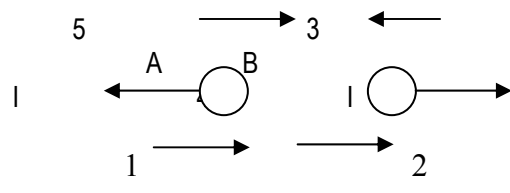


January 2008
6677 Mechanics M1
Mark Scheme

Question Number	Scheme	Marks
1(a)	<p style="text-align: center;">$I = 4(5 - 1) = \underline{16 \text{Ns}}$</p>	M1 A1 (2)
(b)	<p>CLM: $4 \times 5 - m \times 3 = 4 \times 1 + m \times 2$</p> <p style="text-align: center;">$\Rightarrow m = \underline{3.2}$</p> <p style="text-align: center;">or</p> <p style="text-align: center;">$16 = m(3 + 2)$</p> <p style="text-align: center;">$\Rightarrow m = \underline{3.2}$</p>	M1 A1 DM1 A1 (4) or M1 A1 DM1 A1 (4) 6
2(a)	<p style="text-align: center;">$27 = 0 + \frac{1}{2}a \cdot 3^2 \Rightarrow a = \underline{6}$</p>	M1 A1 (2)
(b)	<p style="text-align: center;">$v = 6 \times 3 = \underline{18 \text{ m s}^{-1}}$</p>	M1 A1 f.t. (2)
(c)	<p style="text-align: center;">From $t = 3$ to $t = 5$, $s = 18 \times 2 - \frac{1}{2} \times 9.8 \times 2^2$</p> <p style="text-align: center;">Total ht. = $s + 27 = \underline{43.4 \text{ m}, 43 \text{ m}}$</p>	M1 A1 f.t. M1 A1 (4) 8

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Question Number	Scheme	Marks
1(a)	 <p style="text-align: center;">$I = 4(5 - 1) = \underline{16 \text{ Ns}}$</p>	M1 A1 (2)
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2(a)	<p style="text-align: center;">$27 = 0 + \frac{1}{2}a \cdot 3^2 \Rightarrow a = \underline{6}$</p>	M1 A1 (2)
(b)	<p style="text-align: center;">$v = 6 \times 3 = \underline{18 \text{ m s}^{-1}}$</p>	M1 A1 f.t. (2)
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3. A car moves along a horizontal straight road, passing two points A and B . At A the speed of the car is 15 m s^{-1} . When the driver passes A , he sees a warning sign W ahead of him, 120 m away. He immediately applies the brakes and the car decelerates with uniform deceleration, reaching W with speed 5 m s^{-1} . At W , the driver sees that the road is clear. He then immediately accelerates the car with uniform acceleration for 16 s to reach a speed of $V \text{ m s}^{-1}$ ($V > 15$). He then maintains the car at a constant speed of $V \text{ m s}^{-1}$. Moving at this constant speed, the car passes B after a further 22 s .

(a) Sketch, in the space below, a speed-time graph to illustrate the motion of the car as it moves from A to B .

(3)

(b) Find the time taken for the car to move from A to B .

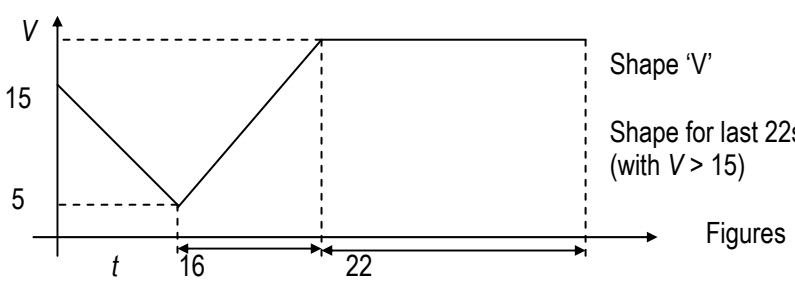
(3)

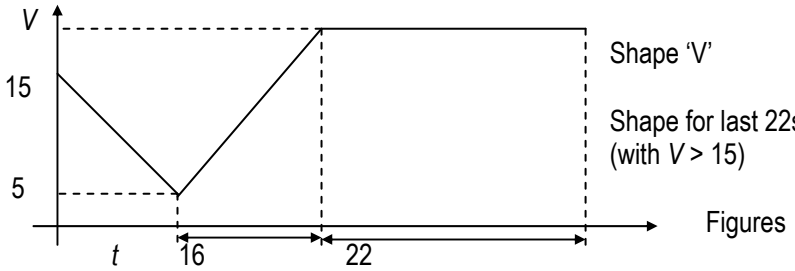
The distance from A to B is 1 km .

