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**Mathematics C2** 

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Question

1

2

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Past Paper

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Centre No.					Pape	er Refer	ence			Surname	Initial(s)
Candidate No.			6	6	6	4	/	0	1	Signature	

Paper Reference(s)

### 6664/01

## **Edexcel GCE**

## **Core Mathematics C2**

## **Advanced Subsidiary**

Wednesday 9 January 2008 – Afternoon

Time: 1 hour 30 minutes

Materials required for examination
Mathematical Formulae (Green)

Items included with question papers
Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

#### **Instructions to Candidates**

In the boxes above, write your centre number, candidate number, your surname, initial(s) and signature.

Check that you have the correct question paper.

You must write your answer for each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

#### **Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 9 questions in this question paper. The total mark for this paper is 75.

There are 24 pages in this question paper. Any blank pages are indicated.

#### **Advice to Candidates**

You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

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1. (a) Find the remainder when

 $x^3 - 2x^2 - 4x + 8$ 

is divided by

- (i) x 3,
- (ii) x + 2.

**(3)** 

(b) Hence, or otherwise, find all the solutions to the equation

$$x^3 - 2x^2 - 4x + 8 = 0.$$

**(4)** 

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## 6664 Core Mathematics C2 **Mark Scheme**

Question Number	Scheme	Marks
1. a)i)	$f(3) = 3^3 - 2 \times 3^2 - 4 \times 3 + 8$ ; = 5	M1; A1
ii)	f(-2) = (-8 - 8 + 8 + 8) = 0 (B1 on Epen, but A1 in fact) M1 is for attempt at either f(3) or f(-3) in (i) or f(-2) or f(2) in (ii).	A1 (3)
(b)	$[(x+2)](x^2-4x+4)$ (= 0 not required) [must be seen or used in (b)] $(x+2)(x-2)^2$ (= 0) (can imply previous 2 marks)	M1 A1 M1
	Solutions: $x = 2$ or $-2$ (both) or $(-2, 2, 2)$ A1 (4)	[7]
Notes: (a)	No working seen: Both answers correct scores full marks One correct ;M1 then A1B0 or A0B1, whichever appropriate.	
	Alternative (Long division)  Divide by $(x-3)$ OR $(x+2)$ to get $x^2+ax+b$ , a may be zero [M1] $x^2+x-1$ and $+5$ seen i.s.w. (or "remainder = 5") [A1] $x^2-4x+4$ and 0 seen (or "no remainder") [B1]	
(b)	First M1 requires division by a found factor ; e.g. $(x+2)$ , $(x-2)$ or what candidate thinks is a factor to get $(x^2+ax+b)$ , $a$ may be zero . First A1 for $[(x+2)]$ ( $x^2-4x+4$ ) or $(x-2)(x^2-4)$ Second M1:attempt to factorise their found quadratic. (or use formula correctly) [Usual rule: $x^2+ax+b=(x+c)(x+d)$ , $where  cd = b $ .]  N.B. Second A1 is for solutions, not factors $alternative (first two marks)$ $(x+2)(x^2+bx+c)=x^3+(2+b)x^2+(2b+c)x+2c=0$ and then compare with $x^3-2x^2-4x+8=0$ to find $b$ and $c$ . [M1] $b=-4$ , $c=4$ [A1] $alternative (first two marks)$	
2. (a)	Complete method, using terms of form $ar^k$ , to find r [e.g. <b>Dividing</b> $ar^6 = 80$ by $ar^3 = 10$ to find r; $r^6 - r^3 = 8$ is M0] $r = 2$	M1 A1 (2)
(b)	Complete method for finding a [e.g. Substituting value for $r$ into equation of form $ar^k = 10$ or 80 and finding a value for $a$ .]	M1

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2.	The fourth term of a geometric series is 10 and the seventh term of the series is 80.		lank
	For this series, find		
	(a) the common ratio,	(2)	
	(b) the first term,	(2)	
	(c) the sum of the first 20 terms, giving your answer to the nearest whole number.	(2)	

