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Mathematics C2

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Question

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Centre No.					Pape	r Refer	ence			Surname	Initial(s)
Candidate No.			6	6	6	4	/	0	1	Signature	

# 6664/01

# **Edexcel GCE**

# Core Mathematics C2 **Advanced Subsidiary**

Wednesday 10 January 2007 – Afternoon

Time: 1 hour 30 minutes

Materials required for examination

Items included with question papers

Mathematical Formulae (Green)

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration. Thus candidates may NOT use calculators such as the Texas Instruments TI 89, TI 92, Casio CFX 9970G, Hewlett Packard HP 48G.

### **Instructions to Candidates**

In the boxes above, write your centre number, candidate number, your surname, initial(s) and signature.

Check that you have the correct question paper.

You must write your answer for each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

### **Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 10 questions in this question paper. The total mark for this paper is 75.

There are 24 pages in this question paper. Any blank pages are indicated.

### **Advice to Candidates**

You must ensure that your answers to parts of questions are clearly labelled.

You must show sufficient working to make your methods clear to the Examiner. Answers without working may gain no credit.

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Total



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Find (a) $f''(x)$ ,		$f(x) = x^3 + 3x^2 + 5.$
(a) $f''(x)$ , (b) $\int_{1}^{2} f(x) dx$ .		$1(\lambda) - \lambda + 3\lambda + 3.$
(b) $\int_{1}^{2} f(x) dx$ .	Find	
(b) $\int_{1}^{2} f(x) dx$ .	(a) $f''(x)$ ,	
(4) (b) $\int_{1}^{1} f(x) dx$ .		(3)
	(b) $\int_1^1 f(x) dx$ .	(4)

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**Mathematics C2** 

# January 2007 6664 Core Mathematics C2 Mark Scheme

Question Number	Scheme	Marks
1. (a)	$f'(x) = 3x^2 + 6x$	B1
	f''(x) = 6x + 6	M1, A1cao (3)

Notes cao = correct answer only

1(a)	
Acceptable alternatives include	B1
$3x^2 + 6x^1$ ; $3x^2 + 3 \times 2x$ ; $3x^2 + 6x + 0$	
Ignore LHS (e.g. use [whether correct or not] of $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ )	
$3x^2 + 6x + c$ or $3x^2 + 6x + c$ onstant (i.e. the written word constant) is B0	
M1 Attempt to differentiate their f '(x); $x^n \to x^{n-1}$ .	M1
$x^n \to x^{n-1}$ seen in at least one of the terms. Coefficient of $x^{}$ ignored for the method mark.	
$x^2 \rightarrow x^1$ and $x \rightarrow x^0$ are acceptable.	
Acceptable alternatives include	A1
$6x^{1} + 6x^{0}$ ; $3 \times 2x + 3 \times 2$	cao
6x + 6 + c or $6x + 6 + $ constant is A0	

### **Examples**

1(a) 
$$f''(x) = 3x^2 + 6x$$
 B1 1(a)  $f'(x) = x^2 + 3x$  B0 M0 A0  $f''(x) = x + 3$  M1 A0

1(a) 
$$f'(x) = 3x^2 + 6x$$
 B1  $f''(x) = 6x$  M1 A0 1(a)  $x^3 + 3x^2 + 5$   $= 3x^2 + 6x$  B1  $= 6x + 6$  M1 A1

1(a) 
$$y = x^3 + 3x^2 + 5$$
 1(a)  $f'(x) = 3x^2 + 6x + 5$  B0

$$\frac{dy}{dx} = 3x^2 + 3x$$
 B0  $f''(x) = 6x + 6$  M1 A1

$$\frac{d^2y}{dx^2} = 6x + 3$$
 M1 A0 1(a)  $f'(x) = 3x^2 + 6x$  B1

f ''(x) = 
$$6x + 6 + c$$
 M1 A0  
1(a) f '(x) =  $3x^2 + 6x + c$  B0  
f ''(x) =  $6x + 6$  M1 A1

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**Mathematics C2** 

Question Number	Scheme	Marks
1. (b)	$\int (x^3 + 3x^2 + 5)  \mathrm{d}x = \frac{x^4}{4} + \frac{3x^3}{3} + 5x$	M1, A1
	$\left[\frac{x^4}{4} + x^3 + 5x\right]_1^2 = 4 + 8 + 10 - \left(\frac{1}{4} + 1 + 5\right)$	M1
	$=15\frac{3}{4}$ o.e.	A1 (4) (7)

Notes o.e. = or equivalent

1(b)	
Attempt to integrate $f(x)$ ; $x^n \to x^{n+1}$	M1
Ignore incorrect notation (e.g. inclusion of integral sign)	
o.e.	A1
Acceptable alternatives include	
$\frac{x^4}{4} + x^3 + 5x$ ; $\frac{x^4}{4} + \frac{3x^3}{3} + 5x^1$ ; $\frac{x^4}{4} + \frac{3x^3}{3} + 5x + c$ ; $\int \frac{x^4}{4} + \frac{3x^3}{3} + 5x$	
N.B. If the candidate has written the integral (either $\frac{x^4}{4} + \frac{3x^3}{3} + 5x$ or what they think is the	
integral) in part (a), it may not be rewritten in (b), but the marks may be awarded if the integral is used in (b).	
Substituting 2 and 1 into any function other than $x^3 + 3x^2 + 5$ and subtracting either way round.	M1
So using their $f'(x)$ or $f''(x)$ or $\int$ their $f'(x)$ dx or $\int$ their $f''(x)$ dx will gain the M mark	
(because none of these will give $x^3 + 3x^2 + 5$ ).	
Must substitute for all x s but could make a slip.	
$4+8+10-\frac{1}{4}+1+5$ (for example) is acceptable for evidence of subtraction ('invisible'	
brackets).	
o.e. (e.g. $15\frac{3}{4}$ , $15.75$ , $\frac{63}{4}$ )	A1
Must be a single number (so $22-6\frac{1}{4}$ is A0).	
Answer only is M0A0M0A0	

