





Question Number	Scheme		Marks
1	$\frac{7+\sqrt{5}}{\sqrt{5}-1} \times \frac{(\sqrt{5}+1)}{(\sqrt{5}+1)}$	Multiplies top and bottom by a correct expression. This statement is sufficient.	M1
	(Allow to multiply top and bottom by $k(\sqrt{5}+1)$ )		
	$= \frac{\dots}{4}$	Obtains a denominator of 4 or sight of $(\sqrt{5}-1)(\sqrt{5}+1) = 4$	A1cso
<b>Note that M0A1 is not possible. The 4 must come from a correct method.</b>			
	$(7+\sqrt{5})(\sqrt{5}+1) = 7\sqrt{5} + 5 + 7 + \sqrt{5}$	An attempt to multiply the numerator by $(\pm\sqrt{5} \pm 1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5} \pm 1)$ . (May be implied)	M1
	$3 + 2\sqrt{5}$	Answer as written or $a = 3$ and $b = 2$ . (Allow $2\sqrt{5} + 3$ )	A1cso
<b>Correct answer with no working scores full marks</b>			
			<b>[4]</b>
Way 2	$\frac{7+\sqrt{5}}{\sqrt{5}-1} \times \frac{(-\sqrt{5}-1)}{(-\sqrt{5}-1)}$	Multiplies top and bottom by a correct expression. This statement is sufficient.	M1
	(Allow to multiply top and bottom by $k(-\sqrt{5}-1)$ )		
	$= \frac{\dots}{-4}$	Obtains a denominator of -4	A1cso
	$(7+\sqrt{5})(-\sqrt{5}-1) = -7\sqrt{5} - 5 - 7 - \sqrt{5}$	An attempt to multiply the numerator by $(\pm\sqrt{5} \pm 1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5} \pm 1)$ . (May be implied)	M1
	$3 + 2\sqrt{5}$	Answer as written or $a = 3$ and $b = 2$	A1cso
<b>Correct answer with no working scores full marks</b>			
			<b>[4]</b>
<b>Alternative using Simultaneous Equations:</b>			
$\frac{7+\sqrt{5}}{\sqrt{5}-1} = a + b\sqrt{5} \Rightarrow 7 + \sqrt{5} = (a-b)\sqrt{5} + 5b - a$ M1			
Multiplies and collects rational and irrational parts			
$a - b = 1, 5b - a = 7$ A1			
Correct equations			
$a = 3, b = 2$			
M1 for attempt to solve simultaneous equations A1 both answers correct			



Question Number	Scheme		Marks
2	$\left(\int\right) \frac{10x^5}{5} - \frac{4x^2}{2}, -\frac{3x^{\frac{1}{2}}}{\frac{1}{2}}$	M1: Some attempt to integrate: $x^n \rightarrow x^{n+1}$ on at least one term. (not for + c)  (If they think $\frac{3}{\sqrt{x}}$ is $3x^{\frac{1}{2}}$ you can still award the method mark for $\frac{1}{x^2} \rightarrow x^{\frac{3}{2}}$ )	M1A1, A1
A1: $\frac{10x^5}{5}$ <b>and</b> $\frac{-4x^2}{2}$ or better			
A1: $-\frac{3x^{\frac{1}{2}}}{\frac{1}{2}}$ or better			
	$= \underline{2x^5 - 2x^2 - 6x^{\frac{1}{2}} + c}$	Each term correct and simplified and the + c all appearing together on the same line. Allow $\sqrt{x}$ for $x^{\frac{1}{2}}$ . Ignore any spurious integral or signs and/or dy/dx's.	A1
	Do <b>not</b> apply isw. If they obtain the correct answer and then e.g. divide by 2 they lose the last mark.		
			<b>[4]</b>



