

Centre No.						Paper Reference							Surname	Initial(s)
Candidate No.						6	6	7	7	/	0	1	Signature	

Paper Reference(s)

6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Wednesday 18 May 2011 – Morning

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

Materials required for examination

Mathematical Formulae (Pink)

Items included with question papers

Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer to each question in the space following the question.

Whenever a numerical value of g is required, take $g = 9.8 \text{ m s}^{-2}$.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet ‘Mathematical Formulae and Statistical Tables’ is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 7 questions in this question paper. The total mark for this paper is 75.

There are 24 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.

You should show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

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1. At time $t = 0$ a ball is projected vertically upwards from a point O and rises to a maximum height of 40 m above O . The ball is modelled as a particle moving freely under gravity.

(a) Show that the speed of projection is 28 m s^{-1} .

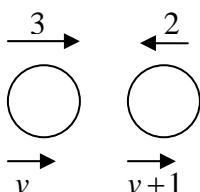
(3)

(b) Find the times, in seconds, when the ball is 33.6 m above O .

(5)



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Mark Scheme

Question Number	Scheme	Marks
1.		
(a)	$0^2 = u^2 - 2 \times 9.8 \times 40$ $u = 28 \text{ m s}^{-1}$ ** GIVEN ANSWER	M1 A1 A1 (3)
(b)	$33.6 = 28t - \frac{1}{2}9.8t^2$ $4.9t^2 - 28t + 33.6 = 0$ $t = \frac{28 \pm \sqrt{28^2 - 4 \times 4.9 \times 33.6}}{9.8}$ $= 4 \text{ s or } (1.7 \text{ s or } 1.71 \text{ s})$	M1 A1 M1 A1 A1 (5) 8
2.		
(a)	 <p>CLM: $3 \times 3 - 2 \times 2 = 3v + 2(v+1)$ $v_P = 0.6 \text{ m s}^{-1}; v_Q = 1.6 \text{ m s}^{-1}$</p>	M1 A1 M1A1 (A1 ft) (5)
(b)	$3(v-3) \quad \text{OR} \quad 2(v+1-2)$ $= 7.2 \text{ N s} \quad \quad = 7.2 \text{ N s}$	M1 A1 ft A1 (3) 8

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2. Particle P has mass 3 kg and particle Q has mass 2 kg. The particles are moving in opposite directions on a smooth horizontal plane when they collide directly. Immediately before the collision, P has speed 3 m s^{-1} and Q has speed 2 m s^{-1} . Immediately after the collision, both particles move in the same direction and the difference in their speeds is 1 m s^{-1} .

(a) Find the speed of each particle after the collision.

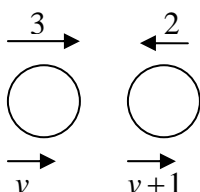
(5)

(b) Find the magnitude of the impulse exerted on P by Q .

(3)



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Mark Scheme

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2.		
(a)	 <p>CLM: $3 \times 3 - 2 \times 2 = 3v + 2(v+1)$ $v_P = 0.6 \text{ m s}^{-1}; v_Q = 1.6 \text{ m s}^{-1}$</p>	M1 A1 M1A1 (A1 ft) (5)
(b)	$3(v-3) \quad \text{OR} \quad 2(v+1-2)$ $= 7.2 \text{ Ns} \quad \quad = 7.2 \text{ Ns}$	M1 A1 ft A1 (3) 8

3.

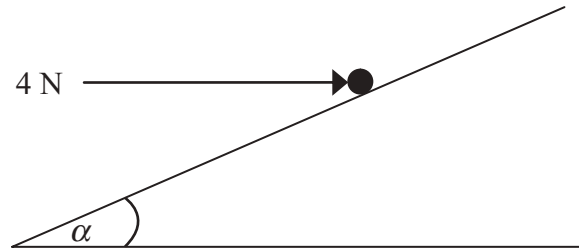


Figure 1

A particle of weight W newtons is held in equilibrium on a rough inclined plane by a horizontal force of magnitude 4 N. The force acts in a vertical plane containing a line of greatest slope of the inclined plane. The plane is inclined to the horizontal at an angle α , where $\tan \alpha = \frac{3}{4}$, as shown in Figure 1.

The coefficient of friction between the particle and the plane is $\frac{1}{2}$.

Given that the particle is on the point of sliding down the plane,

- (i) show that the magnitude of the normal reaction between the particle and the plane is 20 N,
- (ii) find the value of W .