**Examples** 

1(b) 
$$\int_{1}^{2} f(x) dx = 2^{3} + 3 \times 2^{2} + 5 - (1 + 3 + 5)$$
 M0 A0, M0  
= 25 - 9  
= 16 A0

(Substituting 2 and 1 into  $x^3 + 3x^2 + 5$ , so 2nd M0)

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$$1(b) \int_{1}^{2} (6x+6) dx = \left[ 3x^{2} + 6x \right]_{1}^{2} \quad M0 \text{ A0}$$

$$= 12 + 12 - (3+6) \qquad M1 \text{ A0}$$

$$= 8 + 12 - (1+3) \qquad M1 \text{ A0}$$

1(b) 
$$\frac{x^4}{4} + x^3 + 5x$$
 M1 A1  
 $\frac{2^4}{4} + 2^3 + 5 \times 2 - \frac{1^4}{4} + 1^3 + 5$  M1

(one negative sign is sufficient for evidence of subtraction)

$$=22-6\frac{1}{4}=15\frac{3}{4}$$

(allow 'recovery', implying student was using 'invisible brackets')

1(a) 
$$f(x) = x^3 + 3x^2 + 5$$
  
 $f''(x) = \frac{x^4}{4} + x^3 + 5x$  B0 M0 A0  
(b)  $\frac{2^4}{4} + 2^3 + 5 \times 2 - \frac{1^4}{4} - 1^3 - 5$  M1 A1 M1  
 $= 15\frac{3}{4}$  A1

The candidate has written the integral in part (a). It is not rewritten in (b), but the marks may be awarded as the integral is used in (b).

■ Past Paper

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(4)	$(1-2x)^5$ . Give each term in its simplest form.
show that	b) If x is small, so that $x^2$ and higher powers can be ignored
	$(1+x)(1-2x)^5 \approx 1-9x$ .
(2)	

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Question Number	Scheme	Marks
2. (a)	$(1-2x)^5 = 1 + 5 \times (-2x) + \frac{5 \times 4}{2!} (-2x)^2 + \frac{5 \times 4 \times 3}{3!} (-2x)^3 + \dots$	
	$=1-10x+40x^2-80x^3+$	B1, M1, A1, A1
		(4)
(b)	$(1+x)(1-2x)^5 = (1+x)(1-10x+)$ = 1+x-10x+	M1
	$\approx 1 - 9x$ (*)	A1 (2) (6)

### **Notes**

2(a)	
1-10x	B1
1-10x must be seen in this simplified form in (a).	
Correct structure: 'binomial coefficients' (perhaps from Pascal's triangle), increasing powers of x.	M1
Allow slips.	
Accept other forms: ${}^5C_1$ , $\binom{5}{1}$ , also condone $\left(\frac{5}{1}\right)$ but must be attempting to use 5.	
Condone use of invisible brackets and using $2x$ instead of $-2x$ .	
Powers of x: at least 2 powers of the type $(2x)^a$ or $2x^a$ seen for $a \ge 1$ .	
$40x^2$ (1st A1)	A1
$-80x^3$ (2nd A1)	A1
Allow commas between terms. Terms may be listed rather than added	
Allow 'recovery' from invisible brackets, so $1^5 + {5 \choose 1} 1^4 - 2x + {5 \choose 2} 1^3 - 2x^2 + {5 \choose 3} 1^2 - 2x^3$	
$=1-10x+40x^2-80x^3+$ gains full marks.	
$1+5\times(2x)+\frac{5\times4}{2!}(2x)^2+\frac{5\times4\times3}{3!}(2x)^3+=1+10x+40x^2+80x^3+$ gains B0M1A1A0	
Misread: first 4 terms, descending terms: if correct, would score	
B0, M1, 1st A1: one of $40x^2$ and $-80x^3$ correct; 2nd A1: both $40x^2$ and $-80x^3$ correct.	

2(a) Long multiplication	
$(1-2x)^2 = 1-4x+4x^2$ , $(1-2x)^3 = 1-6x+12x^2-8x^3$ , $(1-2x)^4 = 1-8x+24x^2-32x^3$ {+ 16x <sup>4</sup> }	
$(1-2x)^5 = 1 - 10x + 40x^2 + 80x^3 + \dots$	
1-10x	B1
1-10x must be seen in this simplified form in (a).	
Attempt repeated multiplication up to and including $(1-2x)^5$	M1

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$40x^2$ (1st A1)	A1
$-80x^3$ (2nd A1)	A1
Misread: first 4 terms, descending terms: if correct, would score	
B0, M1, 1st A1: one of $40x^2$ and $-80x^3$ correct; 2nd A1: both $40x^2$ and $-80x^3$ correct.	