Question Number	Scheme		Marks
3(a)	$8^{\frac{1}{3}} = 2$ or $8^5 = 32768$	A correct attempt to deal with the $\frac{1}{3}$ or the 5. $8^{\frac{1}{3}} = \sqrt[3]{8}$ or $8^5 = 8 \times 8 \times 8 \times 8 \times 8$	M1
	$\left(8^{\frac{5}{3}} = \right) 32$	Cao	A1
A correct answer with no working scores full marks			
Alternative			
$8^{\frac{5}{3}} = 8 \times 8^{\frac{2}{3}} = 8 \times 2^2 =$ M1 (Deals with the 1/3) $= 32$ A1			
			<b>(2)</b>
(b)	$\left(2x^{\frac{1}{2}}\right)^3 = 2^3 x^{\frac{3}{2}}$	One correct power either $2^3$ or $x^{\frac{3}{2}}$ . $\left(2x^{\frac{1}{2}}\right) \times \left(2x^{\frac{1}{2}}\right) \times \left(2x^{\frac{1}{2}}\right)$ on its own is not sufficient for this mark.	M1
$\frac{8x^{\frac{3}{2}}}{4x^2} = 2x^{-\frac{1}{2}}$ or $\frac{2}{\sqrt{x}}$		M1: Divides coefficients of $x$ and subtracts their powers of $x$ . <b>Dependent on the previous M1</b>	dM1A1
		A1: Correct answer	
Note that unless the power of $x$ implies that they have subtracted their powers you would need to see evidence of subtraction. E.g. $\frac{8x^{\frac{3}{2}}}{4x^2} = 2x^{\frac{1}{2}}$ would score dM0 unless you see some evidence that $3/2 - 2$ was intended for the power of $x$ .			
Note that there is a misconception that $\frac{\left(2x^{\frac{1}{2}}\right)^3}{4x^2} = \left(\frac{2x^{\frac{1}{2}}}{4x^2}\right)^3$ - this scores 0/3			
			<b>(3)</b>
			<b>[5]</b>





Question Number	Scheme		Marks
	<b>For this question, mark (a) and (b) together and ignore labelling.</b>		
<b>4(a)</b>	$(a_2 =) k(4+2) (= 6k)$	Any correct (possibly un-simplified) expression	B1
			<b>(1)</b>
<b>(b)</b>	$a_3 = k(\text{their } a_2 + 2) (= 6k^2 + 2k)$	An attempt at $a_3$ . Can follow through their answer to (a) but $a_2$ must be an expression in $k$ .	M1
	$a_1 + a_2 + a_3 = 4 + (6k) + (6k^2 + 2k)$	An attempt to find their $a_1 + a_2 + a_3$	M1
	$4 + (6k) + (6k^2 + 2k) = 2$	A <b>correct</b> equation in any form.	A1
	Solves $6k^2 + 8k + 2 = 0$ to obtain $k = (6k^2 + 8k + 2 = 2(3k + 1)(k + 1))$	Solves their 3TQ as far as $k = \dots$ according to the general principles. (An independent mark for solving their three term quadratic)	M1
	$k = -1/3$	Any equivalent fraction	A1
	$k = -1$	Must be from a correct equation. (Do not accept un-simplified)	B1
	Note that it is quite common to think the sequence is an AP. Unless they find $a_3$ , this is likely only to score the M1 for solving their quadratic.		
			<b>(6)</b>
			<b>[7]</b>



Question Number	Scheme		Marks
5 (a)	$6x + x > 1 - 8$	Attempts to expand the bracket and collect $x$ terms on one side and constant terms on the other. Condone sign errors and allow one error in expanding the bracket. Allow $<, \leq, \geq, =$ instead of $>$ .	M1
	$x > -1$	Cao	A1
Do not isw here, mark their final answer.			
			<b>(2)</b>
(b)	$(x + 3)(3x - 1) [= 0]$ $\Rightarrow x = -3$ and $\frac{1}{3}$	M1: Attempt to solve the quadratic to obtain two critical values A1: $x = -3$ <b>and</b> $\frac{1}{3}$ (may be implied by their inequality). Allow all equivalent fractions for -3 and 1/3. (Allow 0.333 for 1/3)	M1A1
	$-3 < x < \frac{1}{3}$	M1: Chooses “inside” region (The letter $x$ does not need to be used here) A1ft: Allow $x < \frac{1}{3}$ <b>and</b> $x > -3$ or $\left(-3, \frac{1}{3}\right)$ or $x < \frac{1}{3} \cap x > -3$ . Follow through their critical values. (must be in terms of $x$ here) Allow all equivalent fractions for -3 and 1/3. Both $(x < \frac{1}{3}$ <b>or</b> $x > -3)$ and $(x < \frac{1}{3}, x > -3)$ as a final answer score A0.	M1A1ft
			<b>(4)</b>
			<b>[6]</b>
Note that use of $\leq$ or $\geq$ appearing in an otherwise correct answer in (a) or (b) should only be penalised once, the first time it occurs.			



