Summer 2015 www.mystudybro.com Mathematics M1 This resource was created and owned by Pearson Edexcel Past Paper 6677 Surname Initial(s) Centre Paper Reference No. Signature Candidate 6 6 () No. Paper Reference(s) 6677/01 Examiner's use only **Edexcel GCE** Team Leader's use only **Mechanics M1 Advanced/Advanced Subsidiary** Ouestion Leave Number Blank Wednesday 3 June 2015 – Morning 1 Time: 1 hour 30 minutes 2 3 4 Materials required for examination Items included with question papers 5 Mathematical Formulae (Pink) Nil 6 Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic 7 algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them. 8 **Instructions to Candidates** In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper. Answer ALL the questions. You must write your answer to each question in the space following the question. Whenever a numerical value of g is required, take g = 9.8 m s⁻² and give your answer to either two significant figures or three significant figures. When a calculator is used, the answer should be given to an appropriate degree of accuracy. **Information for Candidates** A booklet 'Mathematical Formulae and Statistical Tables' is provided. Full marks may be obtained for answers to ALL questions. The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2). There are 8 questions in this question paper. The total mark for this paper is 75. There are 28 pages in this question paper. Any blank pages are indicated. **Advice to Candidates** You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

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Total

Turn over

· ·	·	
1.	Particle P of mass m and particle Q of mass km are moving in opposite directions on a	Leave blank
	smooth horizontal plane when they collide directly. Immediately before the collision the speed of P is $5u$ and the speed of Q is u . Immediately after the collision the speed of each particle is halved and the direction of motion of each particle is reversed.	
	Find	
	(a) the value of k , (3)	
	(b) the magnitude of the impulse exerted on P by Q in the collision. (3)	
	(3)	

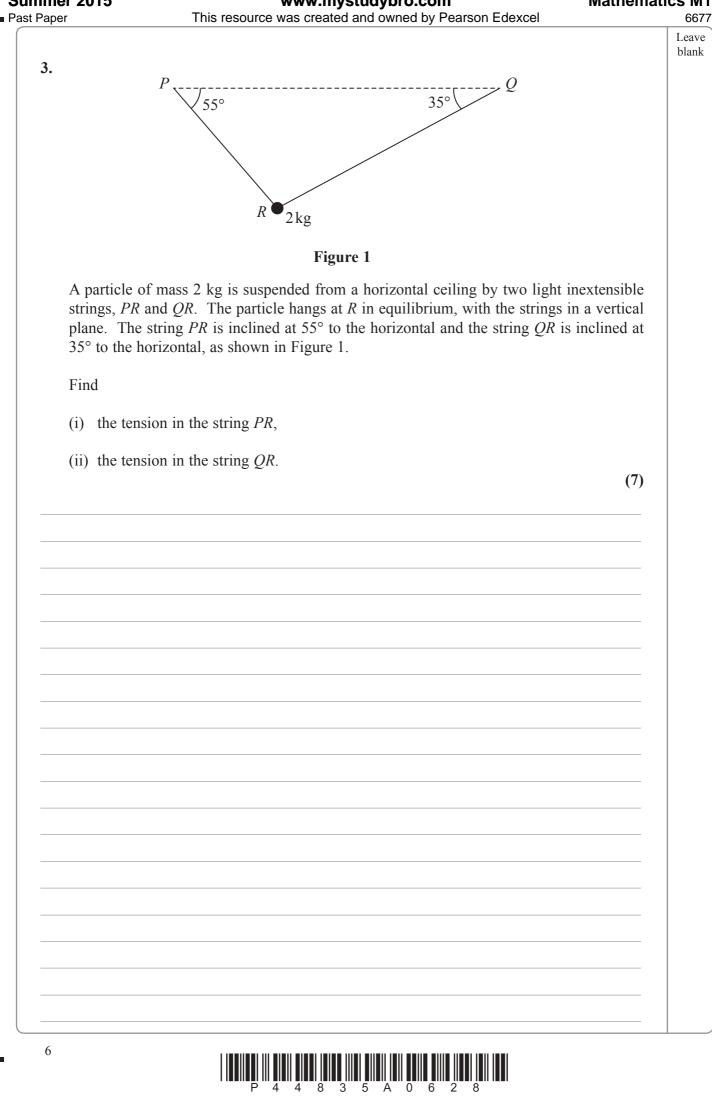
Question	Cahama	Marilia	
Question Number	Scheme	Marks	5
1(a)	$m.5u - kmu = -\frac{m.5u}{2} + \frac{km.u}{2}$	M1 A1	
	k = 5	A1 (3)	
(b)	For $P: I = m\left(\frac{5u}{2} - 5u\right)$ OR For $Q: I = km\left(\frac{u}{2}u\right)$	M1 A1	
	$=\frac{15mu}{2} = \frac{15mu}{2}$	A1	(3)
	$=\frac{1}{2}$ $=\frac{1}{2}$		
	Notes		6
1(a)	M1 for attempt at CLM equation, with correct no. of terms,		
	dimensionally correct. Allow consistent extra g's and cancelled m 's		
	and <i>u</i> 's and sign errors.		
	First A1 for a correct equation with or without <i>m</i> 's and <i>u</i> 's		
	Second A1 for $k = 5$		
	N.B. They may find the impulse on each particle and then equate the		
	impulses to produce an equation. Apply the scheme to this equation.		
1(b)	M1 for attempt at impulse = difference in momenta, for either particle, (must be considering <i>one</i> particle) (M0 if g's are included or if		
	<i>m</i> or <i>u</i> omitted) Allow $\pm m(\frac{5}{2}u - 5u)$ or $\pm km(\frac{1}{2}u - u)$.		
	First A1 for $\pm m(\frac{5}{2}u - 5u)$ or $\pm km(\frac{1}{2}u - u)$		
	A1 for 7.5 <i>mu</i> oe cao (-7.5 <i>mu</i> is A0) Allow change of sign at end to obtain magnitude		