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Past Paper (Mark Scheme)

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2(b)	
Use their (a) and attempt to multiply out; terms (whether correct or incorrect) in $x^2$ or higher	M1
can be ignored.	
If their (a) is correct an attempt to multiply out can be implied from the correct answer, so	
(1+x)(1-10x) = 1-9x will gain M1 A1.	
If their (a) is correct, the 2nd bracket must contain at least $(1 - 10x)$ and an attempt to	
multiply out for the M mark. An attempt to multiply out is an attempt at 2 out of the 3	
relevant terms (N.B. the 2 terms in $x^1$ may be combined – but this will still count as 2 terms).	
If their (a) is incorrect their 2nd bracket must contain all the terms in $x^0$ and $x^1$ from their (a)	
AND an attempt to multiply all terms that produce terms in $x^0$ and $x^1$ .	
N.B. $(1+x)(1-2x)^5 = (1+x)(1-2x)$ [where $1-2x+$ is NOT the candidate's	
answer to (a)]	
=1-x	
i.e. candidate has ignored the power of 5: M0	
N.B. The candidate may start again with the binomial expansion for $(1-2x)^5$ in (b). If correct	
(only needs $1 - 10x$ ) may gain M1 A1 even if candidate did not gain B1 in part (a).	
N.B. Answer given in question.	A1

## **Example**

Answer in (a) is  $=1+10x+40x^2-80x^3+...$ 

(b) 
$$(1+x)(1+10x) = 1 + 10x + x$$
 M1  
= 1 + 11x A0

**Mathematics C2** 

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Find an equation for <i>C</i> .		
		(6)
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Question Number	Scheme	Marks
3.	Centre $\left(\frac{-1+3}{2}, \frac{6+4}{2}\right)$ , i.e. $(1, 5)$	M1, A1
	$r = \frac{\sqrt{(3 - (-1))^2 + (6 - 4)^2}}{2}$ or $r^2 = (1 - (-1))^2 + (5 - 4)^2$ or $r^2 = (3 - 1)^2 + (6 - 5)^2$ o.e.	M1
	$(x-1)^2 + (y-5)^2 = 5$	M1,A1,A1 (6)

# Notes

Some use of correct formula in <i>x</i> or <i>y</i> coordinate. Can be implied.	
Use of $\left(\frac{1}{2}(x_A - x_B), \frac{1}{2}(y_A - y_B)\right) \rightarrow (-2, -1)$ or $(2, 1)$ is M0 A0 but watch out for use of	
$x_A + \frac{1}{2}(x_A - x_B)$ etc which is okay.	
(1, 5)	A1
(5, 1) gains M1 A0.	
Correct method to find $r$ or $r^2$ using given points or f.t. from their centre. Does not need to be	M1
simplified.	
Attempting radius = $\sqrt{\frac{(\text{diameter})^2}{2}}$ is an incorrect method, so M0.	
N.B. Be careful of labelling: candidates may not use $d$ for diameter and $r$ for radius.	
Labelling should be ignored.	
Simplification may be incorrect – mark awarded for correct method.	
Use of $\sqrt{(x_1 - x_2)^2 - (y_1 - y_2)^2}$ is M0.	
Write down $(x \pm a)^2 + (y \pm b)^2 =$ any constant (a letter or a number).	M1
Numbers do not have to be substituted for <i>a</i> , <i>b</i> and if they are they can be wrong.	
LHS is $(x-1)^2 + (y-5)^2$ . Ignore RHS.	A1
RHS is 5.	A1
Ignore subsequent working. Condone use of decimals that leads to exact 5.	
Or correct equivalents, e.g. $x^2 + y^2 - 2x - 10y + 21 = 0$ .	

Alternative – note the order of the marks needed for ePEN.	
As above.	M1
As above.	A1
$x^2 + y^2 + (constant)x + (constant)y + constant = 0$ . Numbers do not have to be substituted for	3rd M1
the constants and if they are they can be wrong.	
Attempt an appropriate substitution of the coordinates of their centre (i.e. working with	2nd M1
coefficient of x and coefficient of y in equation of circle) and substitute $(-1, 4)$ or $(3, 6)$ into	
equation of circle.	
$-2x - 10y$ part of the equation $x^2 + y^2 - 2x - 10y + 21 = 0$ .	A1
$+21 = 0$ part of the equation $x^2 + y^2 - 2x - 10y + 21 = 0$ .	A1
Or correct equivalents, e.g. $(x-1)^2 + (y-5)^2 = 5$ .	

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Solve the equation	
$5^x = 17$ ,	
3 – 17,	
giving your answer to 3 significant figures.	
	(3)

(Total 3 marks)

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Question Number		Scheme	Marks
4.	$x \log 5 = \log 17$ or	$x = \log_5 17$	M1
	$x = \frac{\log 17}{\log 5}$		A1
	= 1.76		A1 (3)

Notes N.B. It is never possible to award an A mark after giving M0. If M0 is given then the marks will be M0 A0 A0.

4	
Acceptable alternatives include	1st M1
$x \log 5 = \log 17$ ; $x \log_{10} 5 = \log_{10} 17$ ; $x \log_{e} 5 = \log_{e} 17$ ; $x \ln 5 = \ln 17$ ; $x = \log_{5} 17$	
Can be implied by a correct exact expression as shown on the first A1 mark	
An exact expression for x that can be evaluated on a calculator. Acceptable alternatives include	1st A1
$x = \frac{\log 17}{\log 5}$ ; $x = \frac{\log_{10} 17}{\log_{10} 5}$ ; $x = \frac{\log_e 17}{\log_e 5}$ ; $x = \frac{\ln 17}{\ln 5}$ ; $x = \frac{\log_q 17}{\log_q 5}$ where $q$ is a number	
This may not be seen (as, for example, $\log_5 17$ can be worked out directly on many calculators) so this A mark can be implied by the correct final answer or the right answer corrected to or	
truncated to a greater accuracy than 3 significant figures or 1.8	
Alternative: $x = \frac{\text{a number}}{\text{a number}}$ where this fraction, when worked out as a decimal rounds to 1.76.	
(N.B. remember that this A mark cannot be awarded without the M mark).	
If the line for the M mark is missing but this line is seen (with or without the $x = $ ) and is <u>correct</u>	
the method can be assumed and M1 1st A1 given.	
1.76 cao	2nd A1
N.B. $\sqrt[5]{17} = 1.76$ and $x^5 = 17$ , $\therefore x = 1.76$ are both M0 A0 A0	
Answer only 1.76: full marks (M1 A1 A1)	
Answer only to a greater accuracy but which rounds to 1.76: M1 A1 A0	
(e.g. 1.760, 1.7603, 1.7604, 1.76037 etc)	
Answer only 1.8: M1 A1 A0	
Trial and improvement: award marks as for "answer only".	

