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Mathematics FP1

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Question

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Centre No.					Pape	er Refer	ence			Surname	Initial(s)
Candidate No.			6	6	6	7	/	0	1	Signature	

Paper Reference(s)

6667/01

Edexcel GCE

Further Pure Mathematics FP1 Advanced/Advanced Subsidiary

Tuesday 22 June 2010 – Afternoon

Time: 1 hour 30 minutes

Items included with question papers Materials required for examination Mathematical Formulae (Pink)

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer to each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 9 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

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Turn over

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(a) Show that $z^2 = -5 - 12i$. (2) Find, showing your working, (b) the value of $ z^2 $, (c) the value of $\arg(z^2)$, giving your answer in radians to 2 decimal places. (d) Show z and z^2 on a single Argand diagram. (1)		
Find, showing your working, (b) the value of $ z^2 $, (c) the value of $\arg(z^2)$, giving your answer in radians to 2 decimal places. (d) Show z and z^2 on a single Argand diagram.	(a) Show that $z^2 = -5 - 12i$.	
 (b) the value of z² , (c) the value of arg(z²), giving your answer in radians to 2 decimal places. (d) Show z and z² on a single Argand diagram. 		(2)
 (c) the value of arg(z²), giving your answer in radians to 2 decimal places. (d) Show z and z² on a single Argand diagram. 	Find, showing your working,	
 (c) the value of arg(z²), giving your answer in radians to 2 decimal places. (d) Show z and z² on a single Argand diagram. 	(b) the value of $ z^2 $,	
(d) Show z and z^2 on a single Argand diagram.		(2)
(d) Show z and z^2 on a single Argand diagram.	(c) the value of $arg(z^2)$, giving your answer in radians to 2 decimal places.	(2)
		(2)
	(d) Show z and z^2 on a single Argand diagram.	(1)

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Past Paper (Mark Scheme)

June 2010 Further Pure Mathematics FP1 6667 Mark Scheme

		1	
Question Number	Scheme	Marks	S
1.	(a) $(2-3i)(2-3i) =$ Expand and use $i^2 = -1$, getting completely correct	M1	
	expansion of 3 or 4 terms		
	Reaches $-5-12i$ after completely correct work (must see $4-9$) (*)	Alcso	(2)
	(b) $ z^2 = \sqrt{(-5)^2 + (-12)^2} = 13$ or $ z^2 = \sqrt{5^2 + 12^2} = 13$	M1 A1	(2)
	Alternative methods for part (b)		` '
	$ z^{2} = z ^{2} = 2^{2} + (-3)^{2} = 13$ Or: $ z^{2} = zz^{*} = 13$	M1 A1	(2)
	(c) $\tan \alpha = \frac{12}{5}$ (allow $-\frac{12}{5}$) or $\sin \alpha = \frac{12}{13}$ or $\cos \alpha = \frac{5}{13}$. /
	$\frac{(c) \tan \alpha - \frac{1}{5}}{5} \left(\frac{\sin \alpha - \frac{1}{13}}{5}\right) \text{ of } \sin \alpha - \frac{1}{13}$	M1	
	$arg(z^2) = -(\pi - 1.176) = -1.97$ (or 4.32) allow awrt	A1	(2)
	Alternative method for part (c) $\alpha = 2 \times \arctan\left(-\frac{3}{2}\right)$ (allow $\frac{3}{2}$) or use $\frac{\pi}{2} + \arctan\frac{5}{12}$ so $\arg(z^2) = -(\pi - 1.176) = -1.97$ (or 4.32) allow awrt		
	Both in correct quadrants. Approximate relative scale No labels needed Allow two diagrams if some indication of scale Allow points or arrows	B1 7 ma	(1) arks
	Notes: (a) M1: for $4-9-12i$ or $4-9-6i-6i$ or $4-3^2-12i$ but must have correct statement seen and see i^2 replaced by -1 maybe later A1: Printed answer. Must see $4-9$ in working. Jump from $4-6i-6i+9i^2$ to -5-12i is M0A0 (b) Method may be implied by correct answer. NB $ z^2 =169$ is M0 A0 (c) Allow $\arctan \frac{12}{5}$ for M1 or $\pm \frac{\pi}{2} \pm \arctan \frac{5}{12}$		

