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**Mathematics C2** 

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Centre No.					Pape	er Refer	ence			Surname	Initial(s)
Candidate No.			6	6	6	4	/	0	1	Signature	

Paper Reference(s)

6664/01

# **Edexcel GCE**

# **Core Mathematics C2 Advanced Subsidiary**

Monday 2 June 2008 – Morning

Time: 1 hour 30 minutes

Materials required for examination<br/>Mathematical Formulae (Green)Items included with question papers<br/>Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

### **Instructions to Candidates**

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions. Write your answers in the spaces provided in this question paper. When a calculator is used, the answer should be given to an appropriate degree of accuracy.

### **Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 9 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

### **Advice to Candidates**

You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

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	$f(x) = 2x^3 - 3x^2 - 39x + 20$	
(a) Use the factor than	orem to show that $(x + 4)$ is a factor of $f(x)$ .	
(a) Osc the factor the	$\text{if the show that } (x + 4) \text{ is a factor of } \Gamma(x).$	(2)
(1) F ( ; (())	1.41	
(b) Factorise $f(x)$ com	pletely.	(4)
		(-)

Question number	Scheme	Marks	
1.	(a) Attempt to find f(-4) or f(4). $(f(-4) = 2(-4)^3 - 3(-4)^2 - 39(-4) + 20)$ (= -128 - 48 + 156 + 20) = 0, so $(x + 4)$ is a factor.	M1 A1	(2)
	(b) $2x^3 - 3x^2 - 39x + 20 = (x+4)(2x^2 - 11x + 5)$	M1 A1	
	or $(2x-1)(x-5)$ (The 3 brackets need not be written together)	M1 A1cso	(4)
			6
	(a) Long division scores no marks in part (a). The <u>factor theorem</u> is required. However, the first two marks in (b) can be earned from division seen in (a) but if a different long division result is seen in (b), the work seen in (b) takes precedence for marks in (b).		
	A1 requires zero and a simple <u>conclusion</u> (even just a tick, or Q.E.D.), or may be scored by a <u>preamble</u> , e.g. 'If $f(-4) = 0$ , $(x + 4)$ is a factor'		
	(b) First M requires use of $(x + 4)$ to obtain $(2x^2 + ax + b)$ , $a \ne 0$ , $b \ne 0$ , even with a remainder. Working need not be seen this could be done 'by inspection'. Second M for the attempt to factorise their three-term quadratic. Usual rule: $(kx^2 + ax + b) = (px + c)(qx + d)$ , where $ cd  =  b $ and $ pq  =  k $ . If 'solutions' appear before or after factorisation, ignore but factors must be seen to score the second M mark.		
	Alternative (first 2 marks): $(x+4)(2x^2 + ax + b) = 2x^3 + (8+a)x^2 + (4a+b)x + 4b = 0$ , then compare coefficients to find values of a and b. [M1] a = -11, $b = 5$ [A1]		
	Alternative:		
	Factor theorem: Finding that $f\left(\frac{1}{2}\right) = 0$ : factor is, $(2x-1)$ [M1, A1] Finding that $f(5) = 0$ : factor is, $(x-5)$ [M1, A1]		
	Finding that $f(5) = 0$ : factor is, $(x-5)$ [M1, A1]		
	"Combining" all 3 factors is <u>not</u> required.  If just one of these is found, score the <u>first 2 marks</u> M1 A1 M0 A0.		
	Losing a factor of 2: $(x+4)\left(x-\frac{1}{2}\right)(x-5)$ scores M1 A1 M1 A0.		
	Answer only, one sign wrong: e.g. $(x+4)(2x-1)(x+5)$ scores M1 A1 M1 A0		

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2.

$$y = \sqrt{(5^x + 2)}$$

(a) Complete the table below, giving the values of y to 3 decimal places.

X	0	0.5	1	1.5	2
у			2.646	3.630	

**(2)** 

(b) Use the trapezium rule, with all the values of y from your table, to find an approximation for the value of  $\int_0^2 \sqrt{(5^x + 2)} dx$ .

