

Centre No.						Paper Reference							Surname	Initial(s)
Candidate No.						6	6	6	4	/	0	1	Signature	

Paper Reference(s)

6664/01

Edexcel GCE

Core Mathematics C2

Advanced Subsidiary

Friday 9 January 2009 – Morning

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

Materials required for examination

Mathematical Formulae (Green)

Items included with question papers

Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer for each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet ‘Mathematical Formulae and Statistical Tables’ is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 10 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.

You should show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

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1. Find the first 3 terms, in ascending powers of x , of the binomial expansion of $(3 - 2x)^5$, giving each term in its simplest form.

(4)

Q1

(Total 4 marks)



H 3 0 9 5 7 A 0 3 2 8

January 2009
6664 Core Mathematics C2
Mark Scheme

Question Number	Scheme	Marks
1	$(3 - 2x)^5 = 243, \dots + 5 \times (3)^4 (-2x) = -810x \dots$ $+ \frac{5 \times 4}{2} (3)^3 (-2x)^2 = +1080x^2$	B1, B1 M1 A1 (4) [4]
Notes	<p>First term must be 243 for B1, writing just 3^5 is B0 (Mark their final answers except in second line of special cases below).</p> <p>Term must be simplified to $-810x$ for B1</p> <p>The x is required for this mark.</p> <p>The method mark (M1) is generous and is awarded for an attempt at Binomial to get the third term.</p> <p>There must be an x^2 (or no x- i.e. not wrong power) and attempt at Binomial Coefficient and at dealing with powers of 3 and 2. The power of 3 should not be one, but the power of 2 may be one (regarded as bracketing slip).</p> <p>So allow $\binom{5}{2}$ or $\binom{5}{3}$ or 5C_2 or 5C_3 or even $\left(\frac{5}{2}\right)$ or $\left(\frac{5}{3}\right)$ or use of '10' (maybe from Pascal's triangle)</p> <p>May see ${}^5C_2(3)^3(-2x)^2$ or ${}^5C_2(3)^3(-2x^2)$ or ${}^5C_2(3)^5(-\frac{2}{3}x^2)$ or $10(3)^3(2x)^2$ which would each score the M1</p> <p>A1 is c.a.o and needs $1080x^2$ (if $1080x^2$ is written with no working this is awarded both marks i.e. M1 A1.)</p>	
Special cases	<p>$243 + 810x + 1080x^2$ is B1B0M1A1 (condone no negative signs)</p> <p>Follows correct answer with $27 - 90x + 120x^2$ can isw here (sp case)– full marks for correct answer</p> <p>Misreads <i>ascending</i> and gives $-32x^5 + 240x^4 - 720x^3$ is marked as B1B0M1A0 special case and must be completely correct. (<i>If any slips could get B0B0M1A0</i>)</p> <p>Ignores 3 and expands $(1 \pm 2x)^5$ is 0/4</p> <p>$243, -810x, 1080x^2$ is full marks but $243, -810, 1080$ is B1,B0,M1,A0</p> <p>NB Alternative method $3^5(1 - \frac{2}{3}x)^5 = 3^5 - 5 \times 3^5 \times (\frac{2}{3}x) + \binom{5}{3} 3^5 (-\frac{2}{3}x)^2 + \dots$ is B0B0M1A0</p> <p>– answers must be simplified to $243 - 810x + 1080x^2$ for full marks (awarded as before)</p> <p>Special case $3(1 - \frac{2}{3}x)^5 = 3 - 5 \times 3 \times (\frac{2}{3}x) + \binom{5}{3} 3(-\frac{2}{3}x)^2 + \dots$ is B0, B0, M1, A0</p> <p>Or $3(1 - 2x)^5$ is B0B0M0A0</p>	

2.