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## 6664 Core Mathematics C2 **Mark Scheme**

Question Number	Scheme	Marks
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(b)	$[(x+2)](x^2-4x+4)$ (= 0 not required) [must be seen or used in (b)] $(x+2)(x-2)^2$ (= 0) (can imply previous 2 marks)	M1 A1 M1
	Solutions: $x = 2$ or $-2$ (both) or $(-2, 2, 2)$ A1 (4)	[7]
Notes: (a)	No working seen: Both answers correct scores full marks One correct ;M1 then A1B0 or A0B1, whichever appropriate.	
	Alternative (Long division)  Divide by $(x-3)$ OR $(x+2)$ to get $x^2+ax+b$ , a may be zero [M1] $x^2+x-1$ and $+5$ seen i.s.w. (or "remainder = 5") [A1] $x^2-4x+4$ and 0 seen (or "no remainder") [B1]	
(b)	First M1 requires division by a found factor ; e.g. $(x+2)$ , $(x-2)$ or what candidate thinks is a factor to get $(x^2+ax+b)$ , $a$ may be zero . First A1 for $[(x+2)]$ ( $x^2-4x+4$ ) or $(x-2)(x^2-4)$ Second M1:attempt to factorise their found quadratic. (or use formula correctly) [Usual rule: $x^2+ax+b=(x+c)(x+d)$ , $where  cd = b $ .]  N.B. Second A1 is for solutions, not factors $alternative (first two marks)$ $(x+2)(x^2+bx+c)=x^3+(2+b)x^2+(2b+c)x+2c=0$ and then compare with $x^3-2x^2-4x+8=0$ to find $b$ and $c$ . [M1] $b=-4$ , $c=4$ [A1] $alternative (first two marks)$	
2. (a)	Complete method, using terms of form $ar^k$ , to find r [e.g. <b>Dividing</b> $ar^6 = 80$ by $ar^3 = 10$ to find r; $r^6 - r^3 = 8$ is M0] $r = 2$	M1 A1 (2)
(b)	Complete method for finding a [e.g. Substituting value for $r$ into equation of form $ar^k = 10$ or 80 and finding a value for $a$ .]	M1

Winter 2008		Mathematics C2
Past Paper (Ma	rk Scheme) This resource was created and owned by Pearson Edexcel (8 $a$ = 10) $a = \frac{5}{4} = 1\frac{1}{4}$ (equivalent single fraction or 1.25)	A1 (2)
(c)	Substituting their values of <i>a</i> and <i>r</i> into <b>correct</b> formula for sum. $S = \frac{a(r^{n} - 1)}{r - 1} = \frac{5}{4}(2^{20} - 1)  (= 1310718.75)$ 1 310 719 (only this)	M1 A1 (2) <b>[6]</b>
Notes:	(a) M1: Condone errors in powers, e.g. $ar^4 = 10$ and/or $ar^7 = 80$ , A1: For $r = 2$ , allow even if $ar^4 = 10$ and $ar^7 = 80$ used (just these) (M mark can be implied from numerical work, if used correctly)  (b) M1: Allow for numerical approach: e.g. $\frac{10}{r_c^3} \leftarrow \frac{10}{r_c^2} \leftarrow \frac{1}{r_c^3}$	
	In (a) and (b) correct answer, with no working, allow both marks.  (c) Attempt 20 terms of series and add is M1 (correct last term 65530 If formula <b>not</b> quoted, errors in applying their <i>a</i> and/or <i>r</i> is M0 Allow full marks for correct answer with no working seen.	
3. (a)	$\left(1 + \frac{1}{2}x\right)^{10} = 1 + \frac{\binom{10}{1}\left(\frac{1}{2}x\right) + \binom{10}{2}\left(\frac{1}{2}x\right)^2 + \binom{10}{3}\left(\frac{1}{2}x\right)^3}{3}$	M1 A1
	= 1 + 5x; + $\frac{45}{4}$ (or 11.25) $x^2$ + 15 $x^3$ (coeffs need to be these, i.e, sim	
<i>a</i> >	[Allow A1A0, if totally correct with unsimplified, single fraction coeffici	ents)
(b)	$(1 + \frac{1}{2} \times 0.01)^{10} = 1 + 5(0.01) + (\frac{45}{4} \text{ or} 11.25)(0.01)^2 + 15(0.01)^3$	M1 A1√
	= 1 + 0.05 + 0.001125 + 0.000015 = 1.05114 cao	A1 (3) <b>[7]</b>
Notes:	<ul> <li>(a) For M1 first A1: Consider underlined expression only.</li> <li>M1 Requires correct structure for at least two of the three terms</li> <li>(i) Must be attempt at binomial coefficients.</li> <li>(ii) Must have increasing powers of x,</li> <li>(iii) May be listed, need not be added; this applies for all marks.</li> </ul>	:

First A1: Requires all three correct terms but need not be simplified, allow  $1^{10}$  etc,  ${}^{10}C_2$  etc, and condone omission of brackets around powers of  $\frac{1}{2}x$ 

First A1 (f.t.): Substitution of (0.01) into their 4 termed expression in (a) Answer with no working scores no marks (calculator gives this answer)

Second A1: Consider as B1 for 1 + 5x

(b) For M1: Substituting their (0.01) into their (a) result

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•	(a)	Find the first 4 terms of the expansion of $\left(1+\frac{x}{2}\right)^{10}$ in ascending powers of $x$ , giving each term in its simplest form. (4)
	(b)	Use your expansion to estimate the value of $(1.005)^{10}$ , giving your answer to 5 decimal places.
		(3)

Winter 2008		Mathematics C2
Past Paper (Ma	rk Scheme) This resource was created and owned by Pearson Edexcel (8 $a$ = 10) $a = \frac{5}{4} = 1\frac{1}{4}$ (equivalent single fraction or 1.25)	A1 (2)
(c)	Substituting their values of <i>a</i> and <i>r</i> into <b>correct</b> formula for sum. $S = \frac{a(r^{n} - 1)}{r - 1} = \frac{5}{4}(2^{20} - 1)  (= 1310718.75)$ 1 310 719 (only this)	M1 A1 (2) <b>[6]</b>
Notes:	(a) M1: Condone errors in powers, e.g. $ar^4 = 10$ and/or $ar^7 = 80$ , A1: For $r = 2$ , allow even if $ar^4 = 10$ and $ar^7 = 80$ used (just these) (M mark can be implied from numerical work, if used correctly)  (b) M1: Allow for numerical approach: e.g. $\frac{10}{r_c^3} \leftarrow \frac{10}{r_c^2} \leftarrow \frac{1}{r_c^3}$	
	In (a) and (b) correct answer, with no working, allow both marks.  (c) Attempt 20 terms of series and add is M1 (correct last term 65530 If formula <b>not</b> quoted, errors in applying their <i>a</i> and/or <i>r</i> is M0 Allow full marks for correct answer with no working seen.	
3. (a)	$\left(1 + \frac{1}{2}x\right)^{10} = 1 + \frac{\binom{10}{1}\left(\frac{1}{2}x\right) + \binom{10}{2}\left(\frac{1}{2}x\right)^2 + \binom{10}{3}\left(\frac{1}{2}x\right)^3}{3}$	M1 A1
	= 1 + 5x; + $\frac{45}{4}$ (or 11.25) $x^2$ + 15 $x^3$ (coeffs need to be these, i.e, sim	
<i>a</i> >	[Allow A1A0, if totally correct with unsimplified, single fraction coeffici	ents)
(b)	$(1 + \frac{1}{2} \times 0.01)^{10} = 1 + 5(0.01) + (\frac{45}{4} \text{ or} 11.25)(0.01)^2 + 15(0.01)^3$	M1 A1√
	= 1 + 0.05 + 0.001125 + 0.000015 = 1.05114 cao	A1 (3) <b>[7]</b>
Notes:	<ul> <li>(a) For M1 first A1: Consider underlined expression only.</li> <li>M1 Requires correct structure for at least two of the three terms</li> <li>(i) Must be attempt at binomial coefficients.</li> <li>(ii) Must have increasing powers of x,</li> <li>(iii) May be listed, need not be added; this applies for all marks.</li> </ul>	:

First A1: Requires all three correct terms but need not be simplified, allow  $1^{10}$  etc,  ${}^{10}C_2$  etc, and condone omission of brackets around powers of  $\frac{1}{2}x$ 

First A1 (f.t.): Substitution of (0.01) into their 4 termed expression in (a) Answer with no working scores no marks (calculator gives this answer)

Second A1: Consider as B1 for 1 + 5x

(b) For M1: Substituting their (0.01) into their (a) result

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**4.** (a) Show that the equation

 $3\sin^2\theta - 2\cos^2\theta = 1$ 

can be written as

$$5 \sin^2 \theta = 3$$
.

**(2)** 

(b) Hence solve, for  $0^{\circ} \le \theta < 360^{\circ}$ , the equation

 $3\sin^2\theta - 2\cos^2\theta = 1,$ 

giving your answers to 1 decimal place.

**(7)** 

Winter 200		matics C2
4. (a)	This resource was created and owned by Pearson Edexcel 3 $\sin^2 \theta - 2 \cos^2 \theta = 1$	6664
	$3 \sin^2 \theta - 2 (1 - \sin^2 \theta) = 1$ (M1: Use of $\sin^2 \theta + \cos^2 \theta = 1$ )	M1
	$3\sin^2\theta - 2 + 2\sin^2\theta = 1$	
	$5 \sin^2 \theta = 3$ cso AG	A1 (2)
(b)	$\sin^2\theta = \frac{3}{5}$ , so $\sin\theta = (\pm)\sqrt{0.6}$	M1
	Attempt to solve both $\sin \theta = +$ and $\sin \theta = -$ (may be implied by later work) M1	
	$\theta$ = 50.7685° awrt $\theta$ = 50.8° (dependent on first M1 only)	A1
	$\theta \ (=180^{\circ} - 50.7685_{\circ}); = 129.23^{\circ} \text{ awrt } 129.2^{\circ}$	M1; A1 √
	[f.t. dependent on first M and 3rd M]	
	$\sin \theta = -\sqrt{0.6}$	
	θ = 230.785° and 309.23152° awrt 230.8°, 309.2° (both)	M1A1 (7) [9]
Notes:	(a) N.B: <b>AG</b> ; need to see at least one line of working after substituting cos <sup>2</sup> 6	9 .
	(b) First M1: Using $5\sin^2\theta = 3$ to find value for $\sin\theta$ or $\theta$	
	Second M1: Considering the – value for $\sin \theta$ . (usually later)	
	First A1: Given for awrt 50.8°. Not dependent on second M.	
	Third M1: For (180 – 50.8 <sub>c</sub> )°, need not see written down	
	Final M1: <b>Dependent</b> on second M (but may be implied by answers)	
	For (180 + candidate' s 50.8)° <b>or</b> (360 – 50.8 <sub>c</sub> )° <b>or equiv</b> .	
	Final A1: Requires both values. (no follow through)	
	[ Finds $\cos^2 \theta = k$ ( $k = 2/5$ ) and so $\cos \theta = (\pm)$ M1, then mark equivalently]	
	[1 mus $\cos \theta = k$ ( $k = 2/3$ ) and so $\cos \theta = (\pm)$ ivi1, then mark equivalently]	

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Given	that a and b are positive constants, solve the simultaneous equations	
	a=3b,	
	$\log_3 a + \log_3 b = 2.$	
Give y	your answers as exact numbers.	
		(6)