Past Paper (Mark Scheme)

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Examples

4. 
$$x = \log 5^{17}$$
 M0 A0  
= 1.76 A0

Working seen, so scheme applied

4. 
$$5^{1.76} = 17$$
 M1 A1 A1  
Answer only but clear that  $x = 1.76$ 

4. 
$$5^{1.8} = 17$$
 M1 A1 A0 Answer only but clear that  $x = 1.8$ 

4. 
$$\log_5 17 = x$$
 M1  $x = 1.760$  A1 A0

4. 
$$x \log 5 = \log 17$$
 M1  
 $x = \frac{1.2304...}{0.69897...}$  A1

**A**1

4. 
$$x \log 5 = \log 17$$
 M1  
 $x = \frac{2.57890}{1.46497}$  A1  
 $x = 1.83$  A0

x = 1.76

4. 
$$5^{1.8} = 18.1, 5^{1.75} = 16.7$$
  
 $5^{1.761} = 17$  M1 A1 A0

4. 
$$x \log 5 = \log 17$$
 M1  $x = 1.8$  A1 A0

Answer only but clear that 
$$x = 1.70$$

M0 A0 A0

 $5^{1.76}$ 

4.

4. 
$$\log_5 17 = x$$
 M1  $x = 1.76$  A1 A1

4. 
$$x \ln 5 = \ln 17$$
 M1  
 $x = \frac{2.833212...}{1.609437...}$  A1  
 $x = 1.76$  A1

4. 
$$\log_{17} 5 = x \qquad M0$$

$$x = \frac{\log 5}{\log 17} \qquad A0$$

$$x = 0.568 \qquad A0$$

4. 
$$x = 5^{1.76}$$
 M0 A0 A0

4. 
$$x = \frac{\log 17}{\log 5}$$
 M1 A1  
  $x = 1.8$  A0

N.B.

4. 
$$x^5 = 17$$
 M0 A0  $x = 1.76$  A0

4. 
$$\sqrt[5]{17}$$
 M0 A0 = 1.76 A0

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5.	$f(x) = x^3 + 4x^2 + x - 6.$		
	(a) Use the factor theorem to show that $(x + 2)$ is a factor of $f(x)$ .		
		(2)	
	(b) Factorise $f(x)$ completely.	(4)	
		(4)	
	(c) Write down all the solutions to the equation		
	$x^3 + 4x^2 + x - 6 = 0.$	(1)	
		(1)	

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Question Number	Scheme	Marks
5. (a)	$f(-2) = (-2)^3 + 4(-2)^2 + (-2) - 6$ $\{ = -8 + 16 - 2 - 6 \}$	M1
(b)	$= 0, \therefore x + 2 \text{ is a factor}$ $x^3 + 4x^2 + x - 6 = (x + 2)(x^2 + 2x - 3)$	A1 (2) M1, A1
(0)	= (x+2)(x+3)(x-1)	M1, A1 M1, A1 (4)
(c)	-3, -2, 1	B1 (1) (7)

Notes Line in mark scheme in { } does not need to be seen.

5(a)	
Attempting $f(\pm 2)$ : No x s; allow invisible brackets for M mark	
Long division: M0 A0.	
= 0 and minimal conclusion (e.g. factor, hence result, QED, $\checkmark$ , $\square$ ).	A1
If result is stated first [i.e. If $x + 2$ is a factor, $f(-2) = 0$ ] conclusion is not needed.	
Invisible brackets used as brackets can get M1 A1, so	
$f(-2) = -2^3 + 4 \times -2^2 + -2 - 6$ { = -8 + 16 - 2 - 6} = 0, $\therefore x + 2$ is a factor M1 A1, but	
$f(-2) = -2^3 + 4 \times -2^2 + -2 - 6 = -8 - 16 - 2 - 6 = 0$ , $\therefore x + 2$ is a factor M1 A0	
Acceptable alternatives include: $x = -2$ is a factor, $f(-2)$ is a factor.	

5(b)	
1st M1 requires division by $(x + 2)$ to get $x^2 + ax + b$ where $a \ne 0$ and $b \ne 0$ or equivalent	M1
with division by $(x + 3)$ or $(x - 1)$ .	
$(x+2)(x^2+2x-3)$ or $(x+3)(x^2+x-2)$ or $(x-1)(x^2+5x+6)$	A1
[If long division has been done in (a), minimum seen in (b) to get first M1 A1 is to make	
some reference to their quotient $x^2 + ax + b$ .]	
Attempt to factorise their quadratic (usual rules).	M1
"Combining" all 3 factors is not required.	A1
Answer only: Correct M1 A1 M1 A1	
Answer only with one sign slip: $(x + 2)(x + 3)(x + 1)$ scores 1st M1 1st A12nd M0 2nd A0	
(x+2)(x-3)(x-1) scores 1st M0 1st A0 2nd M1 2nd A1	
Answer to (b) can be seen in (c).	