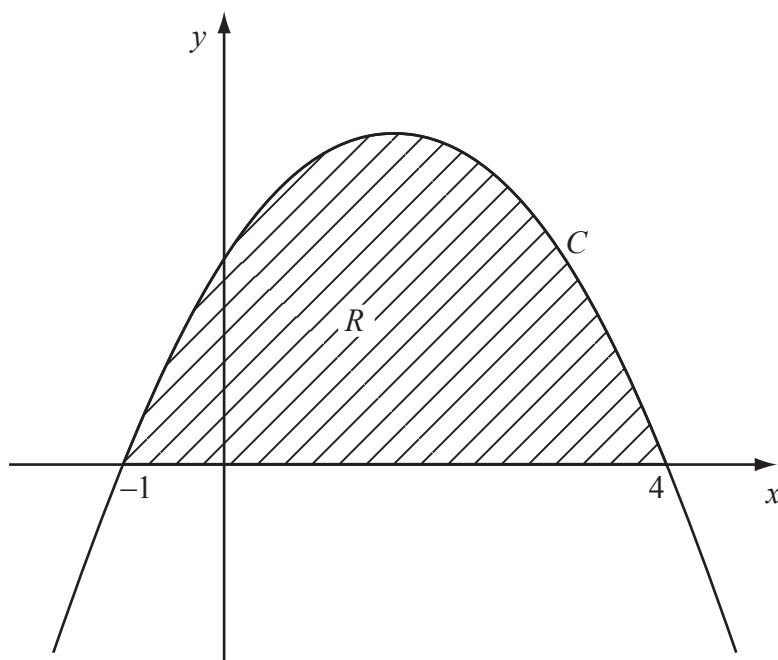


Figure 1

Figure 1 shows part of the curve C with equation $y = (1+x)(4-x)$.

The curve intersects the x -axis at $x = -1$ and $x = 4$. The region R , shown shaded in Figure 1, is bounded by C and the x -axis.

Use calculus to find the exact area of R .

(5)



Question Number	Scheme	Marks
2	$y = (1+x)(4-x) = 4 + 3x - x^2$ M: Expand, giving 3 (or 4) terms $\int (4 + 3x - x^2) dx = 4x + \frac{3x^2}{2} - \frac{x^3}{3}$ M: Attempt to integrate $= [\dots\dots\dots]_{-1}^4 = \left(16 + 24 - \frac{64}{3}\right) - \left(-4 + \frac{3}{2} + \frac{1}{3}\right) = \frac{125}{6} \quad \left(= 20\frac{5}{6}\right)$	M1 M1 A1 M1 A1 (5) [5]
Notes	<p>M1 needs expansion, there may be a slip involving a sign or simple arithmetical error e.g. $1 \times 4 = 5$, but there needs to be a 'constant' an 'x term' and an 'x^2 term'. The x terms do not need to be collected. (Need not be seen if next line correct)</p> <p>Attempt to integrate means that $x^n \rightarrow x^{n+1}$ for at least one of the terms, then M1 is awarded (even 4 becoming $4x$ is sufficient) – one correct power sufficient.</p> <p>A1 is for correct answer only, not follow through. But allow $2x^2 - \frac{1}{2}x^2$ or any correct equivalent. Allow $+c$, and even allow an evaluated extra constant term.</p> <p>M1: Substitute limit 4 and limit -1 into a changed function (must be -1) and indicate subtraction (either way round).</p> <p>A1 must be exact, not 20.83 or similar. If recurring indicated can have the mark. Negative area, even if subsequently positive loses the A mark.</p>	
Special cases	<p>(i) Uses calculator method: M1 for expansion (if seen) M1 for limits if answer correct, so 0, 1 or 2 marks out of 5 is possible (Most likely M0 M0 A0 M1 A0)</p> <p>(ii) Uses trapezium rule : not exact, no calculus – 0/5 unless expansion mark M1 gained.</p> <p>(iii) Using original method, but then change all signs after expansion is likely to lead to: M1 M1 A0, M1 A0 i.e. 3/5</p>	

3.

$$y = \sqrt[3]{(10x - x^2)}.$$

(a) Complete the table below, giving the values of y to 2 decimal places.

x	1	1.4	1.8	2.2	2.6	3
y	3	3.47			4.39	

(2)

(b) Use the trapezium rule, with all the values of y from your table, to find an approximation

for the value of $\int_1^3 \sqrt{10x-x^2} \, dx$.

