Centre No.						Paper Reference	Surname	Initial(s)
Candidate No.						6 6 6 3 / 0 1	Signature	

Paper Reference(s)

6663/01

Edexcel GCE

Core Mathematics C1

Advanced Subsidiary

Wednesday 13 May 2015 – Morning

Time: 1 hour 30 minutes

Examiner's use only

Team Leader's use only

Question Number	Leave Blank
1	
2	
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10	
Total	

Materials required for examination	**Items included with question papers**
Mathematical Formulae (Pink)	Nil

Calculators may NOT be used in this examination.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature.
Check that you have the correct question paper.
Answer ALL the questions.
You must write your answer for each question in the space following the question.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.
Full marks may be obtained for answers to ALL questions.
The marks for individual questions and the parts of questions are shown in round brackets: e.g. **(2)**.
There are 10 questions in this question paper. The total mark for this paper is 75.
There are 32 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.
You should show sufficient working to make your methods clear to the Examiner.
Answers without working may not gain full credit.

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1. Simplify

(a) $(2\sqrt{5})^2$

(1)

(b) $\dfrac{\sqrt{2}}{2\sqrt{5} - 3\sqrt{2}}$ giving your answer in the form $a + \sqrt{b}$, where a and b are integers.

(4)

Question Number	Scheme		Marks
1.(a)	20	Sight of 20. (4×5 is not sufficient)	B1
			(1)
(b)	$\dfrac{\sqrt{2}}{2\sqrt{5}-3\sqrt{2}} \times \dfrac{2\sqrt{5}+3\sqrt{2}}{2\sqrt{5}+3\sqrt{2}}$	Multiplies top and bottom by a **correct** expression. This statement is sufficient. NB $2\sqrt{5}+3\sqrt{2} \equiv \sqrt{20}+\sqrt{18}$	M1
	(Allow to multiply top and bottom by $k(2\sqrt{5}+3\sqrt{2})$)		
	$= \dfrac{...}{2}$	Obtains a denominator of 2 or sight of $\left(2\sqrt{5}-3\sqrt{2}\right)\left(2\sqrt{5}+3\sqrt{2}\right)=2$ with no errors seen in this expansion. May be implied by $\dfrac{...}{2k}$	A1
	Note that M0A1 is not possible. The 2 must come from a correct method.		
	Note that if M1 is scored there is no need to consider the numerator. **e.g.** $\dfrac{2(MR?)}{2\sqrt{5}-3\sqrt{2}} \times \dfrac{2\sqrt{5}+3\sqrt{2}}{2\sqrt{5}+3\sqrt{2}} = \dfrac{...}{2}$ scores M1A1		
	Numerator = $\sqrt{2}(2\sqrt{5}\pm 3\sqrt{2}) = 2\sqrt{10}\pm 6$	An attempt to multiply the numerator by $\pm\left(2\sqrt{5}\pm 3\sqrt{2}\right)$ and obtain an expression of the form $p+q\sqrt{10}$ where p and q are integers. This may be implied by e.g. $2\sqrt{10}+3\sqrt{4}$ or by their final answer.	M1
	(Allow attempt to multiply the numerator by $k(2\sqrt{5}\pm 3\sqrt{2})$)		
	$\dfrac{\sqrt{2}}{2\sqrt{5}-3\sqrt{2}} = \dfrac{2\sqrt{10}+6}{2} = 3+\sqrt{10}$	Cso. For the answer as written or $\sqrt{10}+3$ or a statement that a = 3 and b = 10. Score when first seen and ignore any subsequent attempt to 'simplify'. Allow $1\sqrt{10}$ for $\sqrt{10}$	A1
			(4)
			(5 marks)
	Alternative for (b)		
	$\dfrac{\sqrt{2}}{2\sqrt{5}-3\sqrt{2}} = \dfrac{1}{\sqrt{10}-3}$ or $\dfrac{2}{2\sqrt{10}-6}$	M1: Divides or multiplies top and bottom by $\sqrt{2}$ A1: $\dfrac{k}{k\left(\sqrt{10}-3\right)}$	M1A1
	$= \dfrac{1}{\sqrt{10}-3} \times \dfrac{\sqrt{10}+3}{\sqrt{10}+3}$	M1: Multiplies top and bottom by $\sqrt{10}+3$	M1
	$= 3+\sqrt{10}$		A1
2.	$y-2x-4=0,\quad 4x^2+y^2+20x=0$		