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2.	$\mathbf{M} = \begin{pmatrix} 2a & 3 \\ 6 & a \end{pmatrix}, \text{ where } a \text{ is a real constant.}$	
(a) Given th	hat $a = 2$, find \mathbf{M}^{-1} .	(3)
(b) Find the	e values of a for which M is singular.	(2)

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		1
Question Number	Scheme	Marks
2.	(a) $\mathbf{M} = \begin{pmatrix} 4 & 3 \\ 6 & 2 \end{pmatrix}$ Determinant: $(8-18) = -10$	B1
	$\mathbf{M}^{-1} = \frac{1}{-10} \begin{pmatrix} 2 & -3 \\ -6 & 4 \end{pmatrix} \begin{bmatrix} = \begin{pmatrix} -0.2 & 0.3 \\ 0.6 & -0.4 \end{pmatrix} \end{bmatrix}$	M1 A1 (3)
	(b) Setting $\Delta = 0$ and using $2a^2 \pm 18 = 0$ to obtain $a = .$	M1
	$a=\pm 3$	
		(2) 5 marks
	Notes: (a) B1: must be -10 M1: for correct attempt at changing elements in major diagonal and changing signs in minor diagonal. Three or four of the numbers in the matrix should be correct – eg allow one slip A1: for any form of the correct answer, with correct determinant then isw. Special case: a not replaced is B0M1A0 (b) Two correct answers, $a = \pm 3$, with no working is M1A1 Just $a = 3$ is M1A0, and also one of these answers rejected is A0. Need 3 to be simplified (not $\sqrt{9}$).	

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3.

$$f(x) = x^3 - \frac{7}{x} + 2, \quad x > 0$$

(a) Show that f(x) = 0 has a root α between 1.4 and 1.5

(2)

(b) Starting with the interval [1.4, 1.5], use interval bisection twice to find an interval of width 0.025 that contains α .

(3)

(c) Taking 1.45 as a first approximation to α , apply the Newton-Raphson procedure once to $f(x) = x^3 - \frac{7}{x} + 2$ to obtain a second approximation to α , giving your answer to 3 decimal places.

(5)

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on er	Scheme		Marks
		ate both M	
	$f(1.4) = -0.256$ (or $-\frac{32}{125}$), $f(1.5) = 0.708$ (or $\frac{17}{24}$) Ch	ange of sign, ∴root	1 (2)
	Alternative method:		
	Graphical method could earn M1 if 1.4 and 1.5 are both in	dicated	
	A1 then needs correct graph and conclusion, i.e. change of s	ign ∴root	
Ì	(b) $f(1.45) = 0.221$ or 0.2 [: root is in [1.4, 1.45]]	M	1
	f(1.425) = -0.018 or -0.019 or -0.02	M	1
	∴root is in [1.425, 1.45]	A	1cso
			(3
	(c) $f'(x) = 3x^2 + 7x^{-2}$	M	1 A1
	$f'(1.45) = 9.636$ (Special case: $f'(x) = 3x^2 + 7x^{-2} + 2$ then	n $f'(1.45) = 11.636$)	A1ft
	1.45 f(1.45) 1.45 0.221 1.427	M	1 A1cao
	$x_1 = 1.45 - \frac{f(1.45)}{f'(1.45)} = 1.45 - \frac{0.221}{9.636} = 1.427$		(5
			10 mark

(a) M1: Some attempt at two evaluations

A1: needs accuracy to 1 figure truncated or rounded and conclusion including **sign change** indicated (One figure accuracy sufficient)

(b) M1: See f(1.45) attempted and positive

M1: See f(1.425) attempted and negative

A1: is cso – any slips in numerical work are penalised here even if correct region found.

Answer may be written as $1.425 \le \alpha \le 1.45$ or $1.425 < \alpha < 1.45$ or (1.425, 1.45) must be correct way round. Between is sufficient.

There is no credit for linear interpolation. This is $M0\ M0\ A0$

Answer with no working is also M0M0A0

(c) M1: for attempt at differentiation (decrease in power) A1 is cao

Second A1may be implied by correct answer (do not need to see it)

ft is limited to special case given.

