

Summer 2012
6667 Further Pure FP1
Mark Scheme

Question Number	Scheme	Notes	Marks
1. (a)	$f(x) = 2x^3 - 6x^2 - 7x - 4$		
	$f(4) = \underline{128 - 96 - 28 - 4 = 0}$	$\underline{128 - 96 - 28 - 4 = 0}$	B1
	Just $2(4)^3 - 6(4)^2 - 7(4) - 4 = 0$ or $2(64) - 6(16) - 7(4) - 4 = 0$ is B0 But $2(64) - 6(16) - 7(4) - 4 = 128 - 128 = 0$ or $2(4)^3 - 6(4)^2 - 7(4) - 4 = 4 - 4 = 0$ is B1		
	There must be sufficient working to show that $f(4) = 0$		
			[1]
(b)	$f(4) = 0 \Rightarrow (x - 4)$ is a factor.		
	$f(x) = (x - 4)(2x^2 + 2x + 1)$	M1: $(2x^2 + kx + 1)$ Uses inspection or long division or compares coefficients and $(x - 4)$ (not $(x + 4)$) to obtain a quadratic factor of this form.	M1A1
		A1: $(2x^2 + 2x + 1)$ cao	
	So, $x = \frac{-2 \pm \sqrt{4 - 4(2)(1)}}{2(2)}$ $(2)\left(x^2 + x + \frac{1}{2}\right) = 0 \Rightarrow (2)\left(\left(x \pm \frac{1}{2}\right)^2 \pm k \pm \frac{1}{2}\right) k \neq 0 \Rightarrow x =$	Use of correct quadratic formula for their <u>3TQ</u> or completes the square.	M1
	Allow an attempt at factorisation provided the usual conditions are satisfied and proceeds as far as $x = ..$		
	$\Rightarrow x = \frac{-2 \pm \sqrt{-4}}{2(2)}$		
$\Rightarrow x = 4, \frac{-2 \pm 2i}{4}$	All <u>three</u> roots stated somewhere in (b). Complex roots must be at least as given but apply isw if necessary.	A1	
		[4]	
			5 marks

Question Number	Scheme	Notes	Marks	
2. (a)	$\mathbf{A} = \begin{pmatrix} 3 & 1 & 3 \\ 4 & 5 & 5 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 1 & 1 \\ 1 & 2 \\ 0 & -1 \end{pmatrix}$			
	$\mathbf{AB} = \begin{pmatrix} 3 & 1 & 3 \\ 4 & 5 & 5 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & 2 \\ 0 & -1 \end{pmatrix}$			
	$= \begin{pmatrix} 3 + 1 + 0 & 3 + 2 - 3 \\ 4 + 5 + 0 & 4 + 10 - 5 \end{pmatrix}$	A correct method to multiply out two matrices. Can be implied by two out of four correct (unsimplified) elements in a <u>dimensionally correct</u> matrix. A 2x2 matrix with a number or a calculation at each corner.	M1	
	$= \begin{pmatrix} 4 & 2 \\ 9 & 9 \end{pmatrix}$	Correct answer	A1	
	A correct answer with no working can score both marks			
			[2]	
(b)	$\mathbf{C} = \begin{pmatrix} 3 & 2 \\ 8 & 6 \end{pmatrix}, \mathbf{D} = \begin{pmatrix} 5 & 2k \\ 4 & k \end{pmatrix}, \text{ where } k \text{ is a constant,}$			
	$\mathbf{C} + \mathbf{D} = \begin{pmatrix} 3 & 2 \\ 8 & 6 \end{pmatrix} + \begin{pmatrix} 5 & 2k \\ 4 & k \end{pmatrix} = \begin{pmatrix} 8 & 2k + 2 \\ 12 & 6 + k \end{pmatrix}$	An attempt to add C to D. Can be implied by two out of four correct (unsimplified) elements in a <u>dimensionally correct</u> matrix.	M1	
	$\mathbf{E} \text{ does not have an inverse } \Rightarrow \det \mathbf{E} = 0.$			
	$8(6+k) - 12(2k + 2)$	Applies "ad - bc" to E where E is a 2x2 matrix.	M1	
	$8(6+k) - 12(2k + 2) = 0$	States or applies $\det(\mathbf{E}) = 0$ where $\det(\mathbf{E}) = ad - bc$ or $ad + bc$ only and E is a 2x2 matrix.	M1	
	Note $8(6+k) - 12(2k + 2) = 0$ or $8(6+k) = 12(2k + 2)$ could score both M's			
	$48 + 8k = 24k + 24$ $24 = 16k$			
	$k = \frac{3}{2}$		A1 oe	
			[4]	
			6 marks	