5(b) Alternative comparing coefficients	
$(x+2)(x^2+ax+b) = x^3 + (2+a)x^2 + (2a+b)x + 2b$	M1
Attempt to compare coefficients of two terms to find values of a and b	
a = 2, b = -3	A1
Or $(x+2)(ax^2+bx+c) = ax^3 + (2a+b)x^2 + (2b+c)x + 2c$	M1
Attempt to compare coefficients of three terms to find values of $a$ , $b$ and $c$ .	
a = 1, b = 2, c = -3	A1
Then apply scheme as above	

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5(b) Alternative using factor theorem	
Show $f(-3) = 0$ ; allow invisible brackets	M1
$\therefore x + 3$ is a factor	A1
Show $f(1) = 0$	M1
$\therefore x - 1$ is a factor	A1

5(c)	
[-3, -2, 1  or  (-3, 0), (-2, 0), (1, 0)  only. Do not ignore subsequent working.	B1
Ignore any working in previous parts of the question. Can be seen in (b)	

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$2\cos^2 x + 1 = 5\sin x,$	
giving each solution in terms of $\pi$ .	
	(6)

Question Number	Scheme	Marks
6.	$2(1-\sin^2 x) + 1 = 5\sin x$	M1
	$2\sin^2 x + 5\sin x - 3 = 0$ (2\sin x - 1)(\sin x + 3) = 0	
	$\sin x = \frac{1}{2}$	M1, A1
	$x = \frac{\pi}{2}, \frac{5\pi}{2}$	M1, M1,
	6, 6	A1cso (6)

## Notes

$-\sin^2 x$ .
brackets in first line if $2-2\sin^2 x$ is present (or implied) in a subsequent
$x^{2} = 1 - \sin^{2} x$ . Using $\cos^{2} x = 1 + \sin^{2} x$ is M0.
2 or 3 term quadratic in $\sin x$ up to $\sin x = \dots$
ving quadratics. Method may be factorising, formula or completing the
g for correct quadratic and $\sin x = \frac{1}{2}$ .
as a factor $\rightarrow \sin x = 3$ can be ignored.
g any angle in any range consistent with (either of) their trig. equation(s) in M1
(even if x not exact). [Generous M mark]
olving any trig. equation that comes from minimal working (however bad).
$(\tan^{-1}(\text{number}) \rightarrow \text{answer in degrees or radians correct for their equation})$
g second angle consistent with (either of) their trig. equation(s) in radians. M1
g second angle consistent with (either of) their trig. equation(s) in radians. With $0 \le x < 2\pi$ . Must involve using $\pi$ (e.g. $\pi \pm, 2\pi$ ) but can be
$0 \le x < 2\pi$ . Whast involve using $\pi$ (e.g. $\pi \pm, 2\pi$ ) but can be
same equation as they used to attempt the 3rd M mark.
consistent with the trig. equation they are using (e.g. if using $\cos^{-1}$ then
)
gles in degrees: method for finding 2nd angle equivalent to method above
attempt to change both angles to radians.
Recurring decimals are okay (instead of $\frac{1}{6}$ and $\frac{5}{6}$ ).
alues (corrected or truncated) before the final answer of $\frac{\pi}{6}, \frac{5\pi}{6}$ is
ons outside range; deduct final A mark for extra solutions in range.
$\frac{\pi}{6}$ M0, M0, A0, M1, M1 A1 Answer only $\frac{\pi}{6}$ M0, M0, A0, M1,
ons outside range; deduct final A mark for extra solutions in range. $\frac{\pi}{6}$ M0, M0, A0, M1, M1 A1 Answer only $\frac{\pi}{6}$ M0, M0, A0, M1,

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7.



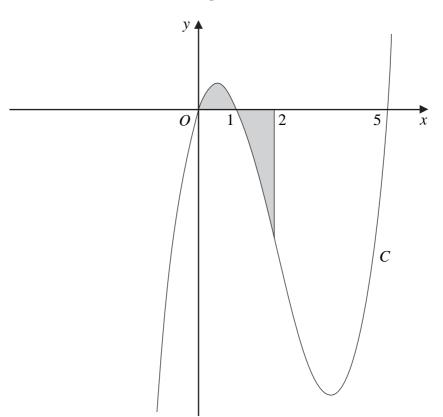


Figure 1 shows a sketch of part of the curve C with equation

$$y = x(x-1)(x-5).$$

Use calculus to find the total area of the finite region, shown shaded in Figure 1, that is between x = 0 and x = 2 and is bounded by C, the x-axis and the line x = 2.

**(9)** 

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**Mathematics C2** 6664

Question Number	Scheme	Marks
7.	$y = x(x^{2} - 6x + 5)$ $= x^{3} - 6x^{2} + 5x$ $\int (x^{3} - 6x^{2} + 5x) dx = \frac{x^{4}}{4} - \frac{6x^{3}}{3} + \frac{5x^{2}}{2}$	M1, A1 M1, A1ft
	$\int \frac{x^4}{4} - 2x^3 + \frac{5x^2}{2} \Big _0^1 = \left(\frac{1}{4} - 2 + \frac{5}{2}\right) - 0 = \frac{3}{4}$	M1
	$\left[\frac{x^4}{4} - 2x^3 + \frac{5x^2}{2}\right]_1^2 = (4 - 16 + 10) - \frac{3}{4} = -\frac{11}{4}$	M1, A1(both)
	$\therefore \text{total area} = \frac{3}{4} + \frac{11}{4}$	M1
	$=\frac{7}{2}$ o.e.	A1cso (9)