 2^{nd} M1: for attempt at Newton Raphson with their values for f(1.45) and f'(1.45).

A1: is cao and needs to be correct to 3dp

Newton Raphson used more than once – isw.

Special case: $f'(x) = 3x^2 + 7x^{-2} + 2$ then f'(1.45) = 11.636...) is M1 A0 A1ft M1 A0 This mark can also be given by implication from final answer of 1.43

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Given that $f(x) = (x+3)(x^2 + ax + b)$, where a and b are real constants,

(a) find the value of a and the value of b.

(2)

(b) Find the three roots of f(x) = 0.

(4)

(c) Find the sum of the three roots of f(x) = 0.

(1)

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Question Marks Scheme Number (a) a = -2, b = 50B1, B1 4. (2) (b) -3 is a root **B**1 Solving 3-term quadratic $x = \frac{2 \pm \sqrt{4 - 200}}{2}$ or $(x - 1)^2 - 1 + 50 = 0$ M1=1+7i, 1-7i A1, A1ft (4) (c) (-3) + (1+7i) + (1-7i) = -1B1ft (1) 7 marks Notes (a) Accept $x^2 - 2x + 50$ as evidence of values of a and b. (b) B1: -3 must be seen in part (b) M1: for solving quadratic following usual conventions A1: for a correct root (simplified as here) and A1ft: for conjugate of first answer. Accept correct answers with no working here. If answers are written down as factors then isw. Must see roots for marks. (c) ft requires the sum of two non-real conjugate roots and a real root resulting in a real number. Answers including x are B0

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5.	The parabola C has equation $y^2 = 20x$.	J Giai
	(a) Verify that the point $P(5t^2, 10t)$ is a general point on C . (1)	
	The point A on C has parameter $t = 4$. The line l passes through A and also passes through the focus of C .	
	(b) Find the gradient of <i>l</i> .	
	(4)	

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Mathematics	FP

Question Number	Scheme	Marks
5.	(a) $y^2 = (10t)^2 = 100t^2$ and $20x = 20 \times 5t^2 = 100t^2$	B1
	Alternative method: Compare with $y^2 = 4ax$ and identify $a = 5$ to give answer.	B1 (2
	(b) Point A is (80, 40) (stated or seen on diagram). May be given in part (a) Focus is $(5,0)$ (stated or seen on diagram) or $(a,0)$ with $a=5$	B1 B1
	May be given in part (a). Gradient: $\frac{40-0}{80-5} = \frac{40}{75} \left(= \frac{8}{15} \right)$	M1 A1 5 mark
	Notes:	
	(a) Allow substitution of x to obtain $y = \pm 10t$ (or just $10t$) or of y to obtain x	
	(b) M1: requires use of gradient formula correctly, for their values of x and y .	
	This mark may be implied by correct answer.	
	Differentiation is M0 A0	
	A1: Accept 0.533 or awrt	

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- **6.** Write down the 2×2 matrix that represents
 - (a) an enlargement with centre (0,0) and scale factor 8,

(1)

(b) a reflection in the *x*-axis.

(1)

Hence, or otherwise,

(c) find the matrix T that represents an enlargement with centre (0,0) and scale factor 8, followed by a reflection in the x-axis.

(2)

$$\mathbf{A} = \begin{pmatrix} 6 & 1 \\ 4 & 2 \end{pmatrix}$$
 and $\mathbf{B} = \begin{pmatrix} k & 1 \\ c & -6 \end{pmatrix}$, where k and c are constants.

(d) Find **AB**.

(3)

Given that AB represents the same transformation as T,

(e) find the value of k and the value of c.