(4)

[illegible]

Question Number	Scheme	Marks
3		
(a)	3.84, 4.14, 4.58 (Any one correct B1 B0. All correct B1 B1)	B1 B1 (2)
(b)	$\frac{1}{2} \times 0.4, \{(3 + 4.58) + 2(3.47 + 3.84 + 4.14 + 4.39)\}$ = 7.852 (awrt 7.9)	B1, M1 A1ft A1 (4)
[6]		
Notes	<p>(a) B1 for one answer correct Second B1 for all three correct</p> <p>Accept awrt ones given or exact answers so $\sqrt{21}$, $\sqrt{\left(\frac{369}{25}\right)}$ or $\frac{3\sqrt{41}}{5}$, and $\sqrt{\left(\frac{429}{25}\right)}$ or $\frac{\sqrt{429}}{5}$, score the marks.</p> <p>(b) B1 is for using 0.2 or $\frac{0.4}{2}$ as $\frac{1}{2}h$.</p> <p>M1 requires first bracket to contain first plus last values and second bracket to include no additional values from those in the table. If the only mistake is to omit one value from 2nd bracket this may be regarded as a slip and can be allowed (An extra repeated term forfeits the M mark however)</p> <p>x values: M0 if values used in brackets are x values instead of y values.</p> <p>Separate trapezia may be used : B1 for 0.2, M1 for $\frac{1}{2}h(a+b)$ used 4 or 5 times (and A1ft all e.g.. $0.2(3 + 3.47) + 0.2(3.47 + 3.84) + 0.2(3.84 + 4.14) + 0.2(4.14 + 4.58)$ is M1 A0 equivalent to missing one term in { } in main scheme</p> <p>A1ft follows their answers to part (a) and is for {correct expression}</p> <p>Final A1 must be correct. (No follow through)</p>	
Special cases	<p>Bracketing mistake: i.e. $\frac{1}{2} \times 0.4(3 + 4.58) + 2(3.47 + 3.84 + 4.14 + 4.39)$</p> <p>scores B1 M1 A0 A0 <u>unless</u> the final answer implies that the calculation has been done correctly (then full marks can be given).</p> <p>Need to see trapezium rule – answer only (with no working) is 0/4.</p>	

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4. Given that $0 < x < 4$ and

$$\log_5(4-x) - 2\log_5 x = 1,$$

find the value of x .

(6)



Question Number	Scheme	Marks
4	$2 \log_5 x = \log_5 (x^2), \quad \log_5 (4-x) - \log_5 (x^2) = \log_5 \frac{4-x}{x^2}$ $\log \left(\frac{4-x}{x^2} \right) = \log 5 \quad 5x^2 + x - 4 = 0 \text{ or } 5x^2 + x = 4 \text{ o.e.}$ $(5x-4)(x+1) = 0 \quad x = \frac{4}{5} \quad (x = -1)$	<p>B1, M1</p> <p>M1 A1</p> <p>dM1 A1</p> <p>(6) [6]</p>
Notes	<p>B1 is awarded for $2 \log x = \log x^2$ anywhere.</p> <p>M1 for correct use of $\log A - \log B = \log \frac{A}{B}$</p> <p>M1 for replacing 1 by $\log_k k$. A1 for correct quadratic</p> <p>$(\log(4-x) - \log x^2 = \log 5 \Rightarrow 4-x-x^2 = 5$ is B1M0M1A0 M0A0)</p> <p>dM1 for attempt to solve quadratic with usual conventions. (Only award if previous two M marks have been awarded)</p> <p>A1 for 4/5 or 0.8 or equivalent (Ignore extra answer).</p>	
Alternative 1	$\log_5 (4-x) - 1 = 2 \log_5 x \text{ so } \log_5 (4-x) - \log_5 5 = 2 \log_5 x$ $\log_5 \frac{4-x}{5} = 2 \log_5 x$ then could complete solution with $2 \log_5 x = \log_5 (x^2)$ $\left(\frac{4-x}{5} \right) = x^2 \quad 5x^2 + x - 4 = 0$ Then as in first method $(5x-4)(x+1) = 0 \quad x = \frac{4}{5} \quad (x = -1)$	<p>M1</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>dM1 A1</p> <p>(6) [6]</p>
Special cases	<p>Complete trial and error yielding 0.8 is M3 and B1 for 0.8</p> <p>A1, A1 awarded for each of two tries evaluated. i.e. 6/6</p> <p>Incomplete trial and error with wrong or no solution is 0/6</p> <p>Just answer 0.8 with no working is B1</p> <p>If log base 10 or base e used throughout - can score B1M1M1A0M1A0</p>	