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2. Solve the simultaneous equations

$$y - 2x - 4 = 0$$

$$4x^2 + y^2 + 20x = 0$$

(7)

Question Number	Scheme		Marks
1.(a)	20	Sight of 20. (4×5 is not sufficient)	B1
			(1)
(b)	$\frac{\sqrt{2}}{2\sqrt{5}-3\sqrt{2}} \times \frac{2\sqrt{5}+3\sqrt{2}}{2\sqrt{5}+3\sqrt{2}}$	Multiplies top and bottom by a **correct** expression. This statement is sufficient. NB $2\sqrt{5}+3\sqrt{2} \equiv \sqrt{20}+\sqrt{18}$	M1
	(Allow to multiply top and bottom by $k(2\sqrt{5}+3\sqrt{2})$)		
	$= \frac{...}{2}$	Obtains a denominator of 2 or sight of $\left(2\sqrt{5}-3\sqrt{2}\right)\left(2\sqrt{5}+3\sqrt{2}\right)=2$ with no errors seen in this expansion. May be implied by $\frac{...}{2k}$	A1
	Note that M0A1 is not possible. The 2 must come from a correct method.		
	Note that if M1 is scored there is no need to consider the numerator. **e.g.** $\frac{2(MR?)}{2\sqrt{5}-3\sqrt{2}} \times \frac{2\sqrt{5}+3\sqrt{2}}{2\sqrt{5}+3\sqrt{2}} = \frac{...}{2}$ scores M1A1		
	Numerator = $\sqrt{2}(2\sqrt{5} \pm 3\sqrt{2}) = 2\sqrt{10} \pm 6$	An attempt to multiply the numerator by $\pm\left(2\sqrt{5} \pm 3\sqrt{2}\right)$ and obtain an expression of the form $p + q\sqrt{10}$ where p and q are integers. This may be implied by e.g. $2\sqrt{10}+3\sqrt{4}$ or by their final answer.	M1
	(Allow attempt to multiply the numerator by $k(2\sqrt{5} \pm 3\sqrt{2})$)		
	$\frac{\sqrt{2}}{2\sqrt{5}-3\sqrt{2}} = \frac{2\sqrt{10}+6}{2} = 3+\sqrt{10}$	Cso. For the answer as written or $\sqrt{10}+3$ or a statement that a = 3 and b = 10. Score when first seen and ignore any subsequent attempt to 'simplify'. Allow $1\sqrt{10}$ for $\sqrt{10}$	A1
			(4)
			(5 marks)
	Alternative for (b)		
	$\frac{\sqrt{2}}{2\sqrt{5}-3\sqrt{2}} = \frac{1}{\sqrt{10}-3}$ or $\frac{2}{2\sqrt{10}-6}$	M1: Divides or multiplies top and bottom by $\sqrt{2}$ A1: $\frac{k}{k\left(\sqrt{10}-3\right)}$	M1A1
	$= \frac{1}{\sqrt{10}-3} \times \frac{\sqrt{10}+3}{\sqrt{10}+3}$	M1: Multiplies top and bottom by $\sqrt{10}+3$	M1
	$= 3+\sqrt{10}$		A1
2.	$y-2x-4=0,\ \ 4x^2+y^2+20x=0$		

Question Number	Scheme		Marks
	$y = 2x + 4 \Rightarrow 4x^2 + (2x+4)^2 + 20x = 0$ **or** $2x = y - 4$ or $x = \frac{y-4}{2}$ $\Rightarrow (y-4)^2 + y^2 + 10(y-4) = 0$	Attempts to rearrange the linear equation to y =... or x =... or $2x$ =... and attempts to **fully** substitute into the second equation.	M1
	$8x^2 + 36x + 16 = 0$ or $2y^2 + 2y - 24 = 0$	M1: Collects terms together to produce quadratic expression = 0. The '= 0' may be implied by later work. A1: Correct three term quadratic equation in x or y. The '= 0' may be implied by later work.	M1 A1
	$(4)(2x+1)(x+4) = 0 \Rightarrow x = ...$ or $(2)(y+4)(y-3) = 0 \Rightarrow y = ...$	Attempt to factorise and solve or complete the square and solve or uses a correct quadratic formula **for a 3 term quadratic.**	M1
	$x = -0.5, x = -4$ or $y = -4, y = 3$	Correct answers for either both values of x or both values of y (possibly un-simplified)	A1 cso
	Sub into $y = 2x + 4$ or Sub into $x = \frac{y-4}{2}$	Substitutes at least one of their values of x into a **correct** equation as far as y =... or substitutes at least one of their values of y into a **correct** equation as far as y =...	M1
	$y = 3,\ y = -4$ and $x = -4,\ x = -0.5$	Fully correct solutions and simplified. **Pairing not required.** If there are any extra values of x or y, score A0.	A1
			(7 marks)
	Special Case: Uses y = -2x - 4		
	$y = 2x + 4 \Rightarrow 4x^2 + (-2x-4)^2 + 20x = 0$		M1
	$8x^2 + 36x + 16 = 0$		M1A1
	$(4)(2x+1)(x+4) = 0 \Rightarrow x = ...$		M1
	$x = -0.5, x = -4$		A0
	Sub into $y = 2x + 4$	Sub into $y = -2x - 4$ is M0	M1
	$y = 3,\ y = -4$ and $x = -4,\ x = -0.5$		A0