Question Number	Scheme	Marks
6	$(-1, 3)$ , $(11, 12)$	
(a)	$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{12 - 3}{11 - (-1)} = \frac{3}{4}$	M1: Correct method for the gradient A1: Any correct fraction or decimal
	$y - 3 = \frac{3}{4}(x + 1)$ or $y - 12 = \frac{3}{4}(x - 11)$ or $y = \frac{3}{4}x + c$ with attempt at substitution to find $c$	Correct straight line method using either of the given points and a numerical gradient.
	$4y - 3x - 15 = 0$	Or equivalent with integer coefficients (= 0 is required)
	This A1 should only be awarded in (a)	
		(4)
(a) Way 2	$\frac{y - y_1}{y_2 - y_1} = \frac{x - x_1}{x_2 - x_1} \Rightarrow \frac{y - 3}{12 - 3} = \frac{x + 1}{11 + 1}$	M1: Use of a correct formula for the straight line A1: Correct equation
	$12(y - 3) = 9(x + 1)$	Eliminates fractions
	$4y - 3x - 15 = 0$	Or equivalent with integer coefficients (= 0 is required)
		(4)
(b)	Solves their equation from part (a) and $L_2$ simultaneously to eliminate one variable	Must reach as far as an equation in $x$ only or in $y$ only. (Allow slips in the algebra)
	$x = 3$ or $y = 6$	One of $x = 3$ or $y = 6$
	<b>Both <math>x = 3</math> and <math>y = 6</math></b>	Values can be un-simplified fractions.
	<b>Fully correct answers with no working can score 3/3 in (b)</b>	
		(3)
(b) Way 2	$(-1, 3) \rightarrow -a + 3b + c = 0$ $(11, 12) \rightarrow 11a + 12b + c = 0$	Substitutes the coordinates to obtain two equations
	$\therefore a = -\frac{3}{4}b, b = -\frac{4}{15}c$	Obtains sufficient equations to establish values for $a, b$ and $c$
	e.g. $c = 1 \Rightarrow b = -\frac{4}{15}, a = \frac{3}{15}$	Obtains values for $a, b$ and $c$
	$\frac{3}{15}x - \frac{4}{15}y + 1 = 0 \Rightarrow 4y - 3x - 15 = 0$	Correct equation
		(4)
		[7]