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A diagram showing a circle C in the Cartesian plane. The circle passes through points $P(-3, 2)$, $Q(9, 10)$, and $R(a, 4)$. The origin is labeled O . The x and y axes are shown.

Figure 2

(a) show that $a = 13$,

(b) find an equation for C . (5)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question Number	Scheme	Marks
5		
(a)	$PQ: m_1 = \frac{10-2}{9-(-3)} (= \frac{2}{3}) \quad \text{and} \quad QR: m_2 = \frac{10-4}{9-a}$	M1
(b)	$m_1 m_2 = -1: \frac{8}{12} \times \frac{6}{9-a} = -1 \quad a = 13 \quad (*)$	M1 A1 (3)
Alt for (a)	(a) Alternative method (Pythagoras) Finds all three of the following $(9-(-3))^2 + (10-2)^2, (i.e. 208), \quad (9-a)^2 + (10-4)^2, \quad (a-(-3))^2 + (4-2)^2$ Using Pythagoras (correct way around) e.g. $a^2 + 6a + 9 = 240 + a^2 - 18a + 81$ to form equation Solve (or verify) for $a, a = 13 (*)$ (b) Centre is at (5, 3) $(r^2 =) (10-3)^2 + (9-5)^2$ or equiv., or $(d^2 =) (13-(-3))^2 + (4-2)^2$ $(x-5)^2 + (y-3)^2 = 65$ or $x^2 + y^2 - 10x - 6y - 31 = 0$	M1 M1 A1 (3) B1 M1 A1 M1 A1 (5)
Alt for (b)	Uses $(x-a)^2 + (y-b)^2 = r^2$ or $x^2 + y^2 + 2gx + 2fy + c = 0$ and substitutes (-3, 2), (9, 10) and (13, 4) then eliminates one unknown Eliminates second unknown Obtains $g = -5, f = -3, c = -31$ or $a = 5, b = 3, r^2 = 65$	M1 M1 A1, A1, B1cao (5) [8]
Notes	(a) M1 -considers gradients of PQ and QR -must be y difference / x difference (or considers three lengths as in alternative method) M1 Substitutes gradients into product = -1 (or lengths into Pythagoras' Theorem the correct way round) A1 Obtains $a = 13$ with no errors by solution or verification. Verification can score 3/3. (b) Geometrical method: B1 for coordinates of centre – can be implied by use in part (b) M1 for attempt to find r^2, d^2, r or d (allow one slip in a bracket). A1 cao. These two marks may be gained implicitly from circle equation M1 for $(x \pm 5)^2 + (y \pm 3)^2 = k^2$ or $(x \pm 3)^2 + (y \pm 5)^2 = k^2$ ft their (5,3) Allow k^2 non numerical. A1 cao for whole equation and rhs must be 65 or $(\sqrt{65})^2$, (similarly B1 must be 65 or $(\sqrt{65})^2$, in alternative method for (b))	