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3. Given that $y = 4x^3 - \dfrac{5}{x^2}$, $x \neq 0$, find in their simplest form

(a) $\dfrac{dy}{dx}$

(3)

(b) $\int y \, dx$

(3)

Question Number	Scheme		Marks
3.	$y = 4x^3 - \frac{5}{x^2}$		
(a)	$12x^2 + \frac{10}{x^3}$	M1: $x^n \to x^{n-1}$ e.g. Sight of x^2 or x^{-3} or $\frac{1}{x^3}$	M1A1A1
		A1: $3\times 4x^2$ or $-5\times -2x^{-3}$ (oe) (Ignore + c for this mark)	
		A1: $12x^2 + \frac{10}{x^3}$ or $12x^2 + 10x^{-3}$ all on one line and no + c	
	Apply ISW here and award marks when first seen.		
			(3)
(b)	$x^4 + \frac{5}{x} + c$ or $x^4 + 5x^{-1} + c$	M1: $x^n \to x^{n+1}$. e.g. Sight of x^4 or x^{-1} or $\frac{1}{x^1}$ **Do not award for integrating their answer to part (a)**	M1A1A1
		A1: $4\frac{x^4}{4}$ or $-5\times\frac{x^{-1}}{-1}$	
		A1: For fully correct and simplified answer with + c all on one line. Allow $x^4 + 5\times\frac{1}{x} + c$ Allow $1x^4$ for x^4	
	Apply ISW here and award marks when first seen. Ignore spurious integral signs for all marks.		
			(3)
			(6 marks)

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4. (i) A sequence $U_1, U_2, U_3, \ldots$ is defined by

$$U_{n+2} = 2U_{n+1} - U_n, \quad n \geqslant 1$$

$$U_1 = 4 \text{ and } U_2 = 4$$

Find the value of

(a) U_3

(1)

(b) $\sum_{n=1}^{20} U_n$

(2)

(ii) Another sequence $V_1, V_2, V_3, \ldots$ is defined by

$$V_{n+2} = 2V_{n+1} - V_n, \quad n \geqslant 1$$

$$V_1 = k \text{ and } V_2 = 2k, \text{ where } k \text{ is a constant}$$

(a) Find V_3 and V_4 in terms of k.

(2)

Given that $\sum_{n=1}^{5} V_n = 165$,

(b) find the value of k.

(3)

Question Number	Scheme		Marks
4(i).(a)	$U_3 = 4$	cao	B1
			(1)
(b)	$\sum_{n=1}^{n=20} U_n = 4+4+4..........+4$ or 20×4	For realising that all 20 terms are 4 and that the sum is required. Possible ways are 4+4+4…..+4 or 20×4 or $\frac{1}{2}\times 20(2\times 4+19\times 0)$ or $\frac{1}{2}\times 20(4+4)$ (Use of a correct sum formula with n = 20, a = 4 and d = 0 or n = 20, a = 4 and l = 4)	M1
	= 80	cao	A1
	Correct answer with no working scores M1A1		
			(2)
(ii)(a)	$V_3 = 3k,\quad V_4 = 4k$	May score in (b) if clearly identified as V_3 and V_4	B1, B1
			(2)
(b)	$\sum_{n=1}^{n=5} V_n = k+2k+3k+4k+5k = 165$ or $\frac{1}{2}\times 5(2\times k+4\times k) = 165$ or $\frac{1}{2}\times 5(k+5k) = 165$	Attempts V_5, adds their V_1, V_2, V_3, V_4, V_5 AND sets equal to 165 or Use of a correct sum formula with $a = k$, $d = k$ and n = 5 or $a = k$, $l = 5k$ and n = 5 AND sets equal to 165	M1
	$15k = 165 \Rightarrow k = ..$	Attempts to solve their linear equation in k **having set the sum of their first 5 terms equal to 165.** Solving V_5 = 165 scores no marks.	M1
	$k = 11$	cao and cso	A1
			(3)
			(8 marks)

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5. The equation

$$(p-1)x^2 + 4x + (p-5) = 0, \text{ where } p \text{ is a constant}$$

has no real roots.