(9)

Question Number	Scheme	Marks
3.	$\begin{aligned} &\nearrow 4\cos\alpha + F = W\sin\alpha \\ &\nwarrow R = 4\sin\alpha + W\cos\alpha \\ &F = 0.5R \\ &\cos\alpha = 0.8 \quad \text{or} \quad \sin\alpha = 0.6 \\ &R = 20\text{N} \quad ** \quad \text{GIVEN ANSWER} \\ &W = 22\text{N} \end{aligned}$	M1 A1 M1 A1 B1 B1 M1 A1 A1 (9)
<u>OR</u>	$\begin{aligned} &\rightarrow R\sin\alpha = 4 + F\cos\alpha \\ &\uparrow R\cos\alpha + F\sin\alpha = W \\ &F = 0.5R \\ &\cos\alpha = 0.8 \quad \text{or} \quad \sin\alpha = 0.6 \\ &R = 20\text{N} \quad ** \quad \text{GIVEN ANSWER} \\ &W = 22\text{N} \end{aligned}$	M1 A1 M1 A1 B1 B1 M1 A1 A1 (9)
4.		9
(a)		B1 shape B1 figs (2)
(b)	$\left(\frac{1}{2} \times 4 \times 5\right) + 60 \times 5$ $= 310$	M1 A1 A1 (3)
(c)	$\frac{(5+V)}{2} \times 20 = (400-310)$ $V = 4$	M1 A2 ft DM1 A1 (5)
(d)	$\frac{5-4}{20} = 0.05 \text{ ms}^{-2}$	M1 A1 (2)
		12

4. A girl runs a 400 m race in a time of 84 s. In a model of this race, it is assumed that, starting from rest, she moves with constant acceleration for 4 s, reaching a speed of 5 m s^{-1} . She maintains this speed for 60 s and then moves with constant deceleration for 20 s, crossing the finishing line with a speed of $V \text{ m s}^{-1}$.
- (a) Sketch, in the space below, a speed-time graph for the motion of the girl during the whole race. (2)
- (b) Find the distance run by the girl in the first 64 s of the race. (3)
- (c) Find the value of V . (5)
- (d) Find the deceleration of the girl in the final 20 s of her race. (2)



Question Number	Scheme	Marks
3.	$\begin{aligned} &\nearrow 4\cos\alpha + F = W\sin\alpha \\ &\nwarrow R = 4\sin\alpha + W\cos\alpha \\ &F = 0.5R \\ &\cos\alpha = 0.8 \quad \text{or} \quad \sin\alpha = 0.6 \\ &R = 20\text{N} \quad ** \quad \text{GIVEN ANSWER} \\ &W = 22\text{N} \end{aligned}$	M1 A1 M1 A1 B1 B1 M1 A1 A1 (9)
<u>OR</u>	$\begin{aligned} &\rightarrow R\sin\alpha = 4 + F\cos\alpha \\ &\uparrow R\cos\alpha + F\sin\alpha = W \\ &F = 0.5R \\ &\cos\alpha = 0.8 \quad \text{or} \quad \sin\alpha = 0.6 \\ &R = 20\text{N} \quad ** \quad \text{GIVEN ANSWER} \\ &W = 22\text{N} \end{aligned}$	M1 A1 M1 A1 B1 B1 M1 A1 A1 (9)
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(a)		B1 shape B1 figs (2)
(b)	$\left(\frac{1}{2} \times 4 \times 5\right) + 60 \times 5$ $= 310$	M1 A1 A1 (3)
(c)	$\frac{(5+V)}{2} \times 20 = (400-310)$ $V = 4$	M1 A2 ft DM1 A1 (5)
(d)	$\frac{5-4}{20} = 0.05 \text{ ms}^{-2}$	M1 A1 (2)
		12

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Question Number	Scheme	Marks
5.		
(a)		
(i)	EITHER $M(R), 8X + 2X = 40g \times 6 + 20g \times 4$ solving for X , $X = 32g = 314$ or 310 N	M1 A2 M1 A1
(ii)	(\uparrow) $X + X = 40g + 20g + Mg$ (or another moments equation) solving for M , $M = 4$	M1 A2 M1 A1
(i)	OR $M(P), 6X = 40g \times 2 + 20g \times 4 + Mg \times 8$ solving for X , $X = 32g = 314$ or 310 N	M1 A2 M1 A1
(ii)	(\uparrow) $X + X = 40g + 20g + Mg$ (or another moments equation) solving for M , $M = 4$	M1 A2 M1 A1
		(10)
(b)	Masses concentrated at a point or weights act at a point	B1 (1)
		11
6.		
(a)	$R = 0.3g \cos \alpha$ $= 0.24g = 2.35$ (3sf) $= 2.4$ (2sf)	M1 A1 (2)
(b)	$mg - T = 1.4m$ $T - 0.3g \sin \alpha - F = 0.3 \times 1.4$ $F = 0.5R$ Eliminating R and T $m = 0.4$	M1 A1 M1 A2 M1 DM1 A1 (8)
(c)	$v = 1.4 \times 0.5$ $-0.3g \sin \alpha - F = 0.3a$ $a = -9.8$ $0 = 0.7 - 9.8t$ $t = 0.071$ s or 0.0714 s (1/14 A0)	B1 M1 A1 A1 M1 A1 (6)
		16

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A diagram showing a mechanical system. A pulley is at the top left. A vertical rope passes over the pulley, with a weight Q hanging from the left end. The right end of the rope is attached to a block P on an inclined plane. The inclined plane makes an angle α with the horizontal. A right-angle symbol is shown at the base of the inclined plane, indicating it is perpendicular to the vertical rope.