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### Notes

Attempt to multiply out, must be a cubic.	M1
Award A mark for their final version of expansion (but final version does not need to have	
like terms collected).	
Attempt to integrate; $x^n \to x^{n+1}$ . Generous mark for some use of integration, so e.g.	M1
$\int x(x-1)(x-5) dx = \frac{x^2}{2} \left(\frac{x^2}{2} - x\right) \left(\frac{x^2}{2} - 5x\right) $ would gain method mark.	
Ft on their final version of expansion provided it is in the form $ax^p + bx^q +$	A1ft
Integrand must have at least two terms and all terms must be integrated correctly.	
If they integrate twice (e.g. $\int_{0}^{1}$ and $\int_{1}^{2}$ ) and get different answers, take the better of the	
two.	
Substitutes and subtracts (either way round) for one integral. Integral must be a 'changed' function. Either 1 and 0, 2 and 1 or 2 and 0.	M1
For $\begin{bmatrix} 1 \\ 0 \end{bmatrix} = 0$ for bottom limit can be implied (provided that it is 0).	
M1 Substitutes and subtracts (either way round) for two integrals. Integral must be a	M1
'changed' function. Must have 1 and 0 and 2 and 1 (or 1 and 2).	
The two integrals do not need to be the same, but they must have come from attempts to	
integrate the same function.	
$\frac{3}{4}$ and $-\frac{11}{4}$ o.e. (if using $\int_{1}^{2} f(x)$ ) or $\frac{3}{4}$ and $\frac{11}{4}$ o.e. (if using $\int_{2}^{1} f(x) \operatorname{or} -\int_{1}^{2} f(x) \operatorname{or}$	A1
$\int_{1}^{2} -f(x)  dx \qquad \text{where } f(x) = \frac{x^4}{4} - 2x^3 + \frac{5x^2}{2}  .$	
The answer must be consistent with the integral they are using (so $\int_{1}^{2} f(x) = \frac{11}{4}$ loses this A	
and the final A).	
$-\frac{11}{4}$ may not be seen explicitly. Can be implied by a subsequent line of working.	
5th M1   their value for $\begin{bmatrix} \\ \\ \end{bmatrix}_0^1$   +   their value for $\begin{bmatrix} \\ \\ \end{bmatrix}_1^2$	M1
Dependent on at least one of the values coming from integration (other may come from	
e.g. trapezium rules).	
This can be awarded even if both values already positive.	
$\frac{7}{2}$ o.e. N.B. c.s.o.	A1 cso

Past Paper

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A diesel lorry is driven from Birmingham to Bury at a steady speed of v kilometres per hour. The total cost of the journey, £C, is given by

 $C = \frac{1400}{v} + \frac{2v}{7}$ .

(a) Find the value of v for which C is a minimum.

**(5)** 

(b) Find  $\frac{d^2C}{dv^2}$  and hence verify that C is a minimum for this value of v.

**(2)** 

(c) Calculate the minimum total cost of the journey.

**(2)** 

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**Mathematics C2** 

Question Number	Scheme	Marks
	$\frac{dC}{dv} = -1400v^{-2} + \frac{2}{7}$	M1, A1
	$-1400v^{-2} + \frac{2}{7} = 0$	M1
	$v^2 = 4900$	<b>d</b> M1
	v = 70	A1cso
		(5)
(b)	$\frac{\mathrm{d}^2 C}{\mathrm{d}v^2} = 2800v^{-3}$	M1
	$\frac{d^2C}{dv^2} = 2800v^{-3}$ $v = 70, \frac{d^2C}{dv^2} > 0 \qquad \{ \Rightarrow \text{minimum} \}$	A1ft (2)
	or $v = 70$ , $\frac{d^2C}{dv^2} = 2800 \times 70^{-3}$ $\{ = \frac{2}{245} = 0.00816 \}$ $\{ \Rightarrow \text{minimum} \}$	(2)
(c)	$v = 70, \ C = \frac{1400}{70} + \frac{2 \times 70}{7}$	M1
	C = 40	A1 (2) (9)

### Notes

8(a)	
Attempt to differentiate $v^n \to v^{n-1}$ . Must be seen and marked in part (a) not part (b).	
Must be differentiating a function of the form $av^{-1} + bv$ .	
o.e.	A1
$(-1400v^{-2} + \frac{2}{7} + c \text{ is A0})$	
Their $\frac{dC}{dv} = 0$ . Can be implied by their $\frac{dC}{dv} = P + Q \rightarrow P = \pm Q$ .	M1
Dependent on both of the previous Ms.	dM1
Attempt to rearrange their $\frac{dC}{dv}$ into the form $v^n = \text{number}$ or $v^n - \text{number} = 0$ , $n \neq 0$ .	
$v = 70$ cso but allow $v = \pm 70$ . $v = 70$ km per h also acceptable.	A1cso
Answer only is 0 out of 5.	
Method of completing the square: send to review.	

8(a) Trial and improvement $f(v) = \frac{1400}{v} + \frac{2v}{7}$	
Attempts to evaluate $f(v)$ for 3 values $a$ , $b$ , $c$ where (i) $a < 70$ , $b = 70$ and $c > 70$ or (ii) $a$ , $b < 10$	M1
70 and $c > 70$ or (iii) $a < 70$ and $b, c > 70$ .	
All 3 correct and states $v = 70$ (exact)	A1
Then 2nd M0, 3rd M0, 2nd A0.	

8(a) Graph	
Correct shape (ignore anything drawn for $v < 0$ ).	M1
v = 70 (exact)	A1
Then 2nd M0, 3rd M0, 2nd A0.	

8(b)	
Attempt to differentiate their $\frac{dC}{dv}$ ; $v^n \to v^{n-1}$ (including $v^0 \to 0$ ).	M1
$\frac{d^2C}{dv^2}$ must be correct. Ft only from their value of v and provided their value of v is +ve.	A1ft
Must be some (minimal) indication that their value of $v$ is being used.	
Statement: "When $v =$ their value of $v$ , $\frac{d^2C}{dv^2} > 0$ " is sufficient provided $2800v^{-3} > 0$ for their	
value of v.	
If substitution of their $v$ seen: correct substitution of their $v$ into $2800v^{-3}$ , but, provided evaluation is +ve, ignore incorrect evaluation.	
N.B. Parts in mark scheme in { } do not need to be seen.	