(a) Show that p satisfies $p^2 - 6p + 1 > 0$

(3)

(b) Hence find the set of possible values of p.

(4)

Question Number	Scheme		Marks
5(a)	$b^2-4ac<0 \Rightarrow$ e.g. $4^2-4(p-1)(p-5)<0$ or $0>4^2-4(p-1)(p-5)$ or $4^2<4(p-1)(p-5)$ or $4(p-1)(p-5)>4^2$	M1: Attempts to use b^2-4ac with at least two of a, b or c correct. May be in the quadratic formula. Could also be, for example, comparing or equating b^2 and $4ac$. Must be considering the given quadratic equation. Inequality sign not needed for this M1.There must be no x terms. A1: For a correct un-simplified **inequality** that is not the given answer	M1A1
	$4<p^2-6p+5$		
	$p^2-6p+1>0$	Correct solution with **no** errors that includes an expansion of $(p-1)(p-5)$	A1*
			(3)
(b)	$p^2-6p+1=0 \Rightarrow p=...$	For an attempt to solve $p^2-6p+1=0$ (**not <u>their</u> quadratic**) leading to 2 solutions for p (do not allow attempts to **factorise** – must be using the quadratic formula or completing the square)	M1
	$p=3\pm\sqrt{8}$	$p=3\pm2\sqrt{2}$ or any equivalent correct expressions e.g. $p=\dfrac{6\pm\sqrt{32}}{2}$ (May be implied by their inequalities) Discriminant must be a single number not e.g. 36 - 4	A1
	Allow the M1A1 to score anywhere for solving the given quadratic		
	$p<3-\sqrt{8}$ or $p>3+\sqrt{8}$	M1: Chooses outside region – **not dependent on the previous method mark** A1: $p<3-\sqrt{8}$, $p>3+\sqrt{8}$ or equivalent e.g. $p<\dfrac{6-\sqrt{32}}{2}$, $p>\dfrac{6+\sqrt{32}}{2}$ $\left(-\infty,\ 3-\sqrt{8}\right)\cup\left(3+\sqrt{8},\ \infty\right)$ Allow ",", "or" or a space between the answers but do **not** allow $p<3-\sqrt{8}$ **and** $p>3+\sqrt{8}$ (this scores M1A0) **Apply ISW if necessary.**	M1A1
A correct solution to the quadratic followed by $p>3\pm\sqrt{8}$ scores M1A1M0A0			
$3+\sqrt{8}<p<3-\sqrt{8}$ scores M1A0			
Allow candidates to use x rather than p but must be in terms of p for the final A1			
			(4)
			(7 marks)

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6. The curve C has equation

$$y = \frac{(x^2 + 4)(x - 3)}{2x}, \quad x \neq 0$$

(a) Find $\frac{dy}{dx}$ in its simplest form.

(5)

(b) Find an equation of the tangent to C at the point where $x = -1$

Give your answer in the form $ax + by + c = 0$, where a, b and c are integers.

(5)