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A small stone is projected vertically upwards from a point O with a speed of 19.6r	$m s^{-1}$.
Modelling the stone as a particle moving freely under gravity,	
(a) find the greatest height above <i>O</i> reached by the stone,	
	(2)
(b) find the length of time for which the stone is more than 14.7 m above O .	(5)
	(3)

Question Number	Scheme	Marks	S
2(a)	$0^2 = 19.6^2 - 2 \times gH$	M1	
	$H = 19.6 \mathrm{m} (20)$	A1	(2)
(b)	$14.7 = 19.6t - \frac{1}{2}gt^2$	M1 A1	
	$t^2 - 4t + 3 = 0$		
	(t-1)(t-3) = 0	DM 1	
	t = 1 or 3; Answer 2 s	A1; A1	(5)
	i = 1 of 5 , Thiswel 2.5	711,711	
2(b)	(their <i>h</i> - 14.7) = $\frac{1}{2}$ g t^2 OR $v^2 = 19.6^2 - 2g x 14.7 \Rightarrow v = (\pm) 9.8$	M1 A1	7
2(0)	$\begin{array}{c} (\text{unen } n = 14.7) = 72 \text{ g } t \\ t = 1 \end{array} \qquad \qquad$	A1	
ALT 1	Total = 2×10^{-2} x their 1	DM 1	
2(b)	$= 2 s$ $v^2 = 19.6^2 - 2g x 14.7$	A1 M1	
	$v = \pm 9.8$	A1	
	EITHER: $-9.8 = 9.8 - gT$	DM 1 A1	
ALT 2/3	T=2	A1	
	OR: $0 = 9.8t - \frac{1}{2} g t^2$	DM 1 A1	
	t = (0) or 2	Al	
2 (a)	Notes		
2(a)	M1 is for a complete method (which could involve use of two <i>suvat</i>		
	equations) for finding <i>H</i> i.e. for an equation in <i>H</i> only, condone sign errors		
	A1 for 19.6 or 20 <u>correctly obtained</u> (2g is A0)		
	(18 101 19:0 01 20 <u>contenty counter</u> (18 10 110)		
2(b)	First M1 is for a quadratic equation in <i>t</i> only (where <i>t</i> is time at 14.7		
	above O)		
	First A1 for a correct equation		
	Second DM1, dependent on first M1, for solving for t Second A1 for <u>both</u> values of t , 1 and 3.		
	N.B. If answer(s) are wrong or have come from an incorrect quadratic,		
	and the quadratic formula has been used, M1 can only be awarded if		
	there is clear evidence that the correct formula has been used. If their		
	expression is not correct for their quadratic, allow a slip but only if we		
	see an attempt to substitute into a stated correct formula.		
	Third A1 for 2 s N.P. Obtaining $t = 1$ at $a = 14.7$ (above O) only, can score may M1.A1		
	N.B. Obtaining $t = 1$ at $s = 14.7$ (above <i>O</i>) only, can score max M1 A1		