(2)

Question	Scheme	Marks
Number 6.	$\begin{pmatrix} 8 & 0 \\ 0 & 8 \end{pmatrix}$	B1 (1)
	$ \begin{array}{c cccc} \hline (b) \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \end{array} $	B1 (1)
	(c) $\mathbf{T} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} 8 & 0 \\ 0 & 8 \end{pmatrix} = \begin{pmatrix} 8 & 0 \\ 0 & -8 \end{pmatrix}$	M1 A1 (2)
	(d) $\mathbf{AB} = \begin{pmatrix} 6 & 1 \\ 4 & 2 \end{pmatrix} \begin{pmatrix} k & 1 \\ c & -6 \end{pmatrix} = \begin{pmatrix} 6k+c & 0 \\ 4k+2c & -8 \end{pmatrix}$	M1 A1 A1 (3)
	(e) " $6k + c = 8$ " and " $4k + 2c = 0$ " Form equations and solve simultaneously	M1
	k=2 and $c=-4$	A1 (2)
		9 marks
	Alternative method for (e) M1: $AB = T \Rightarrow B = A^{-1}T = \text{ and compare elements to find } k \text{ and } c.$ Then A1 as before.	
	Notes (c) M1: Accept multiplication of their matrices either way round (this can be implied by correct answer) A1: cao (d) M1: Correct matrix multiplication method implied by one or two correct terms in correct positions. A1: for three correct terms in correct positions 2 nd A1: for all four terms correct and simplified (e) M1: follows their previous work but must give two equations from which <i>k</i> and <i>c</i> can be found and there must be attempt at solution getting to <i>k</i> = or <i>c</i> =. A1: is cao (but not cso - may follow error in position of 4 <i>k</i> + 2 <i>c</i> earlier).	

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	$f(n) = 2^n + 6^n$	
(a	Show that $f(k+1) = 6f(k) - 4(2^k)$.	
		(3)
(b	Hence, or otherwise, prove by induction that, for $n \in \mathbb{Z}^+$, $f(n)$ is divisible by 8.	(4)

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Question Number	Scheme		Marks
7.	(a) LHS = $f(k+1) = 2^{k+1} + 6^{k+1}$	OR RHS =	M1
		$= 6f(k) - 4(2^k) = 6(2^k + 6^k) - 4(2^k)$	
	$=2(2^k)+6(6^k)$	$=2(2^k)+6(6^k)$	A1
	$= 6(2^k + 6^k) - 4(2^k) = 6f(k) - 4(2^k)$	$= 2^{k+1} + 6^{k+1} = f(k+1) $ (*)	A1
			(3)
	OR $f(k+1) - 6f(k) = 2^{k+1} + 6^{k+1} - 6(2^k + 6^k)$)	M1
	$=(2-6)(2^k)=-4.2^k$, and so $f(k+1)$	$= 6f(k) - 4(2^k)$	A1, A1
	(2 0)(2) 1.2 ; and so I (N 1)	01(%) 1(2)	(3)
	(b) $n = 1$: $f(1) = 2^1 + 6^1 = 8$, which is divis	sible by 8	B1
	Either Assume $f(k)$ divisible by 8 and try	Or Assume $f(k)$ divisible by 8 and try to	M1
	to use $f(k + 1) = 6f(k) - 4(2^k)$	use $f(k + 1) - f(k)$ or $f(k + 1) + f(k)$	
		including factorising $6^k = 2^k 3^k$	
	Show $4(2^k) = 4 \times 2(2^{k-1}) = 8(2^{k-1})$ or $8(\frac{1}{2}2^k)$	$=2^32^{k-3}(1+5.3^k)$ or	A1
	Or valid statement	$=2^32^{k-3}(3+7.3^k)$ o.e.	
	Deduction that result is implied for	Deduction that result is implied for	A1cso
	n = k + 1 and so is true for positive integers by induction (may include $n = 1$ true here)	n = k + 1 and so is true for positive integers by induction (must include explanation of	(4)
	by induction (may include n = 1 true nere)	why $n = 2$ is also true here)	7 marks
	Notes		
	(a) M1: for substitution into LHS (or RHS) or		
	A1: for correct split of the two separate powers	s cao mbiguity (needs (for example) to start with one s	side of
	* *	side separately is $2(2^k) + 6(6^k)$ and conclude	
			,
	(b) B1: for substitution of $n = 1$ and stating "tappear in the concluding statement of the	rue for $n = 1$ " or "divisible by 8" or tick. (This sproof)	tatement may
		$(k+1) = 6f(k) - 4(2^k)$ or equivalent expression	that could
		deduce that 2 is a factor of 6 (see right hand sch	
	A1: Indicates each term divisible by 8 OR take		
	A1: Induction statement . Statement $n = 1$ here		
	NB: $f(k+1) - f(k) = 2^{k+1} - 2^k + 6^{k+1} - 6^k = 0$	$= 2^{\kappa} + 5.6^{\kappa}$ only is M0 A0 A0	
	(b) "Otherwise" methods	12) 265(1) 22(ck) 5(1 · 2) 45(1) · (20(2k):
	Could use: $f(k+1) = 2f(k) + 4(6^k)$ or $f(k+2) = 36f(k) - 32(6^k)$ or $f(k+2) = 4f(k) + 4(6^k)$ similar way to given expression and Left hand mark scheme is applied. Special Case: Otherwise Proof not involving induction : This can only be awarded the checking $n = 1$.		