**(4)** 

Question number	Scheme	Marks	
2.	(a) 1.732, 2.058, 5.196 awrt (One or two correct B1 B0, All correct B1 B1)	B1 B1	(2)
	(b) $\frac{1}{2} \times 0.5$	B1	
	$\dots \{(1.732 + 5.196) + 2(2.058 + 2.646 + 3.630)\}$	M1 A1ft	
	= 5.899 (awrt 5.9, allowed even after minor slips in values)	A1	(4) 6
	(a) Accept awrt (but <u>less</u> accuracy loses these marks). Also accept <u>exact</u> answers, e.g. $\sqrt{3}$ at $x = 0$ , $\sqrt{27}$ or $3\sqrt{3}$ at $x = 2$ .		
	(b) For the M mark, the first bracket must contain the 'first and last' values, and the second bracket must have no additional values. If the only mistake is to omit one of the values from the second bracket, this can be considered as a slip and the M mark can be allowed.		
	Bracketing mistake: i.e. $\frac{1}{2} \times 0.5(1.732 + 5.196) + 2(2.058 + 2.646 + 3.630)$		
	scores B1 M1 A0 A0 <u>unless</u> the final answer implies that the calculation has been done correctly (then full marks can be given).		
	$\underline{x}$ values: M0 if the values used in the brackets are $x$ values instead of $y$ values. Alternative:		
	Separate trapezia may be used, and this can be marked equivalently.		
	$\left[ \frac{1}{4} (1.732 + 2.058) + \frac{1}{4} (2.058 + 2.646) + \frac{1}{4} (2.646 + 3.630) + \frac{1}{4} (3.630 + 5.196) \right]$		

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	$(1 + ax)^{10}$ , where a is a non-zero constant. Give each term in its simplest form.	(4)
(	Given that, in this expansion, the coefficient of $x^3$ is double the coefficient of $x^2$ ,	
(	b) find the value of a.	(2)
		(-)

Question number	Scheme	Marks	
3.	(a) $(1+ax)^{10} = 1+10ax$ (Not unsimplified versions) $10\times9$ (2) $10\times9\times8$ (3) Fig. 1. (C. 1) (1) (2) (3)	B1	
	$+\frac{10\times9}{2}(ax)^2 + \frac{10\times9\times8}{6}(ax)^3$ Evidence from one of these terms is sufficient	M1	
	$+45(ax)^2$ , $+120(ax)^3$ or $+45a^2x^2$ , $+120a^3x^3$	A1, A1	(4)
	(b) $120a^3 = 2 \times 45a^2$ $a = \frac{3}{4}$ or equiv. $\left(\text{e.g.} \frac{90}{120}, 0.75\right)$ Ignore $a = 0$ , if seen	M1 A1	(2)
			6
	(a) The terms can be 'listed' rather than added.  M1: Requires correct structure: 'binomial coefficient' (perhaps from Pascal's triangle) and the correct power of x.  (The M mark can also be given for an expansion in descending powers of x).  Allow 'slips' such as:  \[ \frac{10 \times 9}{2} ax^2,  \frac{10 \times 9}{3 \times 2} (ax)^3,  \frac{10 \times 9}{2} x^2,  \frac{9 \times 8 \times 7}{3 \times 2} a^3 x^3 \]  However, \(45 + a^2 x^2 + 120 + a^3 x^3\) or similar is M0.  \[ \begin{align*} \left(10) \\ 2\end{and} \begin{align*} \left(10) \\ 3\end{and} \begin{align*} \left(10) \\		
	this takes precedence.  Special case:  If $(ax)^2$ and $(ax)^3$ are seen within the working, but then lost  A1 A0 can be given if $45ax^2$ and $120ax^3$ are both achieved.		
	(b) M: Equating their coefficient of $x^3$ to twice their coefficient of $x^2$ or equating their coefficient of $x^2$ to twice their coefficient of $x^3$ .  ( or coefficients can be correct coefficients rather than their coefficients). Allow this mark even if the equation is trivial, e.g. $120a = 90a$ .  An equation in $a$ alone is required for this M mark, although		
	condone, e.g. $120a^3x^3 = 90a^2x^2 \Rightarrow (120a^3 = 90a^2 \Rightarrow) a = \frac{3}{4}$ .  Beware: $a = \frac{3}{4}$ following $120a = 90a$ , which is A0.		