Question Number	Scheme	Marks
Further alternatives	<p>(i) A number of methods find gradient of $PQ = 2/3$ then give perpendicular gradient is $-3/2$ This is M1</p> <p>They then proceed using equations of lines through point Q or by using gradient QR to obtain equation such as $\frac{4-10}{a-9} = -\frac{3}{2}$ M1 (may still have x in this equation rather than a and there may be a small slip)</p> <p>They then complete to give $(a) = 13$ A1</p> <p>(ii) A long involved method has been seen finding the coordinates of the centre of the circle first.</p> <p>This can be done by a variety of methods</p> <p>Giving centre as $(c, 3)$ and using an equation such as $(c-9)^2 + 7^2 = (c+3)^2 + 1^2$ (equal radii)</p> <p>or $\frac{3-6}{c-3} = -\frac{3}{2}$ M1 (perpendicular from centre to chord bisects chord)</p> <p>Then using $c (= 5)$ to find a is M1</p> <p>Finally $a = 13$ A1</p> <p>(iii) Vector Method:</p> <p>States PQ. QR = 0, with vectors stated $12i + 8j$ and $(9-a)i + 6j$ is M1</p> <p>Evaluates scalar product so $108 - 12a + 48 = 0$ (M1)</p> <p>solves to give $a = 13$ (A1)</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p>

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$$f(x) = x^4 + 5x^3 + ax + b,$$

where a and b are constants.

The remainder when $f(x)$ is divided by $(x - 2)$ is equal to the remainder when $f(x)$ is divided by $(x + 1)$.

(a) Find the value of a .

(5)

Given that $(x + 3)$ is a factor of $f(x)$,

(b) find the value of b .

(3)

[illegible]

Question Number	Scheme	Marks
6	<p>(a) $f(2) = 16 + 40 + 2a + b$ or $f(-1) = 1 - 5 - a + b$</p> <p>Finds 2nd remainder and equates to 1st $\Rightarrow 16 + 40 + 2a + b = 1 - 5 - a + b$</p> <p>$a = -20$</p> <p>(b) $f(-3) = (-3)^4 + 5(-3)^3 - 3a + b = 0$</p> <p>$81 - 135 + 60 + b = 0$ gives $b = -6$</p>	<p>M1 A1</p> <p>M1 A1</p> <p>A1cso (5)</p> <p>M1 A1ft</p> <p>A1 cso</p> <p>(3)</p> <p>[8]</p>
Alternative for (a)	<p>(a) Uses long division, to get remainders as $b + 2a + 56$ or $b - a - 4$ or correct equivalent</p> <p>Uses second long division as far as remainder term, to get $b + 2a + 56 = b - a - 4$ or correct equivalent</p> <p>$a = -20$</p>	<p>M1 A1</p> <p>M1 A1</p> <p>A1cso (5)</p>
Alternative for (b)	<p>(b) Uses long division of $x^4 + 5x^3 - 20x + b$ by $(x + 3)$ to obtain $x^3 + 2x^2 - 6x + a + 18$ (with their value for a)</p> <p>Giving remainder $b + 6 = 0$ and so $b = -6$</p>	<p>M1 A1ft</p> <p>A1 cso</p> <p>(3)</p> <p>[8]</p>
Notes	<p>(a) M1 : Attempts $f(\pm 2)$ or $f(\pm 1)$</p> <p>A1 is for the answer shown (or simplified with terms collected) for one remainder</p> <p>M1: Attempts other remainder and puts one equal to the other</p> <p>A1: for correct equation in a (and b) then A1 for $a = -20$ cso</p> <p>(b) M1 : Puts $f(\pm 3) = 0$</p> <p>A1 is for $f(-3) = 0$, (where f is original function), with no sign or substitution errors (follow through on 'a' and could still be in terms of a)</p> <p>A1: $b = -6$ is cso.</p>	
Alternatives	<p>(a) M1: Uses long division of $x^4 + 5x^3 + ax + b$ by $(x \pm 2)$ or by $(x \pm 1)$ as far as three term quotient</p> <p>A1: Obtains at least one correct remainder</p> <p>M1: Obtains second remainder and puts two remainders (no x terms) equal</p> <p>A1: correct equation A1: correct answer $a = -20$ following correct work.</p> <p>(b) M1: complete long division as far as constant (ignore remainder)</p> <p>A1ft: needs correct answer for their a</p> <p>A1: correct answer</p>	
<p>Beware: It is possible to get correct answers with wrong working. If remainders are equated to 0 in part (a) both correct answers are obtained fortuitously. This could score M1A1M0A0A0M1A1A0</p>		

7.