Question Number	Scheme		Marks
7(a)	$600 = 200 + (N - 1)20 \Rightarrow N = \dots$	Use of 600 with a <b>correct</b> formula in an attempt to find $N$ . A correct formula could be implied by a correct answer.	M1
	$N = 21$	cso	A1
	Accept correct answer only.		
	$600 = 200 + 20N \Rightarrow N = 20$ is M0A0 (wrong formula) $\frac{600 - 200}{20} = 20 \therefore N = 21$ is M1A1 (correct formula implied)		
	<b>Listing:</b> All terms must be listed up to 600 and 21 correctly identified. A solution that scores 2 if fully correct and 0 otherwise.		
			(2)
(b)	<b>Look for an AP first:</b>		
	$S = \frac{21}{2}(2 \times 200 + 20 \times 20)$ or $\frac{21}{2}(200 + 600)$ or $S = \frac{20}{2}(2 \times 200 + 19 \times 20)$ or $\frac{20}{2}(200 + 580)$  (= 8400 or 7800)	M1: Use of correct sum formula with their <b>integer</b> $n = N$ or $N - 1$ from part (a) where $3 < N < 52$ and $a = 200$ and $d = 20$ . A1: Any correct un-simplified numerical expression with $n = 20$ or $n = 21$ (No follow through here)	M1A1
	<b>Then for the constant terms:</b>		
	$600 \times (52 - "N") (= 18600)$	M1: $600 \times k$ where $k$ is an integer and $3 < k < 52$ A1: A correct un-simplified follow through expression with their $k$ consistent with $n$ so that $n + k = 52$	M1A1ft
	So total is 27000	Cao	A1
	Note that for the constant terms, they may correctly use an AP sum with $d = 0$ .		
	<b>There are no marks in (b) for just finding <math>S_{52}</math></b>		
			(5)
			[7]
	If they obtain $N = 20$ in (a) (0/2) and then in (b) proceed with, $S = \frac{20}{2}(2 \times 200 + 19 \times 20) + 32 \times 600 = 7800 + 19\ 200 = 27\ 000$ allow them to 'recover' and score full marks in (b) Similarly If they obtain $N = 22$ in (a) (0/2) and then in (b) proceed with, $S = \frac{21}{2}(2 \times 200 + 20 \times 20) + 31 \times 600 = 8400 + 18\ 600 = 27\ 000$ allow them to 'recover' and score full marks in (b)		

8.

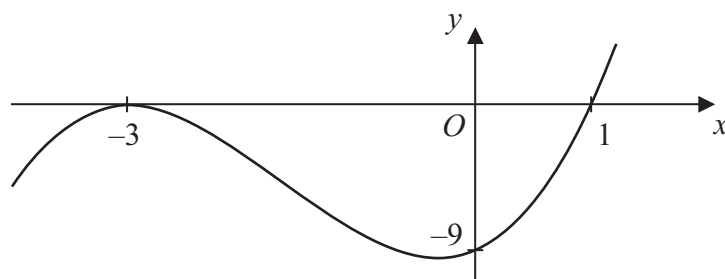


Figure 1

Figure 1 shows a sketch of the curve with equation  $y = f(x)$  where

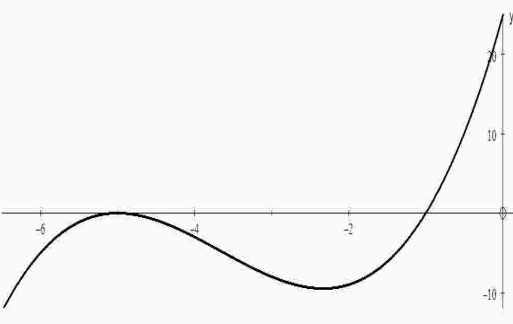
$$f(x) = (x + 3)^2 (x - 1), \quad x \in \mathbb{R}.$$

The curve crosses the  $x$ -axis at  $(1, 0)$ , touches it at  $(-3, 0)$  and crosses the  $y$ -axis at  $(0, -9)$

- (a) In the space below, sketch the curve  $C$  with equation  $y = f(x + 2)$  and state the coordinates of the points where the curve  $C$  meets the  $x$ -axis. (3)
- (b) Write down an equation of the curve  $C$ . (1)
- (c) Use your answer to part (b) to find the coordinates of the point where the curve  $C$  meets the  $y$ -axis. (2)