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<b>4.</b> (a) Find, to 3 significant figures, the value of x for which $5^x = 7$ .	(2)
(b) Solve the equation $5^{2x} - 12(5^x) + 35 = 0$ .	(4)

Question number	Scheme	Marks	
4.	(a) $x = \frac{\log 7}{\log 5}$ or $x = \log_5 7$ (i.e. correct method up to $x =$ )	M1	
	1.21 Must be this answer (3 s.f.)	A1	(2)
	(b) $(5^x - 7)(5^x - 5)$ Or another variable, e.g. $(y - 7)(y - 5)$ , even $(x - 7)(x - 5)$	M1 A1	
	$(5^x = 7 \text{ or } 5^x = 5)$ $x = 1.2 \text{ (awrt)}$ ft from the answer to (a), if used $x = 1$ (allow 1.0 or 1.00 or 1.000)	A1ft B1	(4) <b>6</b>
	(a) 1.21 with no working: M1 A1 (even if it left as $5^{1.21}$ ).		
	Other answers which round to 1.2 with no working: M1 A0.		
	(b) M: Using the <u>correct</u> quadratic equation, attempt to factorise $(5^x \pm 7)(5^x \pm 5)$ , or attempt quadratic formula.		
	Allow $\log_5 7$ or $\frac{\log 7}{\log 5}$ instead of 1.2 for A1ft.		
	No marks for simply substituting a decimal answer from (a) into the given equation (perhaps showing that it gives approximately zero).		
	However, note the following special case: Showing that $5^x = 7$ satisfies the given equation, therefore 1.21 is a solution scores 0, 0, 1, 0 (and could score <u>full marks</u> if the $x = 1$ were also found). e.g. If $5^x = 7$ , then $5^{2x} = 49$ , and $5^{2x} - 12(5^x) + 35 = 49 - 84 + 35 = 0$ , so one solution is $x = 1.21$ ('conclusion' must be seen).		
	To score this special case mark, values substituted into the equation must be exact. Also, the mark would not be scored in the following case: e.g. If $5^x = 7$ , $5^{2x} - 84 + 35 = 0 \implies 5^{2x} = 49 \implies x = 1.21$		
	(Showing no appreciation that $5^{2x} = (5^x)^2$ )		
	B1: Do not award this mark if $x = 1$ clearly follows from wrong working.		

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(b) Find an equation for the tangent to $C$ at $P$ , giving your answer in the form $ax+by+c=0$ , where $a$ , $b$ and $c$ are integers. (5)	(a)	Find an equation for <i>C</i> .	(4)
	(b)	Find an equation for the tangent to $C$ at $P$ , giving your answer in the form $ax + by + c = 0$ , where $a$ , $b$ and $c$ are integers	
		ax + by + c = 0, where $a, b$ and $c$ are integers.	(5)

Question number	Scheme	Marks	
5.	(a) $(8-3)^2 + (3-1)^2$ or $\sqrt{(8-3)^2 + (3-1)^2}$	M1 A1	
	$(x \pm 3)^2 + (y \pm 1)^2 = k$ or $(x \pm 1)^2 + (y \pm 3)^2 = k$ (k a positive <u>value</u> )	M1	
	$(x-3)^2 + (y-1)^2 = 29$ $(\underline{\text{Not}} (\sqrt{29})^2 \text{ or } 5.39^2)$	A1	(4)
	(b) Gradient of radius = $\frac{2}{5}$ (or exact equiv.) Must be seen or used in (b)	B1	
	Gradient of tangent = $\frac{-5}{2}$ (Using perpendicular gradient method)	M1	
	$y-3 = \frac{-5}{2}(x-8)$ (ft gradient of radius, dependent upon <u>both</u> M marks)	M1 A1ft	
	5x + 2y - 46 = 0 (Or equiv., equated to zero, e.g. $92 - 4y - 10x = 0$ ) (Must have <u>integer</u> coefficients)	A1	(5) <b>9</b>
	(a) For the M mark, condone one slip inside a bracket, e.g. $(8-3)^2 + (3+1)^2$ , $(8-1)^2 + (1-3)^2$ The first two marks may be gained implicitly from the circle equation.		
	(b) $2^{nd}$ M: Eqn. of line through (8, 3), in any form, with any grad.(except 0 or $\infty$ ). If the 8 and 3 are the 'wrong way round', this M mark is only given if a correct general formula, e.g. $y - y_1 = m(x - x_1)$ , is quoted.  Alternative: $2^{nd}$ M: Using (8, 3) and an $m$ value in $y = mx + c$ to find a value of $c$ .  Alft: as in main scheme.  (Correct substitution of 8 and 3, then a wrong $c$ value will still score the Alft)		
	(b) <u>Alternatives for the first 2 marks</u> : (but in these 2 cases the 1 <sup>st</sup> A mark is <u>not</u> ft) (i) Finding gradient of tangent by <u>implicit</u> differentiation		
	$2(x-3) + 2(y-1)\frac{dy}{dx} = 0  \text{(or equivalent)}$ B1		
	Subs. $x = 8$ and $y = 3$ into a 'derived' expression to find a value for $\frac{dy}{dx}$ M1		
	(ii) Finding gradient of tangent by differentiation of $y = 1 + \sqrt{20 + 6x - x^2}$		
	$\frac{dy}{dx} = \frac{1}{2} (20 + 6x - x^2)^{-\frac{1}{2}} (6 - 2x)  \text{(or equivalent)}$ B1		
	Subs. $x = 8$ into a 'derived' expression to find a value for $dy/dx$ M1		
	Another alternative: Using $xx_1 + yy_1 + g(x + x_1) + f(y + y_1) + c = 0$		
	8x + 3y, $-3(x+8) - (y+3) - 19 = 0$ M1, M1 A1ft (ft from circle eqn.)		
	5x + 2y - 46 = 0  A1		