Question Number	Scheme		Marks
6(a)	$(x^2+4)(x-3)=x^3-3x^2+4x-12$	Attempt to multiply out the numerator to get a cubic with 4 terms and at least 2 correct	M1
	$\dfrac{x^3-3x^2+4x-12}{2x}=\dfrac{x^2}{2}-\dfrac{3}{2}x+2-6x^{-1}$	M1: Attempt to divide each term by 2*x*. The powers of *x* of at least two terms must follow from their expansion. Allow an attempt to multiply by $2x^{-1}$ A1: Correct expression. May be un-simplified but powers of *x* must be combined e.g. $\dfrac{x^2}{2}$ not $\dfrac{x^3}{2x}$	M1A1
	$\dfrac{dy}{dx}=x-\dfrac{3}{2}+\dfrac{6}{x^2}$ oe e.g. $\dfrac{2x^3-3x^2+12}{2x^2}$	ddM1: $x^n\to x^{n-1}$ or $2\to 0$ **Dependent on both previous method marks.** A1: $x-\dfrac{3}{2}+\dfrac{6}{x^2}$ oe and **isw** Accept $1x$ or even $1x^1$ but not $\dfrac{2x}{2}$ and not x^0. If they lose the previous A1 because of an **incorrect constant only** then allow recovery here and in part (b) for a correct derivative.	ddM1A1
			(5)
	See appendix for alternatives using product/quotient rule		
(b)	At $x=-1,\ y=10$	Correct value for *y*	B1
	$\left(\dfrac{dy}{dx}=\right)-1-\dfrac{3}{2}+\dfrac{6}{1}=3.5$	M1: Substitutes $x=-1$ into their expression for d*y*/d*x* A1: 3.5 oe cso	M1A1
	$y-{}'10'={}'3.5'(x--1)$	Uses their **tangent** gradient **which must come from calculus** with $x=-1$ and their numerical *y* with a correct straight line method. If using $y=mx+c$, this mark is awarded for correctly establishing a value for *c*.	M1
	$2y-7x-27=0$	$\pm k(2y-7x-27)=0$ cso	A1
			(5)
			(10 marks)

Leave blank

7. Given that $y = 2^x$,

(a) express 4^x in terms of y.

(1)

(b) Hence, or otherwise, solve

$$8(4^x) - 9(2^x) + 1 = 0$$

(4)

Question Number	Scheme		Marks
7.(a)	$\left(4^x =\right) y^2$	Allow y^2 or $y \times y$ or "*y* squared" "$4^x =$" not required	B1
	Must be seen in part (a)		
			(1)
(b)	$8y^2 - 9y + 1 = (8y-1)(y-1) = 0 \Rightarrow y = ...$ or $(8(2^x)-1)((2^x)-1) = 0 \Rightarrow 2^x = ...$	For attempting to solve the given equation as a **3 term quadratic** in *y* or as a **3 term quadratic** in 2^x leading to a value of *y* or 2^x (Apply usual rules for solving the quadratic – see general guidance) Allow *x* (or any other letter) instead of *y* for this mark e.g. an attempt to solve $8x^2 - 9x + 1 = 0$	M1
	$2^x (\text{or } y) = \frac{1}{8},\ 1$	Both correct answers of $\frac{1}{8}$ (oe) and 1 for 2^x or *y* or their letter but **<u>not *x*</u>** unless $2^x (\text{or } y)$ is implied later	A1
	$x = -3 \quad x = 0$	M1: A correct attempt to find one **numerical value** of *x* from their $2^x (\text{or } y)$ **which must have come from a 3 term quadratic equation**. If logs are used then they must be evaluated. A1: Both $x = -3$ and/or $x = 0$ May be implied by e.g. $2^{-3} = \frac{1}{8}$ and $2^0 = 1$ **and no extra values.**	M1A1
			(4)
			(5 marks)

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8. (a) Factorise completely $9x - 4x^3$

(3)

(b) Sketch the curve C with equation

$$y = 9x - 4x^3$$

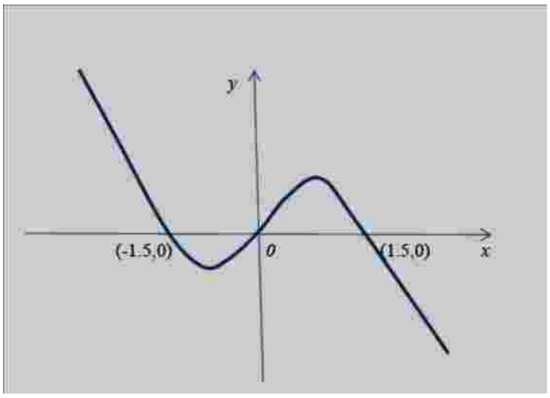
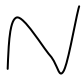
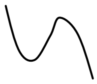
Show on your sketch the coordinates at which the curve meets the x-axis.

(3)

The points A and B lie on C and have x coordinates of –2 and 1 respectively.

(c) Show that the length of AB is $k\sqrt{10}$ where k is a constant to be found.

