given that Ann continues the pattern to complete $k$ rows not have sufficient sticks to complete the $(k+1)$ th row,
(c) show	that $k$ satisfies $(3k-100)(k+35) < 0$ . (4)
(d) Find	the value of $k$ . (2)

Past Paper (Mark Scheme)

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Question number	Scheme	Marks	
9.	(a) Recognising arithmetic series with first term 4 and common difference 3. (If not scored here, this mark may be given if seen elsewhere in the solution). $a + (n-1)d = 4 + 3(n-1)$ (= $3n + 1$ )	B1 M1 A1	(3)
	(b) $S_n = \frac{n}{2} \{ 2a + (n-1)d \} = \frac{10}{2} \{ 8 + (10-1) \times 3 \}, = 175,$	M1 A1, A1	(3)
	(c) $S_k < 1750$ : $\frac{k}{2} \{8 + 3(k - 1)\} < 1750$ or $S_{k+1} > 1750$ : $\frac{k+1}{2} \{8 + 3k\} > 1750$	-M1	
	$3k^2 + 5k - 3500 < 0$ (or $3k^2 + 11k - 3492 > 0$ ) (Allow equivalent 3-term versions such as $3k^2 + 5k = 3500$ ).	-M1 A1	
	(3k-100)(k+35) < 0 Requires use of correct inequality throughout.(*)	A1cso	(4)
	(d) $\frac{100}{3}$ or equiv. seen $\left(\text{or } \frac{97}{3}\right)$ , $k = 33$ (and no other values)	M1, A1	(2) 12
	<ul> <li>(a) B1: Usually identified by a = 4 and d = 3. M1: Attempted use of term formula for arithmetic series, or answer in the form (3n + constant), where the constant is a non-zero value Answer for (a) does not require simplification, and a correct answer without working scores all 3 marks.</li> <li>(b) M1: Use of correct sum formula with n = 9, 10 or 11. A1: Correct, perhaps unsimplified, numerical version. A1: 175 Alternative: (Listing and summing terms). M1: Summing 9, 10 or 11 terms. (At least 1<sup>st</sup>, 2<sup>nd</sup> and last terms must be seen). A1: Correct terms (perhaps implied by last term 31). A1: 175 Alternative: (Listing all sums) M1: Listing 9, 10 or 11 sums. (At least 4, 7,, "last"). A1: Correct sums, correct finishing value 175. A1: 175 Alternative: (Using last term).</li> <li>M1: Using S<sub>n</sub> = n/2 (a + l) with T<sub>9</sub>, T<sub>10</sub> or T<sub>11</sub> as the last term.</li> </ul>		
	A1: Correct numerical version $\frac{10}{2}(4+31)$ . A1: 175 Correct answer with <u>no</u> working scores 1 mark: 1,0,0.		
	<ul> <li>(c) For the first 3 marks, allow any inequality sign, or equals.  1<sup>st</sup> M: Use of correct sum formula to form inequality or equation in k, with the 1750.  2<sup>nd</sup> M: (Dependent on 1<sup>st</sup> M). Form 3-term quadratic in k.  1<sup>st</sup> A: Correct 3 terms.  Allow credit for part (c) if valid work is seen in part (d).</li> <li>(d) Allow both marks for k = 33 seen without working.  Working for part (d) must be seen in part (d), not part (c).</li> </ul>		

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10. (a) On the same axes sketch the graphs of the curves with equations

(i) 
$$y = x^2(x-2)$$
,

**(3)** 

(ii) 
$$y = x(6-x)$$
,

**(3)** 

and indicate on your sketches the coordinates of all the points where the curves cross the *x*-axis.

(b) Use algebra to find the coordinates of the points where the graphs intersect.

**(7)** 

Past Paper (Mark Scheme)

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Question number	Scheme		Marks
10.	(a) (i) Shape or or	B1	
	Max. at (0, 0).	B1	
	(2, 0), (or 2 shown on <i>x</i> -axis).	B1	(3)
	(ii) Shape	-B1	
	(It need not go below x-axis)		
	Through origin.	-B1	
	(6, 0), (or 6 shown on $x$ -axis).	B1	(3)
	(b) $x^2(x-2) = x(6-x)$	-M1	
	Expand to form 3-term cubic (or 3-term quadratic if divided by $x$ ), with all terms on one side. The "= 0" may be implied.	−M1	
	x(x-3)(x+2) = 0 $x =$ Factor $x$ (or divide by $x$ ), and solve quadratic.	-M1	
	x = 3 and $x = -2$	A1	
	x = -2: $y = -16$ Attempt y value for a non-zero x value by	M1	
	substituting back into $x^2(x-2)$ or $x(6-x)$ .	A 1	
	x = 3: $y = 9$ Both y values are needed for A1. $(-2, -16)$ and $(3, 9)$	A1	
	(0, 0) This can just be written down. Ignore any 'method' shown.		
	(But must be seen in part (b)).	B1	(7) <b>13</b>
	(a) (i) For the third 'shape' shown above, where a section of the graph coincides with the <i>x</i> -axis, the B1 for (2, 0) can still be awarded if the 2 is shown on the <i>x</i> -axis.		
	For the final B1 in (i), and similarly for (6, 0) in (ii): There must be a sketch.  If, for example (2, 0) is written <u>separately</u> from the sketch, the sketch must not clearly contradict this.  If (0, 2) instead of (2, 0) is shown <u>on the sketch</u> , allow the mark.  Ignore extra intersections with the <i>x</i> -axis.		
	(ii) 2 <sup>nd</sup> B is dependent on 1 <sup>st</sup> B.		
	Separate sketches can score all marks.		
	(b) Note the dependence of the first three M marks.  A common wrong solution is (-2, 0), (3, 0), (0, 0), which scores M0 A0 B1		
	as the last 3 marks.  A solution using <u>no</u> algebra (e.g. trial and error), can score up to 3 marks:  M0 M0 M0 A0 M1 A1 B1. (The final A1 requires both y values).  Also, if the cubic is found but not solved algebraically, up to 5 marks:  M1 M1 M0 A0 M1 A1 B1. (The final A1 requires both y values).		