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The rectangular hyperbola H has equation $xy = c^2$, where c is a positive constant.	
The point A on H has x -coordinate $3c$.	
(a) Write down the y-coordinate of A.	
	(1)
(b) Show that an equation of the normal to H at A is	
3y = 27x - 80c	
	(5)
The normal to H at A meets H again at the point B .	
(c) Find, in terms of c , the coordinates of B .	. .
	(5)

Question Number	Scheme			Marks
8.	(a) $\frac{c}{3}$			B1 (1)
	(b) $y = \frac{c^2}{x} \Rightarrow \frac{dy}{dx} = -c^2 x^{-2}$,			B1
	or $y + x \frac{\mathrm{d}y}{\mathrm{d}x} = 0 \Rightarrow \frac{\mathrm{d}y}{\mathrm{d}x} = -\frac{y}{x}$	or $\dot{x} = c$, $\dot{y} = -\frac{c}{t^2}$ so $\frac{dy}{dx} = -\frac{c}{t^2}$	$-\frac{1}{t^2}$	
	and at A $\frac{\mathrm{d}y}{\mathrm{d}x} = -\frac{c^2}{(3c)^2} =$	$-\frac{1}{9}$ so gradient of normal is	s 9	M1 A1
	Either $y - \frac{c}{3} = 9(x - 3c)$	or $y=9x+k$ and use	$x=3c$, $y=\frac{c}{3}$	M1
	$\Rightarrow 3y = 27x - 80c$	(*)		A1 (5)
	(c) $\frac{c^2}{x} = \frac{27x - 80c}{3}$	$\frac{c^2}{y} = \frac{3y + 80c}{27}$	$3\frac{c}{t} = 27ct - 80c$	M1
	$3c^2 = 27x^2 - 80cx$	$27c^2 = 3y^2 + 80cy$	$3c = 27ct^2 - 80ct$	A1
	(x-3c)(27x+c) = 0 so $x = 0$			M1
	$x = -\frac{c}{27} , y = -27c$	$x = -\frac{c}{27} , y = -27c$	$\left(t = -\frac{1}{27} \text{ and so }\right)$	A1, A1
			$x = -\frac{c}{27} , y = -27c$	(5) 11 marks
	Notes		_	
	(b) B1: Any valid method of	f differentiation but must get	to correct expression for $\frac{dy}{dx}$	
	M1: Substitutes values and uses negative reciprocal (needs to follow calculus) A1: 9 cao (needs to follow calculus) M1: Finds equation of line through A with any gradient (other than 0 and ∞) A1: Correct work throughout – obtaining printed answer .			
	(c) M1: Obtains equation in a A1: Writes as correct three	one variable (x, y or t) term quadratic (any equivale	ent form)	
	M1: Attempts to solve three term quadratic to obtain $x = \text{or } y = \text{or } t = A1$: x coordinate, A1: y coordinate. (cao but allow recovery following slips)			

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9. (a) Prove by induction that

$$\sum_{r=1}^{n} r^2 = \frac{1}{6} n(n+1)(2n+1)$$

(6)

Using the standard results for $\sum_{r=1}^{n} r$ and $\sum_{r=1}^{n} r^2$,

(b) show that

$$\sum_{r=1}^{n} (r+2)(r+3) = \frac{1}{3}n(n^2+an+b),$$

where a and b are integers to be found.