(4)

Question Number	Scheme		Marks
8(a)	$9x-4x^3 = x(9-4x^2)$ or $-x(4x^2-9)$	Takes out a common factor of x or $-x$ **correctly.**	B1
	$9-4x^2=(3+2x)(3-2x)$ or $4x^2-9=(2x-3)(2x+3)$	$9-4x^2=(\pm3\pm2x)(\pm3\pm2x)$ or $4x^2-9=(\pm2x\pm3)(\pm2x\pm3)$	M1
	$9x-4x^3 = x(3+2x)(3-2x)$	Cao but allow equivalents e.g. $x(-3-2x)(-3+2x)$ or $-x(2x+3)(2x-3)$	A1
Note: $4x^3-9x = x(4x^2-9) = x(2x-3)(2x+3)$ so $9x-4x^3 = x(3-2x)(2x+3)$ **would score full marks**			
	Note: Correct work leading to $9x\left(1-\frac{2}{3}x\right)\left(1+\frac{2}{3}x\right)$ **would score full marks**		
	Allow ($x \pm 0$) or ($-x \pm 0$) instead of x and $-x$		
			(3)
(b)		 or  A cubic shape with one maximum and one minimum	M1
		Any line or curve drawn passing through (not touching) the origin	B1
		Must be the correct shape and in all four quadrants and pass through (-1.5, 0) and (1.5, 0) (Allow (0, -1.5) and (0, 1.5) or just -1.5 and 1.5 provided they are positioned correctly). **Must be on the diagram** (Allow $\sqrt{\frac{9}{4}}$ for 1.5)	A1
			(3)
(c)	$A=(-2,\ 14),\quad B=(1,\ 5)$	B1: y = 14 **or** y = 5 B1: y = 14 **and** y = 5	B1 B1
	These must be seen or used in (c)		
	$(AB=)\sqrt{(-2-1)^2+(14-5)^2}\ \left(=\sqrt{90}\right)$	**Correct** use of Pythagoras <u>including the square root.</u> Must be a correct expression for their A and B if a correct formula is not quoted	M1
	E.g. $AB=\sqrt{(-2+1)^2+(14-5)^2}$ **scores M0.** **However** $AB=\sqrt{(y_2-y_1)^2+(x_2-x_1)^2}=\sqrt{(-2+1)^2+(14-5)^2}$ **scores M1**		
	$(AB=)3\sqrt{10}$	cao	A1
			(4)
			(10 marks)
Special case: Use of $4x^3 - 9x$ for the curve gives (-2, -14) and (1, -5) in part (c). Allow this to score a maximum of B0B0M1A1 as a special case in part (c) as the length AB comes from equivalent work.			

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9. Jess started work 20 years ago. In year 1 her annual salary was £17 000. Her annual salary increased by £1 500 each year, so that her annual salary in year 2 was £18 500, in year 3 it was £20 000 and so on, forming an arithmetic sequence. This continued until she reached her maximum annual salary of £32 000 in year *k*. Her annual salary then remained at £32 000.

(a) Find the value of the constant *k*.

(2)

(b) Calculate the total amount that Jess has earned in the 20 years.

(5)

Question Number	Scheme		Marks
9.(a)	$32000 = 17000 + (k-1)\times 1500 \Rightarrow k = ...$	Use of 32000 with a **correct** formula in an attempt to find *k*. A correct formula could be implied by a correct answer.	M1
	$(k =)\ 11$	Cso (Allow $n = 11$)	A1
	Accept correct answer only.		
	$32000 = 17000 + 1500k \Rightarrow k = 10$ is M0A0 (wrong formula) $\frac{32000-17000}{1500} = 10 \therefore k = 11$ is M1A1 (correct formula implied)		
	Listing: All terms must be listed up to 32000 and 11 correctly identified. A solution that scores 2 if fully correct and 0 otherwise.		
			(2)
(b)	M1: $S = \frac{k}{2}(2\times 17000 + (k-1)\times 1500)$ or $\frac{k}{2}(17000+32000)$ $S = \frac{k-1}{2}(2\times 17000 + (k-2)\times 1500)$ or $\frac{k-1}{2}(17000+30500)$	M1: Use of correct sum formula with their **integer** $n = k$ or $k - 1$ from part (a) where $3 < k < 20$ and $a = 17000$ and $d = 1500$. **See below for special case for using $n = 20$.**	M1A1
	A1: $S = \frac{11}{2}(2\times 17000 + 10\times 1500)$ or $\frac{11}{2}(17000+32000)$ $S = \frac{10}{2}(2\times 17000 + 9\times 1500)$ or $\frac{10}{2}(17000+30500)$ (= 269 500 or 237 500)	A1: Any correct un-simplified numerical expression with $n = 11$ or $n = 10$	
	$32000\times\alpha$	$32000\times\alpha$ where α is an integer and $3 < \alpha < 18$	M1
	288 000 + 269 500 = 557 500 or 320 000 + 237 500 = 557 500	M1: Attempts to add their two values. It is dependent upon the two previous M's being scored and must be the sum of 20 terms i.e. $\alpha + k = 20$ A1: 557 500	ddM1A1
	Special Case: If they just find S_{20} (£625 000) in (b) score the first M1 otherwise apply the scheme.		
			(5)
			(7 marks)