Question Number	Scheme		Marks
<p><b>8</b></p> <p><b>(a)</b></p>		<p>Horizontal translation – does <b>not</b> have to cross the <math>y</math>-axis on the right but must at least reach the <math>x</math>-axis.</p>	B1
		<p>Touching at <math>(-5, 0)</math>. This could be stated anywhere or <math>-5</math> could be marked on the <math>x</math>-axis. Or <math>(0, -5)</math> <b>marked in the correct place</b>. Be fairly generous with ‘touching’ if the intention is clear.</p>	B1
		<p>The right hand tail of their cubic shape crossing at <math>(-1, 0)</math>. This could be stated anywhere or <math>-1</math> could be marked on the <math>x</math>-axis. Or <math>(0, -1)</math> <b>marked in the correct place</b>. The curve must <b>cross</b> the <math>x</math>-axis and not stop at <math>-1</math>.</p>	B1
			<b>(3)</b>
<p><b>(b)</b></p>	<p><math>(x + 5)^2(x + 1)</math></p>	<p>Allow <math>(x + 3 + 2)^2(x - 1 + 2)</math></p>	B1
			<b>(1)</b>
<p><b>(c)</b></p>	<p>When <math>x = 0, y = 25</math></p>	<p>M1: Substitutes <math>x = 0</math> into their expression in <b>part (b)</b> which is not <math>f(x)</math>. This may be implied by their answer. Note that the question asks them to use part (b) but allow independent methods.</p>	M1 A1
		<p>A1: <math>y = 25</math> (Coordinates not needed)</p>	
<p><b>If they expand <u>incorrectly</u> prior to substituting <math>x = 0</math>, score M1 A0</b> <b>NB <math>f(x + 2) = x^3 + 11x^2 + 35x + 25</math></b></p>			
		<b>(2)</b>	
		<b>[6]</b>	



Question Number	Scheme		Marks
9 (a)	$(3-x^2)^2 = 9 - 6x^2 + x^4$	An attempt to expand the numerator obtaining an expression of the form $9 \pm px^2 \pm qx^4$ , $p, q \neq 0$	M1
	$9x^{-2} + x^2$	Must come from $\frac{9+x^4}{x^2}$	A1
	-6	Must come from $\frac{-6x^2}{x^2}$	A1
	Alternative 1: Writes $\frac{(3-x^2)^2}{x^2}$ as $(3x^{-1} - x)^2$ and attempts to expand = M1 then A1A1 as in the scheme.		
	Alternative 2: Sets $(3-x^2)^2 = 9 + Ax^2 + Bx^4$ , expands $(3-x^2)^2$ and compares coefficients = M1 then A1A1 as in the scheme.		
			(3)
	$(f'(x) = 9x^{-2} - 6 + x^2)$		
(b)	$-18x^{-3} + 2x$	M1: $x^n \rightarrow x^{n-1}$ on separate terms at least once. Do not award for $A \rightarrow 0$ (Integrating is M0) A1ft: $-18x^{-3} + 2$ "B" $x$ with a numerical B and no extra terms. (A may have been incorrect or even zero)	M1 A1ft
			(2)
(c)	$f(x) = -9x^{-1} - 6x + \frac{x^3}{3} (+c)$	M1: $x^n \rightarrow x^{n+1}$ on separate terms at least once. (Differentiating is M0) A1ft: $-9x^{-1} + Ax + \frac{Bx^3}{3} (+c)$ with numerical A and B, $A, B \neq 0$	M1A1ft
	$10 = \frac{-9}{-3} - 6(-3) + \frac{(-3)^3}{3} + c$ so $c = \dots$	Uses $x = -3$ and $y = 10$ in what they think is $f(x)$ (They may have differentiated here) but it must be a changed function i.e. not the original $f'(x)$ , to form a linear equation in $c$ and attempts to find $c$ . No $+c$ gets M0 and A0 unless their method implies that they are correctly finding a constant.	M1
	$c = -2$	cso	A1
	$(f(x) =) -9x^{-1} - 6x + \frac{x^3}{3} +$ their $c$	Follow through their $c$ in an otherwise (possibly un-simplified) <b>correct expression</b> . Allow $-\frac{9}{x}$ for $-9x^{-1}$ or even $\frac{9x^{-1}}{-1}$ .	A1ft
	<b>Note that if they integrate in (b), no marks there but if they then go on to use their integration in (c), the marks for integration are available.</b>		
			(5)
			[10]