8(c)	
Substitute their value of $v$ that they think will give $C_{min}$ (independent of the method of	M1
obtaining this value of v and independent of which part of the question it comes from).	
40 or £40	A1
Must have part (a) completely correct (i.e. all 5 marks) to gain this A1.	
Answer only gains M1A1 provided part (a) is completely correct	

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Examples 8(b)

8(b) 
$$\frac{d^2C}{dv^2} = 2800v^{-3}$$
 M1

$$v = 70, \frac{d^2C}{dv^2} > 0$$
 A1

8(b) 
$$\frac{d^2C}{dv^2} = 2800v^{-3}$$
 M1  
> 0 A0 (no indication that a value of v is being used)

8(b) Answer from (a): 
$$v = 30$$

$$\frac{d^{2}C}{dv^{2}} = 2800v^{-3}$$
 M1

$$v = 30, \frac{d^2C}{dv^2} > 0$$
 A1ft

8(b) 
$$\frac{d^2C}{dv^2} = 2800v^{-3} \qquad M1$$

$$v = 70, \frac{d^2C}{dv^2} = 2800 \times 70^{-3}$$

$$= 8.16 \qquad A1 \text{ (correct substitution of 70 seen, evaluation wrong but positive)}$$

8(b) 
$$\frac{d^2C}{dv^2} = 2800v^{-3}$$
 M1
$$v = 70, \frac{d^2C}{dv^2} = 0.00408$$
 A0 (correct substitution of 70 not seen)

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9.

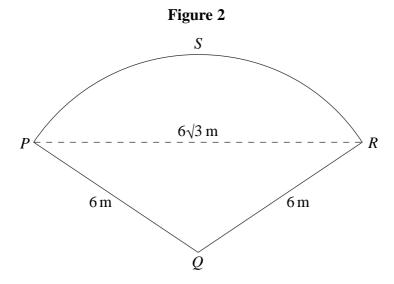


Figure 2 shows a plan of a patio. The patio PQRS is in the shape of a sector of a circle with centre Q and radius  $6 \, \text{m}$ .

Given that the length of the straight line PR is  $6\sqrt{3}$  m,

(a) find the exact size of angle PQR in radians.

(3)

(b) Show that the area of the patio PQRS is  $12\pi$  m<sup>2</sup>.

**(2)** 

(c) Find the exact area of the triangle *PQR*.

**(2)** 

(d) Find, in  $m^2$  to 1 decimal place, the area of the segment *PRS*.

**(2)** 

(e) Find, in m to 1 decimal place, the perimeter of the patio PQRS.

**(2)** 

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Question Number	Scheme	Marks
9. (a)	$\cos PQR = \frac{6^2 + 6^2 - (6\sqrt{3})^2}{2 \times 6 \times 6}  \left\{ = -\frac{1}{2} \right\}$	M1, A1
	$PQR = \frac{2\pi}{3}$	A1 (3)
(b)	Area = $\frac{1}{2} \times 6^2 \times \frac{2\pi}{3} \mathrm{m}^2$	M1
	$= 12\pi \text{ m}^2 (\clubsuit)$	A1cso (2)
(c)	Area of $\Delta = \frac{1}{2} \times 6 \times 6 \times \sin \frac{2\pi}{3} \text{ m}^2$	M1
	$= 9\sqrt{3} \text{ m}^2$	A1cso (2)
(d)	Area of segment = $12\pi - 9\sqrt{3}$ m <sup>2</sup>	M1
	$= 22.1 \text{ m}^2$	A1 (2)
(e)	Perimeter = $6+6+\left[6\times\frac{2\pi}{3}\right]$ m	M1
	= 24.6 m	A1ft (2) (11)

### Notes

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9(a) N.B. $a^2 = b^2 + c^2 - 2bc \cos A$ is in the formulae book.	
Use of cosine rule for $\cos PQR$ . Allow A, $\theta$ or other symbol for angle.	M1
(i) $(6\sqrt{3})^2 = 6^2 + 6^2 - 2.6.6\cos PQR$ : Apply usual rules for formulae: (a) formula not stated,	
must be correct, (b) correct formula stated, allow one sign slip when substituting.	
_	
or (ii) $\cos PQR = \frac{\pm 6^2 \pm 6^2 \pm (6\sqrt{3})^2}{\pm 2 \times 6 \times 6}$	
$\pm 2 \times 6 \times 6$	
Also allow invisible brackets [so allow $6\sqrt{3}^2$ ] in (i) or (ii)	
Correct expression $\frac{6^2 + 6^2 - (6\sqrt{3})^2}{2 \times 6 \times 6}$ o.e. (e.g. $-\frac{36}{72}$ or $-\frac{1}{2}$ )	A1
Correct expression ${2 \times 6 \times 6}$ o.e. (e.g. $-{72}$ or $-{2}$ )	
$\frac{2\pi}{3}$	A1
3	

Past Paper (Mark Scheme)

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9(a) Alternativ	re	
$\sin\theta = \frac{a\sqrt{3}}{6}$	where $\theta$ is any symbol and $a < 6$ .	M1
$\sin\theta = \frac{3\sqrt{3}}{6}$	where $\theta$ is any symbol.	A1
$\frac{2\pi}{3}$		A1

9(b)	
Use of $\frac{1}{2}r^2\theta$ with $r=6$ and $\theta=$ their (a). For M mark $\theta$ does not have to be exact.	
M0 if using degrees.	
$12\pi$ c.s.o. ( $\Rightarrow$ (a) correct exact or decimal value) N.B. Answer given in	A1
question	
Special case:	
Can come from an inexact value in (a)	
$PQR = 2.09 \rightarrow \text{Area} = \frac{1}{2} \times 6^2 \times 2.09 = 37.6 \text{ (or } 37.7) = 12\pi \text{ (no errors seen, assume full)}$	
values used on calculator) gets M1 A1.	
$PQR = 2.09 \rightarrow \text{Area} = \frac{1}{2} \times 6^2 \times 2.09 = 37.6 \text{ (or } 37.7) = 11.97 \pi = 12\pi \text{ gets M1 A0.}$	