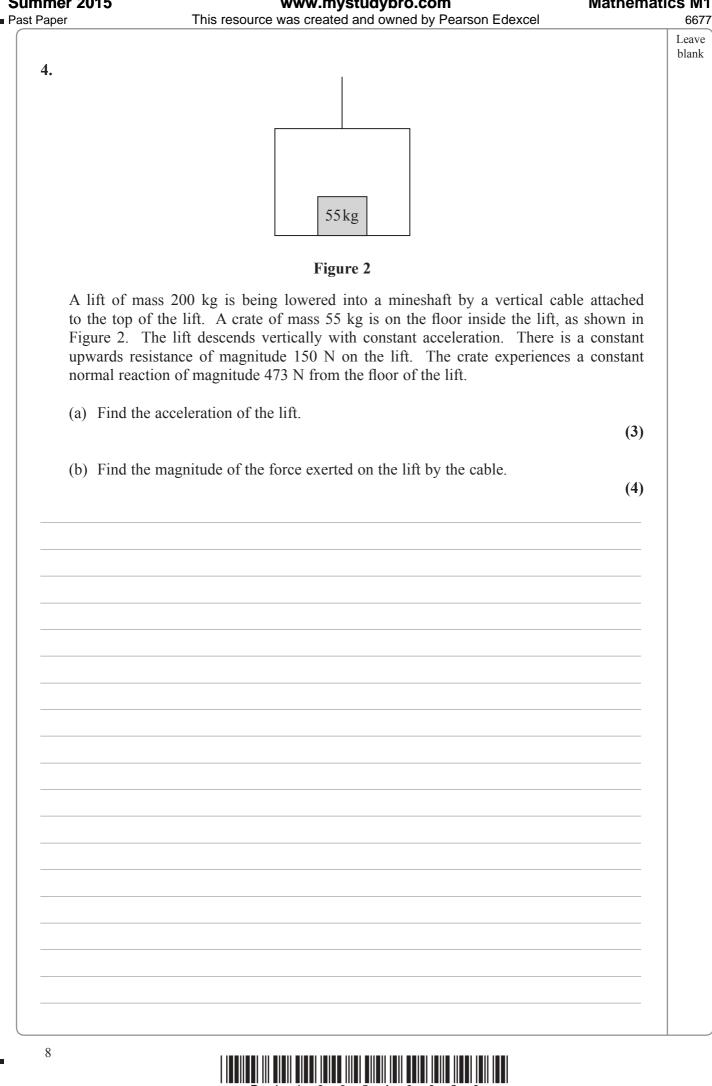




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Question Number	Scheme	Marks
3	$T_P \cos 55 = T_O \cos 35$	M1 A1
	$T_P \sin 55 + T_O \sin 35 = 2g$	M1 A1
	Eliminating T_P or T_O	M1
	$T_p = 16$ N or 16.1N; $T_Q = 11$ N or 11.2N	A1 A1
ALT 1	$(A \log RR) T = 2 \cos 25^{\circ} = 16 N \text{ or } 16 1 N$	M1 M1 A1 A1
	$\left(\text{Along } RP\right) T_p = 2g\cos 35^\circ = 16\text{N or } 16.1\text{N}$	
	$ (Along RQ) T_Q = 2g\cos 55^\circ = 11N \text{ or } 11.2N $ Notes	M1 A1 A1
ALT 1	First M1 for resolving horizontally with correct no. of terms and both T_P and T_Q terms resolved. (M0 if they assume $T_P = T_Q$) First A1 for a correct equation. Second M1 for resolving vertically with correct no. of terms and both T_P and T_Q terms resolved. (M0 if they assume $T_P = T_Q$) Second A1 for a correct equation. Third M1 (independent) for eliminating either T_P or T_Q <u>Third</u> A1 for $T_P = 16$ (N) or 16.1 (N) <u>Fourth</u> A1 for $T_Q = 11$ (N) or 11.2 (N) N.B. If both are given to more than 3SF, deduct the third A1. <u>Alternative 1 (resolving along each string)</u> First M2 for resolving along one of the strings (e.g. $T_P = 2gcos35^\circ$) First A1 for a correct equation ($T_P = 2gsin35^\circ$ scores M2A0A0) <u>Third</u> A1 for $T_P = 16$ (N) or 16.1 (N) Third M1 for resolving along the other string (e.g. $T_Q = 2gcos55^\circ$) Second A1 for a correct equation ($T_Q = 2gsin55^\circ$ scores M1A0A0) <u>Fourth</u> A1 for $T_Q = 11$ (N) or 11.2 (N)	
ALT 2	Alternative 2 (using a Triangle of Forces)Both of the equations in Alternative 1 could come from using sohcahtoa or The Sine Rule on a triangle of forces, so mark in the same way.Note that, in either case, once they have found either T_P or T_Q , they could then use $T_P = T_Q \tan 55^\circ$ or $T_Q = T_P \tan 55^\circ$ to find the other one.(Note that both of these are equivalent to the horizontal resolution) or Pythagoras.e.g. $T_P = 2g\cos 35^\circ$ M2 First A1 Third A1 $T_Q = T_P \tan 35^\circ$ or $\sqrt{\{(2g)^2 - (T_P)^2\}}$ M1 Second A1 Fourth A1	