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**6.** A geometric series has first term 5 and common ratio  $\frac{4}{5}$ .

Calculate

(a) the 20th term of the series, to 3 decimal places,

**(2)** 

(b) the sum to infinity of the series.

**(2)** 

Given that the sum to k terms of the series is greater than 24.95,

(c) show that  $k > \frac{\log 0.002}{\log 0.8}$ 

(4)

(d) find the smallest possible value of k.

**(1)** 

Question number	Scheme	Marks	
6.	(a) $T_{20} = 5 \times \left(\frac{4}{5}\right)^{19} = 0.072$ (Accept awrt) Allow $5 \times \frac{4}{5}^{19}$ for M1	M1 A1	(2)
	(b) $S_{\infty} = \frac{5}{1 - 0.8} = 25$	M1 A1	(2)
	(c) $\frac{5(1-0.8^k)}{1-0.8} > 24.95$ (Allow with = or <)	M1	
	$1-0.8^k > 0.998$ (or equiv., see below) (Allow with = or <)	A1	
	$k \log 0.8 < \log 0.002$ or $k > \log_{0.8} 0.002$ (Allow with = or <)	M1	
	$k > \frac{\log 0.002}{\log 0.8} \tag{*}$	Alcso	(4)
	(d) $k = 28$ (Must be this integer value) Not $k > 27$ , or $k < 28$ , or $k > 28$	B1	(1)
			9
	(a) and (b): Correct answer without working scores both marks.		
	(a) M: Requires use of the correct formula $ar^{n-1}$ .		
	(b) M: Requires use of the correct formula $\frac{a}{1-r}$		
	(c) 1 <sup>st</sup> M: The sum may have already been 'manipulated' (perhaps wrongly), but this mark can still be allowed.		
	$1^{st}$ A: A 'numerically correct' version that has dealt with $(1-0.8)$ denominator,		
	e.g. $1 - \left(\frac{4}{5}\right)^k > 0.998$ , $5(1 - 0.8^k) > 4.99$ , $25(1 - 0.8^k) > 24.95$ ,		
	$5 - 5(0.8^k) > 4.99$ . In any of these, $\frac{4}{5}$ instead of 0.8 is fine,		
	and condone $\frac{4}{5}^k$ if correctly treated later.		
	$2^{\text{nd}}$ M: Introducing logs and using laws of logs correctly (this must include dealing with the power k so that $p^k = k \log p$ ).		
	$2^{\text{nd}}$ A: An <u>incorrect</u> statement (including equalities) at any stage in the working loses this mark (this is often identifiable at the stage $k \log 0.8 > \log 0.002$ ).		
	(So a fully correct method with inequalities is required.)		

7.

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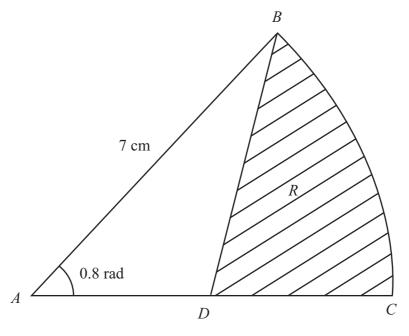


Figure 1

Figure 1 shows ABC, a sector of a circle with centre A and radius 7 cm.

Given that the size of  $\angle BAC$  is exactly 0.8 radians, find

(a) the length of the arc BC,

**(2)** 

(b) the area of the sector ABC.

**(2)** 

The point D is the mid-point of AC. The region R, shown shaded in Figure 1, is bounded by CD, DB and the arc BC.