(c) Find the value of V .

(5)



Question Number	Scheme	Marks
<p>3.(a)</p> <p>(b)</p> <p>(c)</p>	 <p>Shape 'V'</p> <p>Shape for last 22s (with $V > 15$)</p> <p>Figures</p> <p>$\frac{1}{2}(15 + 5) \times t = 120$</p> <p>$\Rightarrow t = 12 \rightarrow T = 12 + 16 + 22 = \underline{50 \text{ s}}$</p> <p>$120 + \frac{1}{2}(V + 5) \cdot 16 + 22V = 1000$</p> <p>Solve: $30V = 840 \Rightarrow V = \underline{28}$</p>	<p>B1</p> <p>B1</p> <p>B1 (3)</p> <p>M1</p> <p>M1 A1 (3)</p> <p>M1 <u>B1</u> A1</p> <p>DM1 A1</p> <p>(5)</p> <p>11</p>
<p>4.(a)</p> <p>(b)</p> <p>(c)</p>	<p>R (// plane): $49 \cos \theta = 6g \sin 30$</p> <p>$\Rightarrow \cos \theta = 3/5 *$</p> <p>R (perp to plane): $R = 6g \cos 30 + 49 \sin \theta$</p> <p>$R \approx \underline{90.1 \text{ or } 90 \text{ N}}$</p> <p>R (// to plane): $49 \cos 30 - 6g \sin 30 = 6a$</p> <p>$\Rightarrow a \approx 2.17 \text{ or } 2.2 \text{ m s}^{-2}$</p>	<p>M1 A1</p> <p>A1 (3)</p> <p>M1 A1</p> <p>DM1 A1 (4)</p> <p>M1 A2,1,0</p> <p>A1 (4)</p> <p>11</p>

Question Number	Scheme	Marks
<p>3.(a)</p> <p>(b)</p> <p>(c)</p>	 <p>Shape 'V'</p> <p>Shape for last 22s (with $V > 15$)</p> <p>Figures</p> <p>$\frac{1}{2}(15 + 5) \times t = 120$</p> <p>$\Rightarrow t = 12 \rightarrow T = 12 + 16 + 22 = \underline{50 \text{ s}}$</p> <p>$120 + \frac{1}{2}(V + 5) \cdot 16 + 22V = 1000$</p> <p>Solve: $30V = 840 \Rightarrow V = \underline{28}$</p>	<p>B1</p> <p>B1</p> <p>B1 (3)</p> <hr/> <p>M1</p> <p>M1 A1 (3)</p> <hr/> <p>M1 B1 A1</p> <p>DM1 A1 (5)</p> <p>11</p>
<p>4.(a)</p> <p>(b)</p> <p>(c)</p>	<p>R (// plane): $49 \cos \theta = 6g \sin 30$</p> <p>$\Rightarrow \cos \theta = 3/5 *$</p> <p>R (perp to plane): $R = 6g \cos 30 + 49 \sin \theta$</p> <p>$R \approx \underline{90.1 \text{ or } 90 \text{ N}}$</p> <p>R (// to plane): $49 \cos 30 - 6g \sin 30 = 6a$</p> <p>$\Rightarrow a \approx \underline{2.17 \text{ or } 2.2 \text{ m s}^{-2}}$</p>	<p>M1 A1</p> <p>A1 (3)</p> <hr/> <p>M1 A1</p> <p>DM1 A1 (4)</p> <hr/> <p>M1 A2,1,0</p> <p>A1 (4)</p> <p>11</p>

5.