	y using The Sine Rule but have say 35°, 55° and Il 3 M marks would be available and at most 1 A	
$T \sin 80$	2 A0A0 1 SecondA1 A0	

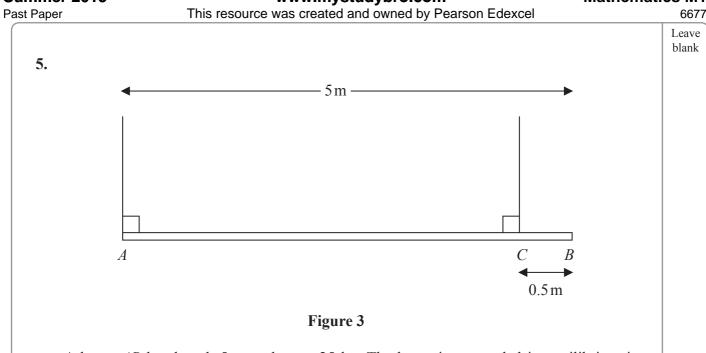


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Question Number	Scheme	Mai	rks
4 (a)	For crate, $55g - 473 = 55a$	M1 A1	
	$a = 1.2 \text{m s}^{-2}$	A1	(3)
(b)	For system, $55g + 200g \pm T - 150 = 255a$	M1 A2	
	M agnitude $= 2040$ N or 2000 N	A1	
	OR		
	For lift, $200g + 473 - 150 \pm T = 200a$	M1 A2	
	M agnitude = 2040 N or 2000 N	A1	(4)
			7
	Notes		
4 (a)	M1 for an equation in <i>a</i> only, with usual rules.		
	First A1 for a correct equation		
	Second A1 for 1.2 (m s ⁻²). Allow $- 1.2$ (m s ⁻²) if appropriate		
4(b)	M1 for an equation, in <i>T</i> and <i>a</i> , for the system or the lift only, with usual rules. (<i>a</i> does not need to be a numerical value) A2 (-1 each error) for a correct equation (Allow $\pm T$). We do not need to see a numerical value for <i>a</i> . Third A1 for 2040 (N) or 2000 (N) N.B. In both parts of this question use the mass which is being used to guide you as to which part of the system is being considered.		



A beam AB has length 5 m and mass 25 kg. The beam is suspended in equilibrium in a horizontal position by two vertical ropes. One rope is attached to the beam at A and the other rope is attached to the point C on the beam where CB = 0.5 m, as shown in Figure 3. A particle P of mass 60 kg is attached to the beam at B and the beam remains in equilibrium in a horizontal position. The beam is modelled as a uniform rod and the ropes are modelled as light strings.

(a) Find

- (i) the tension in the rope attached to the beam at A,
- (ii) the tension in the rope attached to the beam at C.

Particle P is removed and replaced by a particle Q of mass $M \, \text{kg}$ at B. Given that the beam remains in equilibrium in a horizontal position,

(b) find

- (i) the greatest possible value of M,
- (ii) the greatest possible tension in the rope attached to the beam at C.