Find

(c) the perimeter of R, giving your answer to 3 significant figures,

(4)

(d) the area of R, giving your answer to 3 significant figures.

**(4)** 

Question number	Scheme	Marks	
7.	(a) $r\theta = 7 \times 0.8 = 5.6$ (cm)	M1 A1	(2)
	(b) $\frac{1}{2}r^2\theta = \frac{1}{2} \times 7^2 \times 0.8 = 19.6 \text{ (cm}^2)$	M1 A1	(2)
	(c) $BD^2 = 7^2 + (\text{their } AD)^2 - (2 \times 7 \times (\text{their } AD) \times \cos 0.8)$	M1	
	$BD^{2} = 7^{2} + 3.5^{2} - (2 \times 7 \times 3.5 \times \cos 0.8)$ (or awrt 46° for the angle)	A1	
	(BD = 5.21) Perimeter = (their $DC$ ) + "5.6" + "5.21" = 14.3 (cm) (Accept awrt)	M1 A1	(4)
	(d) $\triangle ABD = \frac{1}{2} \times 7 \times (\text{their } AD) \times \sin 0.8$ (or awrt 46° for the angle) (ft their $AD$ )	M1 A1ft	
	(= 8.78)		
	(If the correct formula $\frac{1}{2}ab\sin C$ is <u>quoted</u> the use of any two of the sides of		
	$\triangle ABD$ as a and b scores the M mark).		
	Area = " $19.6$ " – " $8.78$ " = $10.8$ (cm <sup>2</sup> ) (Accept awrt)	M1 A1	(4)
			12
	Units (cm or cm <sup>2</sup> ) are not required in any of the answers.  (a) and (b): Correct answers without working score both marks.		
	(a) M: Use of $r\theta$ (with $\theta$ in radians), or equivalent (could be working in degrees with a correct degrees formula).		
	(b) M: Use of $\frac{1}{2}r^2\theta$ (with $\theta$ in radians), or equivalent (could be working in		
	degrees with a correct degrees formula).		
	(c) $1^{\text{st}}$ M: Use of the (correct) cosine rule formula to find $BD^2$ or $BD$ .  Any other methods need to be complete methods to find $BD^2$ or $BD$ . $2^{\text{nd}}$ M: Adding their $DC$ to their arc $BC$ and their $BD$ .		
	Beware: If 0.8 is used, but calculator is in degree mode, this can still earn M1 A1 (for the required expression), but this gives $BD = 3.50$ so the perimeter may appear as $3.5 + 5.6 + 3.5$ (earning M1 A0).		
	(d) $1^{st}$ M: Use of the (correct) area formula to find $\triangle ABD$ .		
	Any other methods need to be complete methods to find $\triangle ABD$ . $2^{\text{nd}}$ M: Subtracting their $\triangle ABD$ from their sector $ABC$ .		
	Using segment formula $\frac{1}{2}r^2(\theta - \sin \theta)$ scores no marks in part (d).		

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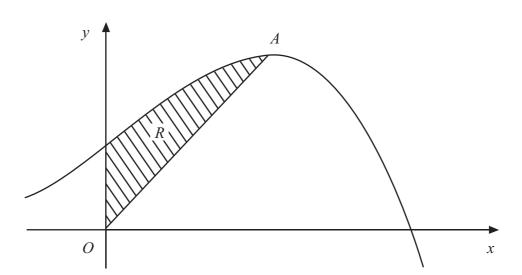


Figure 2

Figure 2 shows a sketch of part of the curve with equation  $y = 10 + 8x + x^2 - x^3$ .

The curve has a maximum turning point A.

(a) Using calculus, show that the x-coordinate of A is 2.

**(3)** 

The region R, shown shaded in Figure 2, is bounded by the curve, the y-axis and the line from O to A, where O is the origin.

(b) Using calculus, find the exact area of R.