Question Number	Scheme	Notes	Marks
3.	$f(x) = x^2 + \frac{3}{4\sqrt{x}} - 3x - 7, \quad x > 0$		
	$f(x) = x^2 + \frac{3}{4}x^{-\frac{1}{2}} - 3x - 7$		
	$f'(x) = 2x - \frac{3}{8}x^{-\frac{3}{2}} - 3 \{+ 0\}$	M1: $x^n \rightarrow x^{n-1}$ on at least one term A1: Correct differentiation.	M1A1
	$f(4) = -2.625 = -\frac{21}{8} = -2\frac{5}{8}$ <p>or $4^2 + \frac{3}{4\sqrt{4}} - 3 \times 4 - 7$</p>	$f(4) = -2.625$ A correct <u>evaluation</u> of $f(4)$ or a correct <u>numerical expression</u> for $f(4)$. This can be implied by a correct answer below but in all other cases, <u>$f(4)$ must be seen explicitly evaluated</u> or as an <u>expression</u> .	B1
	$f'(4) = 4.953125 = \frac{317}{64} = 4\frac{61}{64}$	Attempt to insert $x = 4$ into their $f'(x)$. Not dependent on the first M but must be what they think is $f'(x)$.	M1
	$\alpha_2 = 4 - \left(\frac{"-2.625"}{"4.953125"} \right)$	Correct application of Newton-Raphson using their values.	M1
	$= 4.529968454... \quad \left(= \frac{1436}{317} = 4\frac{168}{317} \right)$		
	$= 4.53 \text{ (2 dp)}$	4.53 cso	A1 cao
	Note that the kind of errors that are being made in differentiating are sometimes giving 4.53 but the final mark is cso and the final A1 should not be awarded in these cases.		
	Ignore any further iterations		
	A correct derivative followed by $\alpha_2 = 4 - \frac{f(4)}{f'(4)} = 4.53$ can score full marks.		
	[6]		
	6 marks		

Question Number	Scheme	Notes	Marks	
4. (a)	$\sum_{r=1}^n (r^3 + 6r - 3)$			
		M1; An attempt to use at least one of the standard formulae correctly in summing at least 2 terms of $r^3 + 6r - 3$	M1A1B1	
	$= \frac{1}{4}n^2(n+1)^2 + 6 \cdot \frac{1}{2}n(n+1) - 3n$	<u>A1: Correct underlined expression.</u>		
		B1: $-3 \rightarrow -3n$		
	$= \frac{1}{4}n^2(n+1)^2 + 3n^2 + 3n - 3n$			
	If any marks have been lost, no further marks are available in part (a)			
	$= \frac{1}{4}n^2(n+1)^2 + 3n^2$ $= \frac{1}{4}n^2((n+1)^2 + 12)$	Cancels out the $3n$ and attempts to factorise out at least $\frac{1}{4}n$.		dM1
Provided the first 3 marks are scored, allow the next two marks for correctly showing the algebraic equivalence. E.g. showing that both				
$\frac{1}{4}n^2(n+1)^2 + 6 \cdot \frac{1}{2}n(n+1) - 3n \quad \text{and} \quad \frac{1}{4}n^2(n^2 + 2n + 13) = \frac{1}{4}n^4 + \frac{1}{2}n^3 + \frac{13}{4}n^2$				
There are no marks for proof by induction but apply the scheme if necessary.				
			[5]	
(b)	$S_n = \sum_{r=16}^{30} (r^3 + 6r - 3) = S_{30} - S_{15}$			
	$= \frac{1}{4}(30)^2(30^2 + 2(30) + 13) - \frac{1}{4}(15)^2(15^2 + 2(15) + 13)$	<u>Use of $S_{30} - S_{15}$ or $S_{30} - S_{16}$</u>	M1	
	NB They must be using $S_n = \frac{1}{4}n^2(n^2 + 2n + 13)$ not $S_n = n^3 + 6n - 3$			
	$= 218925 - 15075$			
	$= 203850$	203850	A1 cao	
	NB $S_{30} - S_{16} = 218925 - 19264 = 199661$ (Scores M1 A0)			
				[2]
			7 marks	