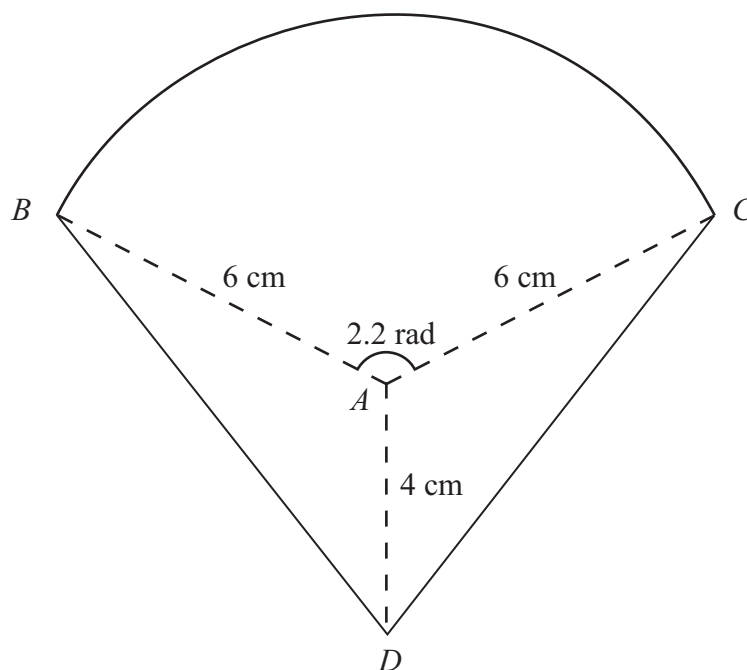


Figure 3

The shape BCD shown in Figure 3 is a design for a logo.

The straight lines DB and DC are equal in length. The curve BC is an arc of a circle with centre A and radius 6 cm. The size of $\angle BAC$ is 2.2 radians and $AD = 4$ cm.

Find

- (a) the area of the sector BAC , in cm^2 , (2)
- (b) the size of $\angle DAC$, in radians to 3 significant figures, (2)
- (c) the complete area of the logo design, to the nearest cm^2 . (4)



Question Number	Scheme	Marks
7	<p>(a) $\frac{1}{2}r^2\theta = \frac{1}{2} \times 6^2 \times 2.2 = 39.6 \text{ (cm}^2\text{)}$</p> <p>(b) $\left(\frac{2\pi - 2.2}{2}\right) \pi - 1.1 = 2.04 \text{ (rad)}$</p> <p>(c) $\Delta DAC = \frac{1}{2} \times 6 \times 4 \sin 2.04 \text{ } (\approx 10.7)$</p> <p>Total area = sector + 2 triangles = 61 $\text{(cm}^2\text{)}$</p>	<p>M1 A1 (2)</p> <p>M1 A1 (2)</p> <p>M1 A1ft</p> <p>M1 A1 (4)</p> <p>[8]</p>
(a)	<p>M1: Needs θ in radians for this formula. Could convert to degrees and use degrees formula.</p> <p>A1: Does not need units. Answer should be 39.6 exactly. Answer with no working is M1 A1. This M1A1 can only be awarded in part (a).</p>	
(b)	<p>M1: Needs full method to give angle in radians</p> <p>A1: Allow answers which round to 2.04 (Just writes 2.04 – no working is 2/2)</p>	
(c)	<p>M1: Use $\frac{1}{2} \times 6 \times 4 \sin A$ (if any other triangle formula e.g. $\frac{1}{2}b \times h$ is used the method must be complete for this mark) (No value needed for A, but should not be using 2.2)</p> <p>A1: fit the value obtained in part (b) – need not be evaluated- could be in degrees</p> <p>M1: Uses Total area = sector + 2 triangles or other complete method</p> <p>A1: Allow answers which round to 61. (Do not need units)</p> <p>Special case degrees: Could get M0A0, M0A0, M1A1M1A0</p> <p>Special case: Use $\Delta BDC - \Delta BAC$ Both areas needed for first M1 Total area = sector + area found is second M1</p> <p>NB Just finding lengths BD, DC, and angle BDC then assuming area BDC is a sector to find area BDC is 0/4</p>	