Question Number	Scheme	Marks	
10(a)	$x^2 - 4k(1 - 2x) + 5k (= 0)$	Makes $y$ the subject from the first equation and substitutes into the second equation ( $= 0$ not needed here) or eliminates $y$ by a correct method.	M1
	So $x^2 + 8kx + k = 0$ *	Correct completion to printed answer. There must be no incorrect statements.	A1cso
			(2)
(b)	$(8k)^2 - 4k$	M1: Use of $b^2 - 4ac$ (Could be in the quadratic formula or an inequality, $= 0$ not needed yet). There must be some correct substitution but there must be no $x$ 's. No formula quoted followed by e.g. $8k^2 - 4k = 0$ is M0. A1: Correct expression. Do not condone missing brackets unless they are implied by later work but can be implied by $(8k)^2 > 4k$ etc.	M1 A1
	$k = \frac{1}{16}$ (oe)	Cso (Ignore any reference to $k = 0$ ) but there must be no contradictory earlier statements. A fully correct solution with no errors.	A1
			(3)
(b) Way 2 Equal roots	$\Rightarrow x^2 + 8kx + k = (x + \sqrt{k})^2$ $\Rightarrow 8k = 2\sqrt{k}$	M1: Correct strategy for equal roots A1: Correct equation	M1A1
	$k = \frac{1}{16}$ (oe)	Cso (Ignore any reference to $k = 0$ )	A1
(b) Way 3	Completes the Square $x^2 + 8kx + k = (x + 4k)^2 - 16k^2 + k$ $\Rightarrow 16k^2 - k = 0$	M1: $(x \pm 4k)^2 \pm p \pm k, p \neq 0$ A1: Correct equation	M1A1
	$k = \frac{1}{16}$ (oe)	Cso (Ignore any reference to $k = 0$ )	A1
			(3)
(c)	$x^2 + \frac{1}{2}x + \frac{1}{16} = 0$ so $(x + \frac{1}{4})^2 = 0 \Rightarrow x =$	Substitutes their value of $k$ into the given quadratic and attempt to solve their 2 or 3 term quadratic as far as $x =$ (may be implied by substitution into the quadratic formula) or starts again and substitutes their value of $k$ into the second equation and solves simultaneously to obtain a value for $x$ .	M1
	$x = -\frac{1}{4}, y = 1\frac{1}{2}$	First A1 one answer correct, second A1 both answers correct.	A1A1
	Special Case: $x^2 + \frac{1}{2}x + \frac{1}{16} = 0 \Rightarrow x = -\frac{1}{4}, \frac{1}{4} \Rightarrow y = 1\frac{1}{2}, \frac{1}{2}$ allow M1A1A0		
			(3)
			[8]



Question Number	Scheme		Marks
11 (a)	$\left(-\frac{3}{4}, 0\right)$ . Accept $x = -\frac{3}{4}$		B1
			(1)
(b)	$y = 4$	B1: One correct asymptote	B1B1
	$x = 0$ or 'y-axis'	B1: Both correct asymptotes and no extra ones.	
	Special case $x \neq 0$ and $y \neq 4$ scores B1B0		
			(2)
(c)	$\frac{dy}{dx} = -3x^{-2}$	$\frac{dy}{dx} = kx^{-2}$ (Allow $\frac{dy}{dx} = kx^{-2} + 4$ )	M1
	At $x = -3$ , gradient of curve = $-\frac{1}{3}$	Cao (may be un-simplified but must be a fraction with no powers) e.g. $-3(-3)^{-2}$ scores A0 unless evaluated as e.g. $\frac{-3}{9}$ or is implied by their normal gradient.	A1
	Gradient of normal = $-1/m$	Correct perpendicular gradient rule applied to a numerical gradient that must have come from substituting $x = -3$ into their derivative. <b>Dependent on the previous M1.</b>	dM1
	Normal at P is $(y - 3) = 3(x + 3)$	M1: Correct straight line method using $(-3, 3)$ and a "changed" gradient. A wrong equation with no formula quoted is M0. <b>Also dependent on the first M1.</b>	dM1A1
		A1: Any correct equation	
			(5)
(d)	$(-4, 0)$ and $(0, 12)$ .	Both correct (May be seen on a sketch)	B1
	So AB has length $\sqrt{160}$ or $AB^2$ has length 160	M1: Correct use of Pythagoras for their A and B one of which lies on the x-axis and the other on the y-axis, obtained from their equation in (c). A correct method for $AB^2$ or AB. A1: $\sqrt{160}$ or better e.g. $4\sqrt{10}$ with no errors seen	M1 A1cso
			(3)
			[11]