Winter 2008	www.mystudybro.com	Mathematics	C2
Past Paper (Mark 5.	Scheme)  This resource was created and owned by Pearson dethod 1 (Substituting a = 3b into second equation at second equation.	edexcel some stage)	6664
	Using a law of logs correctly (anywhere) e.g	$\log_3 ab = 2$ M1	
	Substitution of 3 <i>b</i> for <i>a</i> (or a/3 for b) e.g	$\log_3 3b^2 = 2$ M1	
l	Using base correctly on correctly derived log <sub>3</sub> p= q e.ç	J. $3b^2 = 3^2$ M1	
	First correct value	$b = \sqrt{3} \text{ (allow 3}^{1/2}) \qquad A1$	
Correct method to find other value ( dep. on at least first M mark)			
(	Second answer a	$= 3b = 3 \sqrt{3} \text{ or } \sqrt{27}$ A1	
1	Method 2_(Working with two equations in log₃a and log	<sub>13</sub> b)	
É	' Taking logs" of first equation and " separating" lo	$g_3 a = \log_3 3 + \log_3 b$ = 1 + log <sub>3</sub> b)	
	Solving simultaneous equations to find $\log_3 a$ or $\log_3 b$ $\log_3 a = 1\frac{1}{2}$ , $\log_3 b = \frac{1}{2}$ ]	M1	
ι	Jsing base correctly to find a or b	M1	
(	Correct value for $a$ or $b$ $a = 3 \sqrt{3}$	3 or $b = \sqrt{3}$ A1	
	Correct method for second answer, dep. on first M; correct [Ignore negative values]	ect second answer M1;	A1[6]
1	Answers must be exact; decimal answers lose both A marker are several variations on Method 1, depending on the a = 3b is used, but they should all mark as in scheme. In this method, the first three method marks on Epen are selected in the second M1: correct use of log law, second M1: substitution of a = 3b, second M1: requires using base correctly on correct in the second M1: requires using base correctly on correct in the second M1: requires using base correctly on correct in the second M1: requires using base correctly on correct in the second M1: requires using base correctly on correct in the second M1: requires using base correctly on correct in the second M1: second M	the stage at which	

6.

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Figure 1

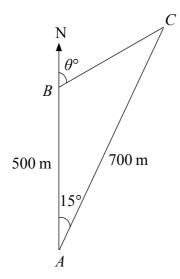


Figure 1 shows 3 yachts A, B and C which are assumed to be in the same horizontal plane. Yacht B is 500 m due north of yacht A and yacht C is 700 m from A. The bearing of C from A is 015°.

(a) Calculate the distance between yacht B and yacht C, in metres to 3 significant figures.

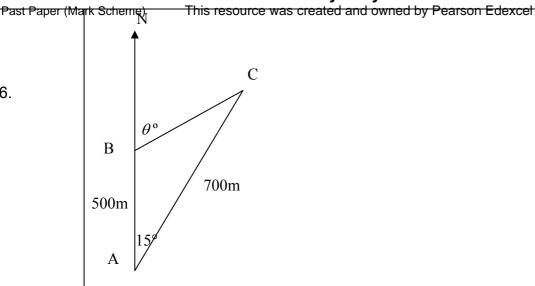
**(3)** 

The bearing of yacht C from yacht B is  $\theta^{\circ}$ , as shown in Figure 1.

(b) Calculate the value of  $\theta$ .

**(4)** 

6.



$$BC^2 = 700^2 + 500^2 - 2 \times 500 \times 700 \cos 15^\circ$$
  
( = 63851.92...)  
 $BC = 253$  awrt

Α1 (3)

M1 A1

(b)

$$\frac{\sin B}{700} = \frac{\sin 15}{\text{candidate's }BC}$$

M1

M1

A1 (4) [7]

 $\sin B = \sin 15 \times 700 / 253_c = 0.716...$  and giving an **obtuse** B (134.2°)

(Dep. on first M only, B can be acute) M1

 $\theta$  = 180 – 134.2 = (0)45.8 (allow 46 or awrt 45.7, 45.8, 45.9) [46 needs to be from correct working]

 $\theta = 180^{\circ}$  – candidate's angle B

Notes:

(a) If use cos 15° = ...., then A1 not scored until written as BC<sup>2</sup> = ... correctly

Splitting into 2 triangles BAX and CAX, where X is foot of perp. from B to AC Finding value for BX and CX and using Pythagoras M1 $BC^2 = (500\sin 15^\circ)^2 + (700 - 500\cos 15^\circ)^2$ Α1

BC = 253A 1

(b) Several alternative methods: (Showing the M marks, 3<sup>rd</sup> M dep. on first M))

(i)  $\cos B = \frac{500^2 + \text{candidate's}BC^2 - 700^2}{2.500 \text{ MHz} + BC}$  or  $700^2 = 500^2 + BC_c^2 - 2x500xBC_c$  M1 2x500xcandidate'sBC Finding angle B M1, then M1 as above

(ii) 2 triangle approach, as defined in notes for (a)

$$\tan CBX = \frac{700 - value for AX}{value for BX}$$
 M1

Finding value for  $\angle CBX$  ( $\approx 59^{\circ}$ ) M1

$$\theta = [180^{\circ} - (75^{\circ} + candidate's \angle CBX)]$$
 M1

(iii) Using sine rule (or cos rule) to find C first:

Correct use of sine or cos rule for C M1, Finding value for C M1 Either  $B = 180^{\circ} - (15^{\circ} + \text{candidate's C})$  or  $\theta = (15^{\circ} + \text{candidate's C})$  M1

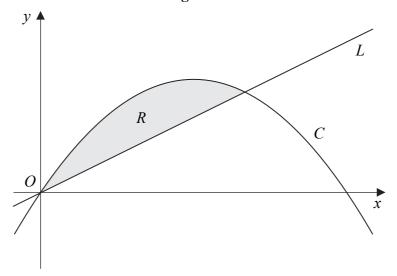
(iv)  $700 \cos 15^{\circ} = 500 + BC \cos \theta$  M2 {first two Ms earned in this case} Solving for  $\theta$ ;  $\theta = 45.8$  (allow 46 or 5.7, 45.8, 45.9 M1; A1

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7.

Figure 2



In Figure 2 the curve C has equation  $y = 6x - x^2$  and the line L has equation y = 2x.

(a) Show that the curve C intersects the x-axis at x = 0 and x = 6.

**(1)** 

(b) Show that the line L intersects the curve C at the points (0, 0) and (4, 8).

**(3)** 

The region R, bounded by the curve C and the line L, is shown shaded in Figure 2.

(c) Use calculus to find the area of R.

**(6)** 

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Past Paper (Ma 7 (a)	This resource was created and owned by Pearson Edexcel  Either solving $0 = x(6 - x)$ and showing $x = 6$ (and $x = 0$ )	B1 (1)
	or showing (6,0) (and $x = 0$ ) satisfies $y = 6x - x^2$ [allow for showing $x = 6$ ]	
(b)	Solving $2x = 6x - x^2$ $(x^2 = 4x)$ to $x =$	M1
	x = 4 (and $x = 0$ )	A1
	Conclusion: when $x = 4$ , $y = 8$ and when $x = 0$ , $y = 0$ ,	A1 (3)
	c(A)	
(c)	(Area =) $\int_{(0)}^{(4)} (6x - x^2) dx$ Limits not required	M1
	Correct integration $3x^2 - \frac{x^3}{3}$ (+ c)	A1
	Correct use of correct limits on their result above (see notes on limits)	M1
	[" $3x^2 - \frac{x^3}{3}$ "] <sup>4</sup> - [" $3x^2 - \frac{x^3}{3}$ "] <sub>0</sub> with limits substituted [= $48 - 21\frac{1}{3} = 26\frac{2}{3}$ ]	
	Area of triangle = $2 \times 8$ = 16 (Can be awarded even if no M scored, i.e. B1)	A1
	Shaded area = $\pm$ (area under curve – area of triangle ) applied correctly	M1
	$(=26\frac{2}{3}-16) = 10\frac{2}{3}$ (awrt 10.7)	A1 (6)[10]
Notes	(b) In scheme first A1: need only give $x = 4$	