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- $$4 \sin^2 x + 9 \cos x - 6 = 0$$

$$4 \cos^2 x - 9 \cos x + 2 = 0.$$

(2)

- $$4\sin^2 x + 9\cos x - 6 = 0,$$

(6)



Question Number	Scheme	Marks
8		
(a)	$4(1 - \cos^2 x) + 9 \cos x - 6 = 0$ $4 \cos^2 x - 9 \cos x + 2 = 0$ (*)	M1 A1 (2)
(b)	$(4 \cos x - 1)(\cos x - 2) = 0$ $\cos x = \dots, \frac{1}{4}$ $x = 75.5$ (α) $360 - \alpha, \quad 360 + \alpha$ or $720 - \alpha$ $284.5, 435.5, 644.5$	M1 A1 B1 M1, M1 A1 (6) [8]
(a)	M1: Uses $\sin^2 x = 1 - \cos^2 x$ (may omit bracket) not $\sin^2 x = \cos^2 x - 1$ A1: Obtains the printed answer without error – must have = 0	
(b)	M1: Solves the quadratic with usual conventions A1: Obtains $\frac{1}{4}$ accurately- ignore extra answer 2 but penalise e.g. -2. B1: allow answers which round to 75.5 M1: $360 - \alpha$ ft their value, M1: $360 + \alpha$ ft their value or $720 - \alpha$ ft A1: Three and only three correct exact answers in the range achieves the mark	
Special cases	In part (b) Error in solving quadratic $(4\cos x - 1)(\cos x + 2)$ Could yield, M1A0B1M1M1A1 losing one mark for the error Works in radians: Complete work in radians :Obtains 1.3 B0 . Then allow M1 M1 for $2\pi - \alpha, 2\pi + \alpha$ or $4\pi - \alpha$ Then gets 5.0, 7.6, 11.3 A0 so 2/4 Mixed answer 1.3, $360 - 1.3, 360 + 1.3, 720 - 1.3$ still gets B0M1M1A0	

9. The first three terms of a geometric series are $(k + 4)$, k and $(2k - 15)$ respectively, where k is a positive constant.

(b) Hence show that $k = 12$. (2)

(c) Find the common ratio of this series. (2)

(d) Find the sum to infinity of this series. (2)



Question Number	Scheme	Marks
9	<p>(a) Initial step: Two of: $a = k + 4$, $ar = k$, $ar^2 = 2k - 15$ Or one of: $r = \frac{k}{k+4}$, $r = \frac{2k-15}{k}$, $r^2 = \frac{2k-15}{k+4}$, Or $k = \sqrt{(k+4)(2k-15)}$ or even $k^3 = (k+4)k(2k-15)$ $k^2 = (k+4)(2k-15)$, so $k^2 = 2k^2 + 8k - 15k - 60$ Proceed to $k^2 - 7k - 60 = 0$ (*)</p> <p>(b) $(k-12)(k+5) = 0$ $k = 12$ (*)</p> <p>(c) Common ratio: $\frac{k}{k+4}$ or $\frac{2k-15}{k} = \frac{12}{16} \left(= \frac{3}{4} \text{ or } 0.75 \right)$</p> <p>(d) $\frac{a}{1-r} = \frac{16}{\left(\frac{1}{4}\right)} = 64$</p>	<p>M1 M1, A1 A1 (4)</p> <p>M1 A1 (2)</p> <p>M1 A1 (2)</p> <p>M1 A1 (2) [10]</p>
	<p>(a) M1: The ‘initial step’, scoring the first M mark, may be implied by next line of proof M1: Eliminates a and r to give valid equation in k only. Can be awarded for equation involving fractions. A1 : need some correct expansion and working and answer equivalent to required quadratic but with uncollected terms. Equations involving fractions do not get this mark. (No fractions, no brackets – could be a cubic equation) A1: as answer is printed this mark is for cso (Needs = 0) All four marks must be scored in part (a)</p> <p>(b) M1: Attempt to solve quadratic A1: This is for correct factorisation or solution and $k = 12$. Ignore the extra solution ($k = -5$ or even $k = 5$), if seen. Substitute and verify is M1 A0 Marks must be scored in part (b)</p> <p>(c) M1: Complete method to find r Could have answer in terms of k A1: 0.75 or any correct equivalent Both Marks must be scored in (c)</p> <p>(d) M1: Tries to use $\frac{a}{1-r}$, (even with $r > 1$). Could have an answer still in terms of k. A1: This answer is 64 cao.</p>	