Figure 2

The string lies in a vertical plane through a line of greatest slope of the inclined plane. The particle P is held at rest on the inclined plane and the particle Q hangs freely below the pulley with the string taut, as shown in Figure 2.

The system is released from rest and Q accelerates vertically downwards at 1.4 m s^{-2} . Find

- (a) the magnitude of the normal reaction of the inclined plane on P ,
(2)
- (b) the value of m .
(8)

When the particles have been moving for 0.5 s, the string breaks. Assuming that P does not reach the pulley,

- (c) find the further time that elapses until P comes to instantaneous rest. (6)

[illegible]

Question Number	Scheme	Marks
5.		
(a)		
(i)	EITHER $M(R), 8X + 2X = 40g \times 6 + 20g \times 4$ solving for X , $X = 32g = 314$ or 310 N	M1 A2 M1 A1
(ii)	(↑) $X + X = 40g + 20g + Mg$ (or another moments equation) solving for M , $M = 4$	M1 A2 M1 A1
(i)	OR $M(P), 6X = 40g \times 2 + 20g \times 4 + Mg \times 8$ solving for X , $X = 32g = 314$ or 310 N	M1 A2 M1 A1
(ii)	(↑) $X + X = 40g + 20g + Mg$ (or another moments equation) solving for M , $M = 4$	M1 A2 M1 A1
		(10)
(b)	Masses concentrated at a point or weights act at a point	B1 (1)
		11
6.		
(a)	$R = 0.3g \cos \alpha$ $= 0.24g = 2.35$ (3sf) $= 2.4$ (2sf)	M1 A1 (2)
(b)	$mg - T = 1.4m$ $T - 0.3g \sin \alpha - F = 0.3 \times 1.4$ $F = 0.5R$ Eliminating R and T $m = 0.4$	M1 A1 M1 A2 M1 DM1 A1 (8)
(c)	$v = 1.4 \times 0.5$ $-0.3g \sin \alpha - F = 0.3a$ $a = -9.8$ $0 = 0.7 - 9.8t$ $t = 0.071$ s or 0.0714 s (1/14 A0)	B1 M1 A1 A1 M1 A1 (6)
		16

7. [In this question \mathbf{i} and \mathbf{j} are unit vectors due east and due north respectively. Position vectors are given relative to a fixed origin O .]

Two ships P and Q are moving with constant velocities. Ship P moves with velocity $(2\mathbf{i} - 3\mathbf{j}) \text{ km h}^{-1}$ and ship Q moves with velocity $(3\mathbf{i} + 4\mathbf{j}) \text{ km h}^{-1}$.

- (a) Find, to the nearest degree, the bearing on which Q is moving. (2)

At 2 pm, ship P is at the point with position vector $(\mathbf{i} + \mathbf{j})$ km and ship Q is at the point with position vector $(-2\mathbf{j})$ km.

At time t hours after 2 pm, the position vector of P is \mathbf{p} km and the position vector of Q is \mathbf{q} km.

- (b) Write down expressions, in terms of t , for

- (i) \mathbf{p} ,

- (ii) \mathbf{q} ,

- (iii) \overrightarrow{PQ} .

(5)

- (c) Find the time when

- (i) Q is due north of P ,

- (ii) Q is north-west of P .

(4)



Question Number	Scheme	Marks
7.		
(a)	$\tan \theta = \frac{3}{4}$; bearing is 37° (nearest degree)	M1; A1 (2)
(b)		
(i)	$\mathbf{p} = (\mathbf{i} + \mathbf{j}) + t(2\mathbf{i} - 3\mathbf{j})$	M1 A1
(ii)	$\mathbf{q} = (-2\mathbf{j}) + t(3\mathbf{i} + 4\mathbf{j})$	A1
(iii)	$\mathbf{PQ} = \mathbf{q} - \mathbf{p} = (-\mathbf{i} - 3\mathbf{j}) + t(\mathbf{i} + 7\mathbf{j})$	M1 A1 (5)
(c)		
(i)	$-1 + t = 0$ $t = 1$ or 3pm	M1 A1
(ii)	$-1 + t = -(-3 + 7t)$ $t = \frac{1}{2}$ or 2.30 pm	M1 A1 (4) 11