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Question number	Scheme	Marks	
8.	(a) $\left(\frac{dy}{dx}\right) = 8 + 2x - 3x^2$ (M: $x^n \to x^{n-1}$ for one of the terms, <u>not</u> just $10 \to 0$ )	M1 A1	
	$3x^2 - 2x - 8 = 0$ $(3x + 4)(x - 2) = 0$ $x = 2$ (Ignore other solution) (*)	Alcso	(3)
	(b) Area of triangle = $\frac{1}{2} \times 2 \times 22$ (M: Correct method to find area of triangle)	M1 A1	
	(Area = 22 with no working is acceptable)		
		M1 A1 A1	
	$\left[10x + \frac{8x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4}\right]_0^2 = \dots$ (Substitute limit 2 into a 'changed function') $\left[ = 20 + 16 + \frac{8}{3} - 4 \right]$ (This M can be awarded even if the other limit is wrong)	M1	
	Area of $R = 34\frac{2}{3} - 22 = \frac{38}{3} \left( = 12\frac{2}{3} \right)$ (Or 12.6)	M1 A1	(8)
	M: Dependent on use of calculus in (b) and correct overall 'strategy': subtract either way round.  A: Must be exact, not 12.67 or similar.  A negative area at the end, even if subsequently made positive, loses the A mark.		11
	(a) The final mark may also be scored by <u>verifying</u> that $\frac{dy}{dx} = 0$ at $x = 2$ .		11
	(b) Alternative:		
	Eqn. of line $y = 11x$ . (Marks dependent on subsequent use in integration) (M1: Correct method to find equation of line. A1: Simplified form $y = 11x$ )	M1 A1	
	$\int 10 + kx + x^2 - x^3 dx = 10x + \frac{kx^2}{2} + \frac{x^3}{3} - \frac{x^4}{4}$ (k perhaps -3)	M1 A1 A1	
	$\left[10x + \frac{kx^2}{2} + \frac{x^3}{3} - \frac{x^4}{4}\right]_0^2 = \dots $ (Substitute limit 2 into a 'changed function')	M1	
	Area of $R = \left[10x - \frac{3x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4}\right]_0^2 = 20 - 6 + \frac{8}{3} - 4 = \frac{38}{3}$ $\left(=12\frac{2}{3}\right)$	M1 A1	(8)
	Final M1 for $\int (\text{curve}) - \int (\text{line})$ or $\int (\text{line}) - \int (\text{curve})$ .		

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9.	Solve, for $0 \le x < 360^{\circ}$ ,	

- - (a)  $\sin(x-20^\circ) = \frac{1}{\sqrt{2}}$

**(4)** 

(b)  $\cos 3x = -\frac{1}{2}$ 

**(6)** 





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Question number	Scheme	Marks	
9.	(a) 45 ( $\alpha$ ) (This mark can be implied by an answer 65) $180 - \alpha$ , Add 20 (for at least one angle)	B1 M1, M1	
	<ul> <li>65 155</li> <li>(b) 120 or 240 (β): (This mark can be implied by an answer 40 or 80)</li> <li>(Could be achieved by working with 60, using 180 – 60 and/or180 + 60)</li> </ul>	A1 B1	(4)
	$360 - \beta$ , $360 + \beta$ (or $120 + $ an angle that has been divided by 3) Dividing by 3 (for at least one angle)	M1, M1 M1	
	40 80 160 200 280 320 First A1: at least 3 correct	A1 A1	(6) <b>10</b>
	<ul> <li>(a) Extra solution(s) in range: Loses the A mark. Extra solutions outside range: Ignore (whether correct or not). Common solutions: 65 (only correct solution) will score 65 (and 115 will score B1 M0 M1 A0 (2 marks) B1 M0 M1 A0 (2 marks) 44.99 (or similar) for α is B0, and 64.99, 155.01 (or similar) is A0.</li> </ul>		
	(b) Extra solution(s) in range: Loses the final A mark.  Extra solutions outside range: Ignore (whether correct or not).  Common solutions:  40 (only correct solution) will score  40 and 80 (only correct solutions)  B1 M0 M0 M1 A0 A0 (2 marks)  40 and 320 (only correct solutions)  B1 M0 M0 M1 A0 A0 (2 marks)  B1 M0 M0 M1 A0 A0 (2 marks)		
	Answers without working: Full marks can be given (in both parts), B and M marks by implication.		
	Answers given in radians:  Deduct a maximum of 2 marks (misread) from B and A marks. (Deduct these at first and second occurrence.)		
	Answers that begin with statements such as $\sin(x-20) = \sin x - \sin 20$ or		
	$\cos x = -\frac{1}{6}$ , then go on to find a value of '\alpha' or '\beta', however badly, can		
	continue to earn the first M mark in either part, but will score <u>no further marks</u> .		
	Possible misread: $\cos 3x = \frac{1}{2}$ , giving 20, 100, 140, 220, 260, 340		
	Could score up to 4 marks B0 M1 M1 M1 A0 A1 for the above answers.		