Listing:

n	1	2	3	4	5	6	7	8	9	10
u_n	17000	18500	20000	21500	23000	24500	26000	27500	29000	30500
n	11	12	13	14	15	16	17	18	19	20
u_n	32000	32000	32000	32000	32000	32000	32000	32000	32000	32000

Look for a sum before awarding marks. Award the M's as above then A2 for 557 500
If they sum the 'parts' separately then apply the scheme.

Leave blank

10. A curve with equation $y = f(x)$ passes through the point (4, 9).

Given that

$$f'(x) = \frac{3\sqrt{x}}{2} - \frac{9}{4\sqrt{x}} + 2, \quad x > 0$$

(a) find f(x), giving each term in its simplest form.

(5)

Point P lies on the curve.

The normal to the curve at P is parallel to the line $2y + x = 0$

(b) Find the x coordinate of P.

(5)

Question Number	Scheme		Marks
10(a)	$\mathrm{f}(x)=x^{\frac{3}{2}}-\frac{9}{2}x^{\frac{1}{2}}+2x(+c)$	M1: $x^n \to x^{n+1}$ A1: Two terms in *x* correct, simplification is not required in coefficients or powers A1: All terms in *x* correct. Simplification not required in coefficients or powers and + c is not required	M1A1A1
	Sub $x=4, y=9$ into $\mathrm{f}(x)\Rightarrow c=...$	M1: Sub *x* = 4, *y* = 9 into f (*x*) to obtain a value for *c*. If no + *c* then M0. Use of *x* = 9, *y* = 4 is M0.	M1
	$(\mathrm{f}(x)=)x^{\frac{3}{2}}-\frac{9}{2}x^{\frac{1}{2}}+2x+2$	Accept equivalents **but must be simplified** e.g. $\mathrm{f}(x)=x^{\frac{3}{2}}-4.5\sqrt{x}+2x+2$ Must be all 'on one line' **and simplified**. Allow $x\sqrt{x}$ for $x^{\frac{3}{2}}$	A1
			(5)
(b)	Gradient of normal is $-\frac{1}{2}\Rightarrow$ Gradient of tangent = +2	M1: Gradient of $2y+x=0$ is $\pm\frac{1}{2}(m)\Rightarrow\frac{\mathrm{d}y}{\mathrm{d}x}=-\frac{1}{\pm\frac{1}{2}}$ A1: Gradient of tangent = +2 (May be implied)	M1A1
	The A1 may be implied by $\frac{-1}{\frac{3\sqrt{x}}{2}-\frac{9}{4\sqrt{x}}+2}=-\frac{1}{2}$		
	$\frac{3\sqrt{x}}{2}-\frac{9}{4\sqrt{x}}+2=2\Rightarrow\frac{3\sqrt{x}}{2}-\frac{9}{4\sqrt{x}}=0$	Sets the given $\mathrm{f}'(x)$ **or their** $\mathrm{f}'(x)$ = their **changed** *m* and **not** their *m* where *m* has come from 2*y* + *x* = 0	M1
	$\times 4\sqrt{x}\Rightarrow 6x-9=0\Rightarrow x=..$	$\times 4\sqrt{x}$ or equivalent **correct algebraic** processing (**allow sign/arithmetic errors only**) and attempt to solve to obtain a value for *x*. If $\mathrm{f}'(x)\neq 2$ they need to be solving a three term quadratic in $\sqrt{x}$ correctly and square to obtain a value for *x*. **Must be using the given** $\mathrm{f}'(x)$ **for this mark.**	M1
	$x=1.5$	$x=\frac{3}{2}$ (1.5) Accept equivalents e.g . $x=\frac{9}{6}$ **If any 'extra' values are not rejected, score A0.**	A1
			(5)
	Beware $\frac{-1}{\frac{3\sqrt{x}}{2}-\frac{9}{4\sqrt{x}}+2}=-\frac{1}{2}\Rightarrow\frac{-2}{3\sqrt{x}}+\frac{4\sqrt{x}}{9}-\frac{1}{2}=-\frac{1}{2}$ etc. leads to the correct answer and could score M1A1M1M0(incorrect processing)A0		
			(10 marks)