(b) In scheme first A1: need only give x = 4

If verifying approach used:

Verifying (4,8) satisfies both the line and the curve M1(attempt at both),

Both shown successfully

For final A1, (0,0) needs to be mentioned; accept "clear from diagram"

- (c) Alternative Using Area =  $\pm \int_{(0)}^{(4)} \{(6x x^2); -2x\} dx$
- (i) If candidate integrates separately can be marked as main scheme If combine to work with =  $\pm \int_{(0)}^{(4)} (4x - x^2) dx$ , first M mark and third M mark =  $(\pm) \left[ 2x^2 - \frac{x^3}{3} (+c) \right]$  A1,

Correct use of correct limits on their result **second** M1,

Totally correct, unsimplified ± expression (may be implied by correct ans.) A1 [Allow this if, having given - 10<sup>2</sup>/<sub>3</sub>, they correct it]

M1 for correct use of correct limits. Must substitute correct limits for their strategy into a changed expression and subtract, either way round, e.g  $\pm \{ [ ]^4 - [ ]_0 \}$ If a long method is used, e,g, finding three areas, this mark only gained for correct strategy and all limits need to be correct for this strategy.

Use of trapezium rule: M0A0MA0,possibleA1for triangle M1(if correct application of trap. rule from x = 0 to x = 4) A0

**(2)** 

Leave

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- **8.** A circle C has centre M(6, 4) and radius 3.
  - (a) Write down the equation of the circle in the form

$$(x-a)^2 + (y-b)^2 = r^2.$$

Figure 3

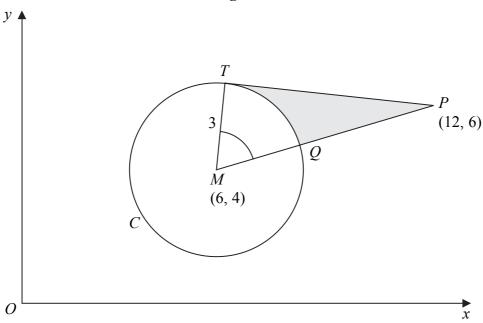


Figure 3 shows the circle C. The point T lies on the circle and the tangent at T passes through the point P (12, 6). The line MP cuts the circle at Q.

(b) Show that the angle TMQ is 1.0766 radians to 4 decimal places.

**(4)** 

The shaded region TPQ is bounded by the straight lines TP, QP and the arc TQ, as shown in Figure 3.

(c) Find the area of the shaded region TPQ. Give your answer to 3 decimal places.

**(5)** 

**A**1

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Rast Paper_((viar	k Scheme) I his resource was created and owned by Pearson Edexcel	0004	4
8	$(x-6)^2 + (y-4)^2 = ; 3^2$	B1; B1 (	(2)
` ′	$(x - 0) \cdot (y - 7) = 0$	$\mathbf{D}_{1},\mathbf{D}_{1}$	(2)

(b) Complete method for 
$$MP$$
: =  $\sqrt{(12-6)^2 + (6-4)^2}$  M1 =  $\sqrt{40}$  (= 6.325)

Complete method for 
$$\cos \theta$$
,  $\sin \theta$  or  $\tan \theta$ 

e.g.  $\cos \theta = \frac{MT}{MP} = \frac{3}{candidate's\sqrt{40}}$  (= 0.4743) ( $\theta = 61.6835^{\circ}$ )

[If 
$$TP = 6$$
 is used, then  $M0$ ]

$$\theta$$
= 1.0766 rad **AG** A1 (4)

(c) Complete method for area 
$$TMP$$
; e.g. =  $\frac{1}{2} \times 3 \times \sqrt{40} \sin \theta$  M1 =  $\frac{3}{2} \sqrt{31}$  (= 8.3516..) allow awrt 8.35 A1

Area (sector)
$$MTQ = 0.5 \times 3^2 \times 1.0766$$
 (= 4.8446...)