(6)

(6)



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Question Number	Scheme	Marks
5(a)	$T_A + T_C = 85 g$	
	OR $M(A)$, $25g \times 2.5 + 60g \times 5 = 4.5 \times T_c$	M1 A1
	OR $M(C)$, $T_A \times 4.5 + 60g \times 0.5 = 25g \times 2$	
	OR $M(B)$, $T_A \times 5 + T_C \times 0.5 = 25g \times 2.5$	
	OR $M(G)$, $T_A \times 2.5 + 60g \times 2.5 = 2 \times T_C$	M1 A1
	$T_A = \frac{40g}{9} = 44$ N or 43.6N; $T_C = \frac{725g}{9} = 790$ N or 789 N	A1; A1 (6)
(b)	$M(C), \ 25g \times 2 = Mg \times 0.5$	M1 A1
(i)	M = 100	A1
(ii)	$T_c = 25g + 100g$	M1 A1
	$T_c = 125g \ (1200 \text{ or } 1230) \text{N}$	D1 (0 12
	Notes	B1 (6) 12
5(a) 5(b)	First M1 for a moments or vertical resolution equation, with correct no. of terms and dimensionally correct. First A1 for a correct equation. Second M1 for a moments equation, with correct no. of terms and dimensionally correct. Second A1 for a correct equation. Third A1 for 44 (N) or 43.6 (N) or 40g/9 Fourth A1 for 790 (N) or 789 (N) or 725g/9 Deduct 1 mark for inexact multiples of g <u>N.B.</u> If they assume that both tensions are the same, can only score max M1 in (a) for $M(A)$ or $M(C)$. If a vertical resolution is used, please give marks for this equation FIRST. If not, enter marks for each moments equation in the order in which they appear.	
	SCHEME CHANGE B1 BECOMES THE FOURTH A1 First M1 for a moments equation with $T_A = 0$ First A1 for a correct equation Second A1 for $M = 100$ Second M1 for a(nother) moments or vertical resolution equation with $T_A = 0$ Third A1 for a correct equation Fourth A1 (B1) for $T_C = 125g$ or 1230 (N) or 1200 (N) N.B. Some candidates may need to solve 2 simult. equations in M and T_C and so will earn the 'equation' marks before they earn Second and Fourth A (B) marks. If a vertical resolution is used, please give marks for this equation	

in which they appear.

The possible equations are: $T_{\rm C} = 25g + Mg$ $M(C), 25g \ge 2 = Mg \ge 0.5$ $M(A), 25g \ge 2.5 + 5Mg = 4.5 T_{\rm C}$ $M(B), 25g \ge 2.5 = T_{\rm C} \ge 0.5$ $M(G), T_{\rm C} \ge 2 = Mg \ge 2.5$

Any two of these can each earn M1A1 (M0 if incorrect no. of terms) Then Second A1 for M = 100And Fourth A1 (B1) for $T_{\rm C} = 125$ g or 1230 or 1200

N.B. No marks in (b) if they use any answers from (a) or M = 60

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		L
6.	A particle <i>P</i> is moving with constant velocity. The position vector of <i>P</i> a $(t \ge 0)$ is r metres, relative to a fixed origin <i>O</i> , and is given by	t time t seconds
	$\mathbf{r} = (2t - 3)\mathbf{i} + (4 - 5t)\mathbf{j}$	
	(a) Find the initial position vector of <i>P</i> .	
		(1)
	The particle <i>P</i> passes through the point with position vector $(3.4\mathbf{i} - 12\mathbf{j})$ n time <i>T</i> seconds.	n at
	(b) Find the value of <i>T</i> .	
		(3)
	(c) Find the speed of <i>P</i> .	
		(4)

Summer 2015 Past Paper (Mark Scheme)