9(c)	
Use of $\frac{1}{2}r^2\sin\theta$ with $r=6$ and their (a).	M1
$\theta = \cos^{-1}(\text{their }PQR)$ in degrees or radians	
Method can be implied by correct decimal provided decimal is correct (corrected or truncated	
to at least 3 decimal places).	
15.58845727	
$9\sqrt{3}$ c.s.o. Must be exact, but correct approx. followed by $9\sqrt{3}$ is okay (e.g = 15.58845	A1cso
$=9\sqrt{3}$ )	

9(c) Alternative (using $\frac{1}{2}bh$ )	
Attempt to find h using trig. or Pythagoras and use this h in $\frac{1}{2}bh$ form to find the area of	M1
triangle PQR	
$9\sqrt{3}$ c.s.o. Must be exact, but correct approx. followed by $9\sqrt{3}$ is okay (e.g = 15.58845	A1cso
$=9\sqrt{3}$ )	

9(d)	
Use of area of sector – area of $\Delta$ or use of $\frac{1}{2}r^2(\theta - \sin \theta)$ .	M1
Any value to 1 decimal place or more which rounds to 22.1	A1

9(e)	
$6 + 6 + [6 \times \text{their (a)}].$	M1
Correct for their (a) to 1 decimal place or more	A1 ft

**(3)** 

**(3)** 

■ Past Paper

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- **10.** A geometric series is  $a + ar + ar^2 + ...$ 
  - (a) Prove that the sum of the first n terms of this series is given by

$$S_n = \frac{a(1-r^n)}{1-r}.$$

(4)

(b) Find

$$\sum_{k=1}^{10} 100(2^k).$$

(c) Find the sum to infinity of the geometric series

$$\frac{5}{6} + \frac{5}{18} + \frac{5}{54} + \dots$$

(d) State the condition for an infinite geometric series with common ratio r to be convergent.

(1)



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Question Number	Scheme	Marks
10. (a)	$\{S_n = \} a + ar + \ldots + ar^{n-1}$	B1
(11)	$\{rS_n = \} ar + ar^2 + \dots + ar^n$	M1
	$(1-r)S_n = a(1-r^n)$ $S_n = \frac{a(1-r^n)}{1-r}  (*)$	dM1 A1cso (4)
(b)	$a = 200, r = 2, n = 10, S_{10} = \frac{200(1 - 2^{10})}{1 - 2}$	M1, A1
	= 204,600	A1 (3)
(c)	$a = \frac{5}{6}, \ r = \frac{1}{3}$	B1
	$S_{\infty} = \frac{a}{1-r}, \qquad S_{\infty} = \frac{\frac{5}{6}}{1-\frac{1}{3}}$	M1
	$=\frac{5}{4}$ o.e.	A1 (3)
(d)	-1 < r < 1 (or $ r  < 1$ )	B1 (1) (11)

### <u>Notes</u>

10(a)	
$S_n$ not required. The following must be seen: at least one + sign, $a$ , $ar^{n-1}$ and one other	B1
intermediate term. No extra terms (usually $ar^n$ ).	
Multiply by $r$ ; $rS_n$ not required. At least 2 of their terms on RHS correctly multiplied by $r$ .	M1
Subtract both sides: LHS must be $\pm (1 - r)S_n$ , RHS must be in the form $\pm a(1 - r^{pn+q})$ .	dM1
Only award this mark if the line for $S_n =$ or the line for $rS_n =$ contains a term of the	
form $ar^{cn+d}$	
Method mark, so may contain a slip but not awarded if last term of their $S_n$ = last term of their	
$rS_n$ .	
Completion c.s.o. N.B. Answer given in question	A1 cso

10(a)	
$S_n$ not required. The following must be seen: at least one + sign, $a$ , $ar^{n-1}$ and one other	B1
intermediate term. No extra terms (usually $ar^n$ ).	
On DIIS multiply by 1-r	M1
On RHS, multiply by $\frac{1-r}{1-r}$	
Or Multiply LHS and RHS by $(1-r)$	

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Ī	Multiply by (	$\overline{1-r}$ ) convi	ncingly (RHS) and take out factor of a.		dM1
	Method mark, so may contain a slip.				
	Completion	c.s.o.	N.B. Answer given in question		A1 cso

10(b)	
Substitute $r = 2$ with $a = 100$ or 200 and $n = 9$ or 10 into formula for $S_n$ .	M1
$\frac{200(1-2^{10})}{1-2}$ or equivalent.	A1
204,600	A1

10(b) Alternative method: adding 10 terms	
(i) Answer only: full marks. (M1 A1 A1)	
(ii) 200 + 400 + 800 + + 102,400 = 204,600 or $100(2 + 4 + 8 + + 1,024) =$	M1
204,600	
M1 for two correct terms (as above o.e.) and an indication that the sum is needed (e.g. + sign	
or the word sum).	
102,400 o.e. as final term. Can be implied by a correct final answer.	A1
204,600.	A1

10(c) N.B. $S_{\infty} = \frac{a}{1-r}$ is in the formulae book.	
$r = \frac{1}{3}$ seen or implied anywhere.	B1
Substitute $a = \frac{5}{6}$ and their <i>r</i> into $\frac{a}{1-r}$ . Usual rules about quoting formula.	M1
$\frac{5}{4}$ o.e.	A1

10(d) N.B. $S_{\infty} = \frac{a}{1-r}$ for $ r  < 1$ is in the formulae book.	
-1 < r < 1 or $ r  < 1$ In words or symbols.	B1
Take symbols if words and symbols are contradictory. Must be < not ≤.	