Appendix

6(a)

Way 2 Quotient	$(x^2+4)(x-3)=x^3-3x^2+4x-12$	Attempt to multiply out the numerator to get a cubic with 4 terms and at least 2 correct	M1
	$\frac{\mathrm{d}y}{\mathrm{d}x}=\frac{2x\left(3x^2-6x+4\right)-2\left(x^3-3x^2+4x-12\right)}{(2x)^2}$	M1: Correct application of quotient rule A1: Correct derivative	M1A1
	$=\frac{4x^3}{4x^2}-\frac{6x^2}{4x^2}+\frac{24}{4x^2}=x-\frac{3}{2}+\frac{6}{x^2}$ oe e.g. $\frac{2x^3-3x^2+12}{2x^2}$	M1: Collects terms and divides by denominator. **Dependent on both previous method marks.** A1: $x-\frac{3}{2}+\frac{6}{x^2}$ oe and **isw** Accept $1x$ or even $1x^1$ but not $\frac{2x}{2}$ and not x^0.	ddM1A1
Way 3 Product	$y=\left(\frac{x}{2}+\frac{2}{x}\right)(x-3)$ or $\left(x^2+4\right)\left(\frac{1}{2}-\frac{3}{2x}\right)$	Divides one bracket by $2x$	M1
	$\frac{\mathrm{d}y}{\mathrm{d}x}=(x-3)\left(\frac{1}{2}-\frac{2}{x^2}\right)+\left(\frac{x}{2}+\frac{2}{x}\right)$ or $\frac{\mathrm{d}y}{\mathrm{d}x}=\left(x^2+4\right)\frac{3}{2x^2}+2x\left(\frac{1}{2}-\frac{3}{2x}\right)$	M1: Correct application of product rule A1: Correct derivative	M1A1
	$=\frac{3}{2}+\frac{6}{x^2}+x-3=x-\frac{3}{2}+\frac{6}{x^2}$ oe e.g. $\frac{2x^3-3x^2+12}{2x^2}$	M1: Expands and collects terms. **Dependent on both previous method marks.** A1: $x-\frac{3}{2}+\frac{6}{x^2}$ oe and **isw** Accept $1x$ or even $1x^1$ but not $\frac{2x}{2}$ and not x^0.	ddM1A1
Way 4 Product	$(x^2+4)(x-3)=x^3-3x^2+4x-12$	Attempt to multiply out the numerator to get a cubic with 4 terms and at least 2 correct	M1
	$\frac{\mathrm{d}y}{\mathrm{d}x}=\left(x^3-3x^2+4x-12\right)\times-\frac{1}{2}x^{-2}+\frac{1}{2}x^{-1}\left(3x^2-6x+4\right)$ M1: Correct application of product rule A1: Correct derivative		M1A1
	$\frac{\mathrm{d}y}{\mathrm{d}x}=-\frac{x}{2}+\frac{3}{2}-\frac{2}{x}+\frac{6}{x^2}+\frac{3x}{2}-3+\frac{2}{x}=x-\frac{3}{2}+\frac{6}{x^2}$ ddM1: Expands and collects terms **Dependent on both previous method marks.** A1: $x-\frac{3}{2}+\frac{6}{x^2}$ oe e.g. $\frac{2x^3-3x^2+12}{2x^2}$ and **isw**. Accept $1x$ or even $1x^1$ but not $\frac{2x}{2}$ and not x^0.		ddM1A1

Way 5	$y=\left(\frac{x}{2}+\frac{2}{x}\right)(x-3)$ or $(x^2+4)\left(\frac{1}{2}-\frac{3}{2x}\right)$	Divides one bracket by $2x$	M1
	$=\frac{x^2}{2}-\frac{3}{2}x+2-6x^{-1}$	M1: Expands A1: Correct expression	M1A1
	$\frac{dy}{dx}=x-\frac{3}{2}+\frac{6}{x^2}$ oe e.g. $\frac{2x^3-3x^2+12}{2x^2}$	ddM1: $x^n \to x^{n-1}$ or $2 \to 0$ **Dependent on both previous method marks.** A1: $x-\frac{3}{2}+\frac{6}{x^2}$ oe and **isw** Accept $1x$ or even $1x^1$ but not $\frac{2x}{2}$ If they lose the previous A1 because of an **incorrect constant only** then allow recovery here for a correct derivative.	ddM1A1