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Question	Ochama		
Number 6(a)	\mathbf{Scheme} $\mathbf{r} = (-3\mathbf{i} + 4\mathbf{j}) \mathbf{m}$	B1 Ma	<u>rks</u> (1)
(b)	3.4 = 2T - 3 or $-12 = 4 - 5T$	M1 A1	
	T = 3.2		
(c)	$\mathbf{r} = (-3\mathbf{i} + 4\mathbf{j}) + t(2\mathbf{i} - 5\mathbf{j})$	A1 M1	(3)
	v = (2i - 5j) v = (2i - 5j)		
	$\mathbf{v} = (2\mathbf{i} - 3\mathbf{j})$	A1	
	$\sqrt{\left(2^2 + (2^2)^2\right)}$	M1 A1	(4)
	speed = $\sqrt{(2^2 + (-5)^2)} = \sqrt{29} = 5.4 \text{ m s}^{-1}$ or better		
Alt (c)			8
	$\int \int (-1)^2 (-1)^2 = (-1)^2$		
	$ \mathbf{s} = \sqrt{6.4^2 + (-16)^2} = 17.23$	M1 A1	
	$\therefore \text{ speed} = \frac{17.23}{3.2} = 5.4 \text{ or better}$	M1 A1	(4)
	3.2 Notes		
6(a)	Allow column vectors throughout. B1 for $(-3i+4j)$ (m)		
(b)	M1 for a clear attempt at aithor $3 \land (i) = (2T \land 2) (i)$ or $12(i) = (4 \land 5T) (i)$		
	either 3.4 (i)= $(2T-3)$ (i) or $-12(j) = (4-5T)$ (j) First A1 for a correct equation (either) without i's and j's		
	A1 for 3.2 oe		
	N.B. $T = \frac{6.4\mathbf{i} - 16\mathbf{j}}{2\mathbf{i} - 5\mathbf{j}} = 3.2$ scores M1A1A1 <u>BUT</u> if RHS is not a single		
	number, then M0. Also, if they get 3.2 and another value and don't clearly choose 3.2 then A0		
	clearly choose 5.2 then Ab		
(c)	First M1 for a complete method for finding v		
	e.g. $\mathbf{r} = (-3\mathbf{i} + 4\mathbf{j}) + t(2\mathbf{i} - 5\mathbf{j})$ so $\mathbf{v} = 2\mathbf{i} - 5\mathbf{j}$		
	OR: $\mathbf{v} = \frac{(3.4\mathbf{i} - 12\mathbf{j}) - (-3\mathbf{i} + 4\mathbf{j})}{\text{their } T}$		
	$d\mathbf{r}$ $d\mathbf{r}$		
	OR: $\mathbf{v} = \frac{\mathrm{d}\mathbf{r}}{\mathrm{d}t} = 2\mathbf{i} - 5\mathbf{j}$		
	First A1 for $2i-5j$; M1A1 can be awarded for $2i-5j$ only.		
	Second M1 for attempt to find magnitude of their v , i.e. $\sqrt{2^2 + (-5)^2}$		
	Second A1 for $\sqrt{29}$ or 5.4 or better		
	OR		
	First M1 for attempt to find distance travelled:		
	$d = \sqrt{(-3 - 3.4)^2 + (412)^2}$		
	First A1 if correct		
	Second M1 for their d / their T		
	Second A1 for $\sqrt{29}$ or 5.4 or better		

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- 7. A train travels along a straight horizontal track between two stations, A and B. The train starts from rest at A and moves with constant acceleration 0.5 m s⁻² until it reaches a speed of $V \text{ m s}^{-1}$, (V < 50). The train then travels at this constant speed before it moves with constant deceleration 0.25 m s⁻² until it comes to rest at B.
 - (a) Sketch in the space below a speed-time graph for the motion of the train between the two stations *A* and *B*.

(2)

(5)

(6)

The total time for the journey from A to B is 5 minutes.

(b) Find, in terms of V, the length of time, in seconds, for which the train is

- (ii) decelerating,
- (iii) moving with constant speed.

Given that the distance between the two stations A and B is 6.3 km,

(c) find the value of *V*.