(5)

(c) Hence show that

$$\sum_{r=n+1}^{2n} (r+2)(r+3) = \frac{1}{3}n(7n^2 + 27n + 26)$$

(3)

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Question Number	Scheme	Marks
9.	(a) If $n = 1$, $\sum_{r=1}^{n} r^2 = 1$ and $\frac{1}{6}n(n+1)(2n+1) = \frac{1}{6} \times 1 \times 2 \times 3 = 1$, so true for $n = 1$. Assume result true for $n = k$	B1 M1
	$\sum_{r=1}^{k+1} r^2 = \frac{1}{6}k(k+1)(2k+1) + (k+1)^2$	M1
	$= \frac{1}{6}(k+1)(2k^2+7k+6) \text{ or } = \frac{1}{6}(k+2)(2k^2+5k+3) \text{ or } = \frac{1}{6}(2k+3)(k^2+3k+2)$	A1
	$= \frac{1}{6}(k+1)(k+2)(2k+3) = \frac{1}{6}(k+1)(\{k+1\}+1)(2\{k+1\}+1) \text{ or equivalent}$	dM1
	True for $n = k + 1$ if true for $n = k$, (and true for $n = 1$) so true by induction for all n .	A1cso (6)
	Alternative for (a) After first three marks B M M1 as earlier:	B1M1M1
	May state RHS = $\frac{1}{6}(k+1)(\{k+1\}+1)(2\{k+1\}+1) = \frac{1}{6}(k+1)(k+2)(2k+3)$ for third M1	dM1
	Expands to $\frac{1}{6}(k+1)(2k^2+7k+6)$ and show equal to $\sum_{r=1}^{k+1} r^2 = \frac{1}{6}k(k+1)(2k+1) + (k+1)^2$ for A1	A1
	So true for $n = k + 1$ if true for $n = k$, and true for $n = 1$, so true by induction for all n .	A1cso (6)
	(b) $\sum_{r=1}^{n} (r^2 + 5r + 6) = \sum_{r=1}^{n} r^2 + 5 \sum_{r=1}^{n} r + (\sum_{r=1}^{n} 6)$	M1
	$\frac{1}{6}n(n+1)(2n+1) + \frac{5}{2}n(n+1), +6n$	A1, B1
	$= \frac{1}{6}n[(n+1)(2n+1)+15(n+1)+36]$	M1
	$= \frac{1}{6}n[2n^2 + 18n + 52] = \frac{1}{3}n(n^2 + 9n + 26) $ or $a = 9, b = 26$	A1 (5)
	(c) $\sum_{r=n+1}^{2n} (r+2)(r+3) = \frac{1}{3} 2n(4n^2 + 18n + 26) - \frac{1}{3} n(n^2 + 9n + 26)$	M1 A1ft
	$\frac{1}{3}n(8n^2 + 36n + 52 - n^2 - 9n - 26) = \frac{1}{3}n(7n^2 + 27n + 26) \tag{*}$	A1cso (3) 14 marks
	Notes: (a) B1: Checks $n = 1$ on both sides and states true for $n = 1$ here or in conclusion M1: Assumes true for $n = k$ (should use one of these two words) M1: Adds $(k+1)$ th term to sum of k terms A1: Correct work to support proof M1: Deduces $\frac{1}{6}n(n+1)(2n+1)$ with $n = k+1$ A1: Makes induction statement. Statement true for $n = 1$ here could contribute to B1 m	ark earlier

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Past Paper (Mark Scheme)

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Mathematics FP1

Question 9 Notes continued:

(b) M1: Expands and splits (but allow 6 rather than sigma 6 for this mark)

A1: first two terms correct

B1: for 6*n*

M1: Take out factor n/6 or n/3 correctly – no errors factorising

A1: for correct factorised cubic or for identifying a and b

(c) M1: Try to use $\sum_{1}^{2n} (r+2)(r+3) - \sum_{1}^{n} (r+2)(r+3)$ with previous result used **at least once**

A1ft Two correct expressions for their a and b values

A1: Completely correct work to printed answer