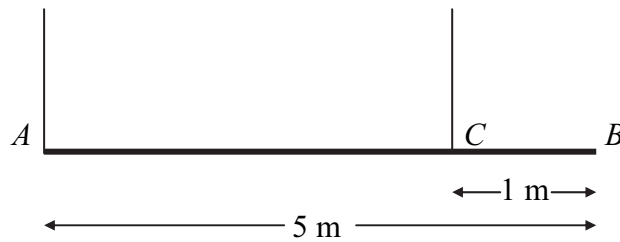


Figure 2

A beam AB has mass 12 kg and length 5 m . It is held in equilibrium in a horizontal position by two vertical ropes attached to the beam. One rope is attached to A , the other to the point C on the beam, where $BC = 1\text{ m}$, as shown in Figure 2. The beam is modelled as a uniform rod, and the ropes as light strings.

(a) Find

- (i) the tension in the rope at C ,
- (ii) the tension in the rope at A .

(5)

A small load of mass 16 kg is attached to the beam at a point which is y metres from A . The load is modelled as a particle. Given that the beam remains in equilibrium in a horizontal position,

(b) find, in terms of y , an expression for the tension in the rope at C .

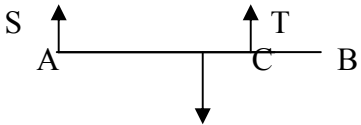
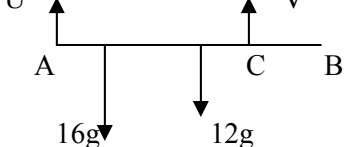
(3)

The rope at C will break if its tension exceeds 98 N . The rope at A cannot break.

(c) Find the range of possible positions on the beam where the load can be attached without the rope at C breaking.

(3)



Question Number	Scheme	Marks
5.(a)	 $M(A): T \times 4 = 12g \times 2.5$ $T = \underline{7.5g \text{ or } 73.5 \text{ N}}$ $R(\uparrow) S + T = 12g$ $\Rightarrow S = \underline{4.5g \text{ or } 44.1 \text{ N}}$	M1 A1 A1 M1 A1 (5)
(b)	 $M(A) V \times 4 = 16g \times y + 12g \times 2.5$ $V = \underline{4gy + 7.5g \text{ or } 39.2y + 73.5 \text{ N}}$	M1 A1 A1 (3)
(c)	$V \leq 98 \Rightarrow 39.2y + 73.5 \leq 98$ $\Rightarrow y \leq 0.625 = 5/8$ <p>Hence "load must be no more than 5/8 m from A" (o.e.)</p>	M1 DM1 A1 (3) 11
6.(a)	$\text{Speed} = \sqrt{5^2 + 8^2} \approx \underline{9.43 \text{ m s}^{-1}}$	M1 A1 (2)
(b)	Forming $\arctan 8/5$ or $\arctan 5/8$ oe	M1
(c)	$\text{Bearing} = 360 - \arctan 5/8 \text{ or } 270 + \arctan 8/5 = \underline{328}$	DM1 A1 (3)
(d)	$\text{At } t = 3, \text{ p.v. of } P = (7 - 15)\mathbf{i} + (-10 + 24)\mathbf{j} = -8\mathbf{i} + 14\mathbf{j}$ $\text{Hence } -8\mathbf{i} + 14\mathbf{j} + 4(u\mathbf{i} + v\mathbf{j}) = \mathbf{0}$ $\Rightarrow \underline{u = 2, v = -3.5}$	M1 A1 M1 DM1 A1 (5)
(d)	$\text{p.v. of } P \text{ } t \text{ secs after changing course} = (-8\mathbf{i} + 14\mathbf{j}) + t(2\mathbf{i} - 3.5\mathbf{j})$ $= 7\mathbf{i} + \dots$ $\text{Hence total time} = \underline{10.5 \text{ s}}$	M1 DM1 A1 (3) 13

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6. [In this question, the unit vectors **i** and **j** are due east and due north respectively.]