Question Number	Scheme	Notes	Marks
5.	$C: y^2 = 8x \Rightarrow a = \frac{8}{4} = 2$		
	(a)	$PQ = 12 \Rightarrow$ By symmetry $y_p = \frac{12}{2} = \underline{6}$	$y = \underline{6}$ B1
			[1]
(b)	$y^2 = 8x \Rightarrow 6^2 = 8x$	Substitutes their y-coordinate into $y^2 = 8x$.	M1
	$\Rightarrow x = \frac{36}{8} = \frac{9}{2}$ (So P has coordinates $(\frac{9}{2}, 6)$)	$\Rightarrow x = \frac{36}{8}$ or $\frac{9}{2}$	A1 oe
			[2]
(c)	Focus S(2, 0)	Focus has coordinates (2, 0). Seen or implied. Can score anywhere.	B1
	Gradient $PS = \frac{6-0}{\frac{9}{2}-2} \left\{ = \frac{6}{(\frac{5}{2})} = \frac{12}{5} \right\}$	Correct method for finding the gradient of the line segment PS. If no gradient formula is quoted and the gradient is incorrect, score M0 but allow this mark if there is a clear use of $\frac{y_2 - y_1}{x_2 - x_1}$ even if their coordinates are 'confused'.	M1
	Either $y - 0 = \frac{12}{5}(x - 2)$ or $y - 6 = \frac{12}{5}(x - \frac{9}{2})$; ----- or $y = \frac{12}{5}x + c$ and $0 = \frac{12}{5}(2) + c \Rightarrow c = -\frac{24}{5}$;	$y - y_1 = m(x - x_1)$ with 'their PS gradient' and their (x_1, y_1) Their PS gradient must have come from using P and S (not calculus) and they must use their P or S as (x_1, y_1). ----- or uses $y = mx + c$ with 'their gradient' in an attempt to find c. Their PS gradient must have come from using P and S (not calculus) and they must use their P or S as (x_1, y_1).	M1
	$l: \underline{12x - 5y - 24 = 0}$	$\underline{12x - 5y - 24 = 0}$	A1
	Allow any equivalent form e.g. $k(12x - 5y - 24) = 0$ where k is an integer		[4]
			7 marks

Question Number	Scheme	Notes	Marks
6.	$f(x) = \tan\left(\frac{x}{2}\right) + 3x - 6, \quad -\pi < x < \pi$		
(a)	f(1) = -2.45369751... f(2) = 1.557407725...	Attempts to evaluate both f(1) and f(2) and evaluates at least one of them correctly to awrt (or trunc.) 2 sf. Nm	M1
	Sign change (and f(x) is continuous) therefore a root α is between $x = 1$ and $x = 2$.	Both values correct to awrt (or trunc.) 2 sf, sign change (or a statement which implies this e.g. $-2.453.. < 0 < 1.5574..$) and conclusion.	A1
			[2]
(b)	$\frac{\alpha - 1}{\text{"2.45369751..."}} = \frac{2 - \alpha}{\text{"1.557407725..."}}$ or $\frac{\text{"2.45369751..." + "1.557407725"}}{1} = \frac{\text{"2.45369751..."}{\alpha - 1}$	Correct linear interpolation method. It must be a <u>correct statement</u> using their f(2) and f(1). Can be implied by working below.	M1
	If any "negative lengths" are used, score M0		
	$\alpha = 1 + \left(\frac{\text{"2.45369751..."}{\text{"1.557407725..." + "2.45369751..."}} \right) 1$ $= \frac{6.464802745}{4.011105235}$	Correct follow through expression to find α . Method can be implied here. (Can be implied by awrt 1.61.)	A1 $\sqrt{\quad}$
	= 1.611726037...	awrt 1.61	A1
			[3]
5 marks			
Special Case – Use of Degrees			
	f(1) = -2.991273132... f(2) = 0.017455064...	Attempts to evaluate both f(1) and f(2) and evaluates at least one of them correctly to awrt (or trunc.) 2 sf.	M1A0
	$\frac{\alpha - 1}{\text{"2.991273132..."}} = \frac{2 - \alpha}{\text{"0.017455064..."}}$	Correct linear interpolation method. It must be a <u>correct statement</u> using their f(2) and f(1). Can be implied by working below.	M1
If any "negative lengths" are used, score M0			
	$\alpha = 1 + \left(\frac{\text{"2.99127123..."}{\text{"0.017455064..." + "2.99127123..."}} \right) 1$	Correct follow through expression to find α . Method can be implied here. (Can be implied by awrt 1.99.)	A1 $\sqrt{\quad}$
	= 1.994198523...		A0