Question Number	Scheme	Marks
10	<p>(a) $2\pi rh + 2\pi r^2 = 800$</p> <p>$h = \frac{400 - \pi r^2}{\pi r}, \quad V = \pi r^2 \left(\frac{400 - \pi r^2}{\pi r} \right) = 400r - \pi r^3 \quad (*)$</p> <p>(b) $\frac{dV}{dr} = 400 - 3\pi r^2$</p> <p>$400 - 3\pi r^2 = 0 \quad r^2 = \dots, \quad r = \sqrt{\frac{400}{3\pi}} \quad (= 6.5 \text{ (2 s.f.)})$</p> <p>$V = 400r - \pi r^3 = 1737 = \frac{800}{3} \sqrt{\frac{400}{3\pi}} \text{ (cm}^3\text{)}$</p> <p>(accept awrt 1737 or exact answer)</p> <p>(c) $\frac{d^2V}{dr^2} = -6\pi r$, Negative, \therefore maximum</p> <p>(Parts (b) and (c) should be considered together when marking)</p>	<p>B1</p> <p>M1, M1 A1 (4)</p> <p>M1 A1</p> <p>M1 A1</p> <p>M1 A1 (6)</p> <p>M1 A1 (2)</p> <p>[12]</p>
Other methods for part (c):	<p><u>Either:</u> M: Find <u>value</u> of $\frac{dV}{dr}$ on each side of "$r = \sqrt{\frac{400}{3\pi}}$" and consider sign.</p> <p>A: Indicate sign change of positive to negative for $\frac{dV}{dr}$, and conclude max.</p> <p><u>Or:</u> M: Find <u>value</u> of V on each side of "$r = \sqrt{\frac{400}{3\pi}}$" and compare with "1737".</p> <p>A: Indicate that both values are less than 1737 or 1737.25, and conclude max.</p>	
Notes	<p>(a) B1: For any correct form of this equation (may be unsimplified, may be implied by 1st M1)</p> <p>M1 : Making h the subject of their three or four term formula</p> <p>M1: Substituting expression for h into $\pi r^2 h$ (independent mark) Must now be expression in r only.</p> <p>A1: cso</p> <p>(b) M1: At least one power of r decreased by 1 A1: cao</p> <p>M1: Setting $\frac{dV}{dr} = 0$ and finding a value for correct power of r for candidate</p> <p>A1 : This mark may be credited if the value of V is correct. Otherwise answers should round to 6.5 (allow ± 6.5) or be exact answer</p> <p>M1: Substitute a positive value of r to give V A1: 1737 or 1737.25..... or exact answer</p>	

<p>(c)</p> <p>Alternative for (a)</p>	<p>M1: needs complete method e.g. attempts differentiation (power reduced) of their first derivative and considers its sign</p> <p>A1(first method) should be $-6\pi r$ (do not need to substitute r and can condone wrong r if found in (b))</p> <p>Need to conclude maximum or indicate by a tick that it is maximum.</p> <p>Throughout allow confused notation such as dy/dx for dV/dr</p> <p>$A = 2\pi r^2 + 2\pi rh$, $\frac{A}{2} \times r = \pi r^3 + \pi r^2 h$ is M1 Equate to $400r$ B1</p> <p>Then $V = 400r - \pi r^3$ is M1 A1</p>
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