A particle *P* is moving with constant velocity $(-5\mathbf{i} + 8\mathbf{j}) \text{ m s}^{-1}$. Find

(a) the speed of *P*, **(2)**

(b) the direction of motion of *P*, giving your answer as a bearing. **(3)**

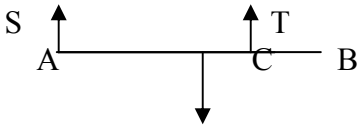
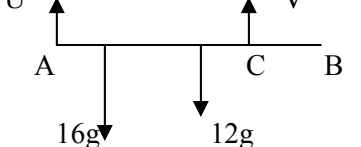
At time $t = 0$, *P* is at the point *A* with position vector $(7\mathbf{i} - 10\mathbf{j}) \text{ m}$ relative to a fixed origin *O*. When $t = 3 \text{ s}$, the velocity of *P* changes and it moves with velocity $(u\mathbf{i} + v\mathbf{j}) \text{ m s}^{-1}$, where *u* and *v* are constants. After a further 4 s, it passes through *O* and continues to move with velocity $(u\mathbf{i} + v\mathbf{j}) \text{ m s}^{-1}$.

(c) Find the values of *u* and *v*. **(5)**

(d) Find the total time taken for *P* to move from *A* to a position which is due south of *A*. **(3)**

Horizontal lines for writing answers.



Question Number	Scheme	Marks
5.(a)	 <p>M(A): $T \times 4 = 12g \times 2.5$</p> <p>$T = \underline{7.5g \text{ or } 73.5 \text{ N}}$</p> <p>R($\uparrow$) $S + T = 12g$</p> <p>$\Rightarrow S = \underline{4.5g \text{ or } 44.1 \text{ N}}$</p>	<p>M1 A1</p> <p>A1</p> <p>M1</p> <p>A1 (5)</p>
(b)	 <p>M(A) $V \times 4 = 16g \times y + 12g \times 2.5$</p> <p>$V = \underline{4gy + 7.5g \text{ or } 39.2y + 73.5 \text{ N}}$</p>	<p>M1 A1</p> <p>A1 (3)</p>
(c)	<p>$V \leq 98 \Rightarrow 39.2y + 73.5 \leq 98$</p> <p>$\Rightarrow y \leq 0.625 = 5/8$</p> <p>Hence "load must be no more than 5/8 m from A" (o.e.)</p>	<p>M1</p> <p>DM1</p> <p>A1 (3)</p> <p>11</p>
6.(a)	<p>Speed = $\sqrt{5^2 + 8^2} \approx \underline{9.43 \text{ m s}^{-1}}$</p>	<p>M1 A1 (2)</p>
(b)	<p>Forming $\arctan 8/5$ or $\arctan 5/8$ oe</p>	<p>M1</p>
(c)	<p>Bearing = $360 - \arctan 5/8$ or $270 + \arctan 8/5 = \underline{328}$</p>	<p>DM1 A1 (3)</p>
(d)	<p>At $t = 3$, p.v. of $P = (7 - 15)\mathbf{i} + (-10 + 24)\mathbf{j} = -8\mathbf{i} + 14\mathbf{j}$</p> <p>Hence $-8\mathbf{i} + 14\mathbf{j} + 4(u\mathbf{i} + v\mathbf{j}) = \mathbf{0}$</p> <p>$\Rightarrow \underline{u = 2, v = -3.5}$</p>	<p>M1 A1</p> <p>M1</p> <p>DM1 A1 (5)</p>
(d)	<p>p.v. of P t secs after changing course = $(-8\mathbf{i} + 14\mathbf{j}) + t(2\mathbf{i} - 3.5\mathbf{j})$</p> <p>$= 7\mathbf{i} + \dots$</p> <p>Hence total time = $\underline{10.5 \text{ s}}$</p>	<p>M1</p> <p>DM1</p> <p>A1 (3)</p> <p>13</p>

Question Number	Scheme	Marks
7.(a)	$B: \quad 2mg - T = 2m \times 4g/9$ $\Rightarrow T = \underline{10mg/9}$	M1 A1 A1 (3)
(b)	$A: \quad T - \mu mg = m \times 4g/9$ Sub for T and solve: $\mu = 2/3 *$	M1 B1 A1 DM1 A1 (5)
(c)	When B hits: $v^2 = 2 \times 4g/9 \times h$ Deceleration of A after B hits: $ma = \mu mg \Rightarrow a = 2g/3$ Speed of A at P : $V^2 = 8gh/9 - 2 \times 2g/3 \times h/3$ $\Rightarrow V = \frac{2}{3} \sqrt{gh}$	M1 A1 M1 A1 f.t. DM1 A1 (6)
(d)	Same tension on A and B	B1 (1) 15