Question Number	Scheme	Notes	Marks
7. (a)	$\arg z = -\tan^{-1}\left(\frac{\sqrt{3}}{2}\right)$	$\tan^{-1}\left(\pm\frac{\sqrt{3}}{2}\right)$ or $\tan^{-1}\left(\pm\frac{2}{\sqrt{3}}\right)$ seen or evaluated	M1
	Awrt ± 0.71 or awrt ± 0.86 can be taken as evidence for the method mark. Or ± 40.89 or ± 49.10 if working in degrees		
	$= -0.7137243789.. = -0.71$ (2 dp)	awrt -0.71 or awrt 5.57	A1
	NB $\tan\left(\frac{\sqrt{3}}{2}\right) = 1.18$ and $\tan\left(\frac{2}{\sqrt{3}}\right) = 2.26$ and both score M0		
			[2]
(b)	$z^2 = (2 - i\sqrt{3})(2 - i\sqrt{3})$ $= 4 - 2i\sqrt{3} - 2i\sqrt{3} + 3i^2$	An attempt to multiply out the brackets to give four terms (or four terms implied).	M1
	$= 2 - i\sqrt{3} + (4 - 4i\sqrt{3} - 3)$ $= 2 - i\sqrt{3} + (1 - 4i\sqrt{3})$ $= 3 - 5i\sqrt{3}$ (Note: $a = 3, b = -5$.)	M1: An understanding that $i^2 = -1$ and an attempt to add z and put in the form $a + bi\sqrt{3}$	M1A1
		A1: $3 - 5i\sqrt{3}$	
	$z + z^2 = 2 - i\sqrt{3} + (4 - 4i\sqrt{3} + 3) = 9 - 5i\sqrt{3}$ scores MIM0A0 (No evidence of $i^2 = -1$)		
			[3]
(c)	$\frac{z+7}{z-1} = \frac{2-i\sqrt{3}+7}{2-i\sqrt{3}-1}$	Substitutes $z = 2 - i\sqrt{3}$ into both numerator and denominator.	M1
	$= \frac{(9 - i\sqrt{3})}{(1 - i\sqrt{3})} \times \frac{(1 + i\sqrt{3})}{(1 + i\sqrt{3})}$	Simplifies $\frac{z+7}{z-1}$ and multiplies by $\frac{\text{their } (1 + i\sqrt{3})}{\text{their } (1 + i\sqrt{3})}$	dM1
	$= \frac{9 + 9i\sqrt{3} - i\sqrt{3} + 3}{1 + 3}$ $= \frac{12 + 8i\sqrt{3}}{4}$	Simplifies realising that a real number is needed in the denominator and applies $i^2 = -1$ in their numerator expression and denominator expression.	M1
	$= 3 + 2i\sqrt{3}$ (Note: $c = 3, d = 2$.)	$3 + 2i\sqrt{3}$	A1
			[4]
(d)	$w = \lambda - 3i$, and $\arg(4 - 5i + 3w) = -\frac{\pi}{2}$		
	$(4 - 5i + 3w = 4 + 3\lambda - 14i)$		
	So real part of $(4 - 5i + 3w) = 0$ or $4 + 3\lambda = 0$	States real part of $(4 - 5i + 3w) = 0$ or $4 + 3\lambda = 0$	M1
	So, $\lambda = -\frac{4}{3}$	$-\frac{4}{3}$	A1
	Allow $\pm\left(\frac{14}{3\lambda+4}\right) = \pm\infty \Rightarrow 3\lambda+4=0$ M1 $\Rightarrow \lambda = -\frac{4}{3}$ A1		
			11 marks