#### **Notes**

- (a) Allow 9 for 3<sup>2</sup>.
- (b) First M1 can be implied by √ 40

For second M1:

May find TP = 
$$\sqrt{(\sqrt{40})^2 - 3^2} = \sqrt{31}$$
, then either  $\sin \theta = \frac{TP}{MP} = \frac{\sqrt{31}}{\sqrt{40}}$  (= 0.8803...) or  $\tan \theta = \frac{\sqrt{31}}{3}$  (1.8859..) or cos rule

NB. Answer is given, but allow final A1 if all previous work is correct.

(c) First M1: (alternative) 
$$\frac{1}{2} \times 3 \times \sqrt{40-9}$$

9.

Leave blank

Figure 4

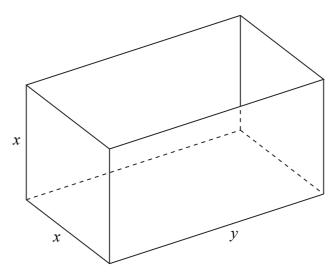


Figure 4 shows an open-topped water tank, in the shape of a cuboid, which is made of sheet metal. The base of the tank is a rectangle x metres by y metres. The height of the tank is x metres.

The capacity of the tank is 100 m<sup>3</sup>.

(a) Show that the area  $A ext{ m}^2$  of the sheet metal used to make the tank is given by

$$A = \frac{300}{x} + 2x^2 \,. \tag{4}$$

(b) Use calculus to find the value of x for which A is stationary.

(4)

(c) Prove that this value of x gives a minimum value of A.

**(2)** 

(d) Calculate the minimum area of sheet metal needed to make the tank.

**(2)** 

**Mathematics C2** Winter 2008 www.mystudybro.com Past Paper (Mark Scheme) This resource was created and owned by Pearson Edexcel (Total area ) =  $3xy + 2x^2$ B1 (a)  $x^2y = 100$   $(y = \frac{100}{r^2}, xy = \frac{100}{r})$ (Vol:) **B**1 Deriving expression for area in terms of x only M1(Substitution, or clear use of, y or xy into expression for area) (Area =)  $\frac{300}{x} + 2x^2$ A1 cso (4) (b)  $\frac{dA}{dx} = -\frac{300}{x^2} + 4x$ M1A1 Setting  $\frac{dA}{dx} = 0$  and finding a value for correct power of x, for cand. M1  $[ x^3 = 75]$ x = 4.2172 awrt 4.22 (allow exact  $\sqrt[3]{75}$ ) A1 (4) (c)  $\frac{d^2 A}{dx^2} = \frac{600}{x^3} + 4 = \text{positive}$  therefore minimum M1A1(2)Substituting found value of x into (a) M1(d) (Or finding y for found x and substituting both in  $3xy + 2x^2$ )  $[y = \frac{100}{42172^2} = 5.6228]$ Area = 106.707**A**1 awrt 107 (2)[12] **Notes** (a) First B1: Earned for correct unsimplified expression, isw. (c) For M1: Find  $\frac{d^2 A}{dr^2}$  and explicitly consider its sign, state > 0 or "positive" A1: Candidate's  $\frac{d^2A}{dr^2}$  must be correct for their  $\frac{dA}{dr}$ , sign must be + ve and conclusion "so minimum", (allow QED,  $\sqrt{\phantom{a}}$ ). ( may be wrong x, or even no value of x found) Alternative: M1: Find value of  $\frac{dA}{dx}$  on either side of " $x = \sqrt[3]{75}$ " and consider sign A1: Indicate sign change of negative to positive for  $\frac{dA}{dx}$ , and conclude minimum. OR M1: Consider values of A on either side of " $x = \sqrt[3]{75}$ " and compare with" 107" A1: Both values greater than "x = 107" and conclude minimum. Allow marks for (c) and (d) where seen; even if part labelling confused.