Question Number	Scheme	Notes	Marks
8.		$xy = c^2$ at $(ct, \frac{c}{t})$.	
(a)	$y = \frac{c^2}{x} = c^2 x^{-1} \Rightarrow \frac{dy}{dx} = -c^2 x^{-2} = -\frac{c^2}{x^2}$	$\frac{dy}{dx} = k x^{-2}$	M1
	$xy = c^2 \Rightarrow x \frac{dy}{dx} + y = 0$	Correct use of product rule. The sum of two terms, one of which is correct and rhs = 0	
	$\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = -\frac{c}{t^2} \cdot \frac{1}{c}$	their $\frac{dy}{dt} \times \left(\frac{1}{\text{their } \frac{dx}{dt}} \right)$	
	$\frac{dy}{dx} = -c^2 x^{-2}$ or $x \frac{dy}{dx} + y = 0$ or $\frac{dy}{dx} = \frac{-c}{t^2} \cdot \frac{1}{c}$ or equivalent expressions	Correct differentiation	A1
	So, $m_T = \frac{dy}{dx} = -\frac{1}{t^2}$	$-\frac{1}{t^2}$	
	$y - \frac{c}{t} = -\frac{1}{t^2}(x - ct)$ ($\times t^2$)	$y - \frac{c}{t} = \text{their } m_T (x - ct)$ or $y = mx + c$ with their m_T and $(ct, \frac{c}{t})$ in an attempt to find 'c'. Their m_T must have come from calculus and should be a function of t or c or both c and t.	M1
	$x + t^2 y = 2ct$ (Allow $t^2 y + x = 2ct$)	Correct solution.	A1 *
(a) Candidates who derive $x + t^2 y = 2ct$, by stating that $m_T = -\frac{1}{t^2}$, with no justification score <u>no</u> marks in (a).			
			[4]
(b)	$y = 0 \Rightarrow x = 2ct \Rightarrow A(2ct, 0)$.	$x = 2ct$, seen or implied.	B1
	$x = 0 \Rightarrow y = \frac{2ct}{t^2} \Rightarrow B\left(0, \frac{2c}{t}\right)$.	$y = \frac{2ct}{t^2}$ or $\frac{2c}{t}$, seen or implied.	B1
	Area $OAB = 36 \Rightarrow \frac{1}{2}(2ct)\left(\frac{2c}{t}\right) = 36$	Applies $\frac{1}{2}(\text{their } x)(\text{their } y) = 36$ where x and y are functions of c or t or both (not x or y) and some attempt was made to substitute both $x = 0$ and $y = 0$ in the tangent to find A and B .	M1
	Do not allow the x and y coordinates of P to be used for the dimensions of the triangle.		
	$\Rightarrow 2c^2 = 36 \Rightarrow c^2 = 18 \Rightarrow c = 3\sqrt{2}$	$c = 3\sqrt{2}$	A1
Do not allow $c = \pm 3\sqrt{2}$			[4]
			8 marks

Question Number	Scheme	Notes	Marks
9.	$\det \mathbf{M} = 3(-5) - (4)(2) = -15 - 8 = -23$	<u>-23</u>	B1
(a)			[1]
(b)	Therefore, $\begin{pmatrix} 3 & 4 \\ 2 & -5 \end{pmatrix} \begin{pmatrix} 2a - 7 \\ a - 1 \end{pmatrix} = \begin{pmatrix} 25 \\ -14 \end{pmatrix}$	Using the information in the question to form the matrix equation. Can be implied by any of the correct equations below.	M1
	Either, $3(2a - 7) + 4(a - 1) = 25$ or $2(2a - 7) - 5(a - 1) = -14$ or $\begin{pmatrix} 3(2a - 7) + 4(a - 1) \\ 2(2a - 7) - 5(a - 1) \end{pmatrix} = \begin{pmatrix} 25 \\ -14 \end{pmatrix}$	Any one correct equation (unsimplified) inside or outside matrices	A1
	giving $a = 5$	$a = 5$	A1
			[3]
(c)	$\text{Area}(ORS) = \frac{1}{2}(6)(4); = 12 \text{ (units)}^2$	M1: $\frac{1}{2}(6)(\text{Their } a - 1)$ A1: 12 cao and cso	M1A1
	Note A(6, 0) is sometimes misinterpreted as (0, 6) – this is the wrong triangle and scores M0 e.g. $1/2 \times 6 \times 3 = 9$		
			[2]
(d)	$\text{Area}(OR'S') = \pm 23 \times (12)$	$\pm \det \mathbf{M} \times (\text{their part (c) answer})$	M1
		<u>276</u> (follow through provided area > 0)	A1 $\sqrt{}$
	A method not involving the determinant requires the coordinates of R' to be calculated ((18, 12)) and then a correct method for the area e.g. $(26 \times 25 - 7 \times 13 - 9 \times 12 - 7 \times 25)$ M1 = 276 A1		
			[2]
(e)	Rotation; 90° anti-clockwise (or 270° clockwise) about (0, 0).	B1: Rotation, Rotates, Rotate, Rotating (not turn) B1: 90° anti-clockwise (or 270° clockwise) about (around/from etc.) (0, 0)	B1;B1
			[2]
(f)	$\mathbf{M} = \mathbf{BA}$	$\mathbf{M} = \mathbf{BA}$, seen or implied.	M1
	$\mathbf{A}^{-1} = \frac{1}{(0)(0) - (1)(-1)} \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}; = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\mathbf{A}^{-1} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	A1
	$\mathbf{B} = \begin{pmatrix} 3 & 4 \\ 2 & -5 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	Applies $\mathbf{M}(\text{their } \mathbf{A}^{-1})$	M1
	$\mathbf{B} = \begin{pmatrix} -4 & 3 \\ 5 & 2 \end{pmatrix}$		A1
	NB some candidates state $\mathbf{M} = \mathbf{AB}$ and then calculate \mathbf{MA}^{-1} or state $\mathbf{M} = \mathbf{BA}$ and then calculate $\mathbf{A}^{-1}\mathbf{M}$. These could score M0A0 M1A1ft and M1A1M0A0 respectively.		[4]
			14 marks
	Special case		
(f)	$\mathbf{M} = \mathbf{AB}$	$\mathbf{M} = \mathbf{AB}$, seen or implied.	M0
		$\mathbf{A}^{-1} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	A0
	$\mathbf{B} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \begin{pmatrix} 3 & 4 \\ 2 & -5 \end{pmatrix} = \begin{pmatrix} 2 & -5 \\ -3 & -4 \end{pmatrix}$	Applies (their $\mathbf{A}^{-1})\mathbf{M}$	M1A1ft

Question Number	Scheme	Notes	Marks
10.	$f(n) = 2^{2n-1} + 3^{2n-1}$ is divisible by 5.		
	$f(1) = 2^1 + 3^1 = 5,$	Shows that $f(1) = 5.$	B1
	Assume that for $n = k,$ $f(k) = 2^{2k-1} + 3^{2k-1}$ is divisible by 5 for $k \in \mathbb{C}^+.$		
	$f(k+1) - f(k) = 2^{2(k+1)-1} + 3^{2(k+1)-1} - (2^{2k-1} + 3^{2k-1})$	M1: Attempts $f(k+1) - f(k).$ A1: Correct expression for $f(k+1)$ (Can be unsimplified)	M1A1
	$= 2^{2k+1} + 3^{2k+1} - 2^{2k-1} - 3^{2k-1}$		
	$= 2^{2k-1+2} + 3^{2k-1+2} - 2^{2k-1} - 3^{2k-1}$		
	$= 4(2^{2k-1}) + 9(3^{2k-1}) - 2^{2k-1} - 3^{2k-1}$	Achieves an expression in 2^{2k-1} and 3^{2k-1}	M1
	$= 3(2^{2k-1}) + 8(3^{2k-1})$		
	$= 3(2^{2k-1}) + 3(3^{2k-1}) + 5(3^{2k-1})$		
	$= 3f(k) + 5(3^{2k-1})$		
	$\therefore f(k+1) = 4f(k) + 5(3^{2k-1})$ or $4(2^{2k-1} + 3^{2k-1}) + 5(3^{2k-1})$	Where $f(k+1)$ is correct and is clearly a multiple of 5.	A1
	If the result is true for $n = k,$ then it is now true for $n = k+1.$ As the result has shown to be true for $n = 1,$ then the result is true for all $n.$	Correct conclusion at the end, at least as given, and all previous marks scored.	A1 cso
		[6]	
		6 marks	
All methods should complete to $f(k+1) = \dots$ where $f(k+1)$ is clearly shown to be divisible by 5 to enable the final 2 marks to be available.			
Note that there are many different ways of proving this result by induction.			