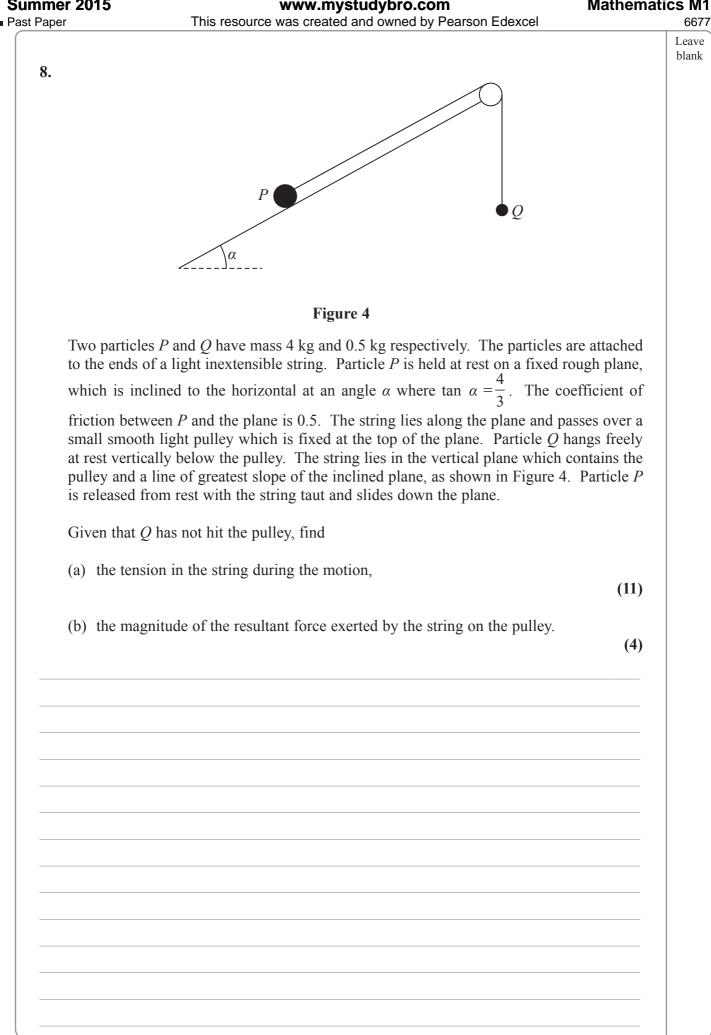


⁽i) accelerating,

Question Number	Scheme	Marks
7(a)	V	B1 (shape) B1 (V) (2)
(b) (i) (ii)	$\frac{V}{t_1} = \frac{1}{2} \implies t_1 = 2V \text{ s}; \ t_2 = 4V \text{ s}$	M1 A1; A1
(iii)	$t_3 = 300 - 2V - 4V = 300 - 6V s$	M1 A1 (5)
(c)	$6300 = \frac{V(300 + 300 - 6V)}{2} \text{ or } \frac{1}{2}2V.V + (300 - 6V).V + \frac{1}{2}4V.V$	M1 A1 ft
	$V^{2} - 100V + 2100 = 0$ (V - 30)(V - 70) = 0	A1 M1 A1
	V = 30 or 70 V = 30 (< 50)	A1 (6)
7(a)	NotesB1 for a trapezium with line starting and finishing on the <i>t</i> -axisB1 for V correctly marked	
(b)	First M1 for a correct method First A1 for $V/0.5$ oe Second A1 for $V/0.25$ oe Second M1 for $(300 - \text{sum of previous answers})$ Allow 5 instead of 300. Third A1 for $300 - 6V$ oe	
(c)	First M1 for using the area under the curve (distance travelled) to form an equation in V only. (Allow use of 6.3 but must see $\frac{1}{2}$ used at least once in their expression.) First A1 ft on their answers in (b) for a correct equation so must have used 6300 not 6.3 Second A1 for correct equation in form $aV^2 + bV + c = 0$ Second M1 for solving a 3 term quadratic. (Can be implied by correct <u>answers</u>) Second A1 for either 30 or 70	

Third A1 for 30 as final answer. N.B. If answer(s) are wrong or have come from an incorrect quadratic, and the quadratic formula is used, M1 can only be awarded if there is clear evidence that the correct formula has been used. i.e. we need to see numbers substituted into a stated correct formula.	





Question Number	Scheme	Marks
8(a)	$R = 4g \cos \alpha$	M1 A1
	T - 0.5g = 0.5a	
	$4g\sin\alpha - T - F = 4a$	M1 A1 M1 A1
		IVIT AT
	(OR: $4g\sin\alpha - F - 0.5g = 4.5a$)	
	$F = \frac{1}{2}R;$ $\sin \alpha = \frac{4}{5}$ or $\cos \alpha = \frac{3}{5}$	B1; B1
	Eliminating <i>a</i> or finding <i>a</i>	M1
	Solving for T (must have had an a)	MI
	$T = \frac{2g}{3}$ N or 6.5N or 6.53N	A1
		(11
(b)	$(90-\alpha)$	(
	Magnitude = $2T \cos\left(\frac{90-\alpha}{2}\right)$	M1 A1
	$= 2 \ge \frac{2g}{3} \ge \frac{3}{\sqrt{10}} = (0.94868)$	A1 ft on T
	$= 12N \text{ or } 12.4N \left(\frac{4g}{\sqrt{10}}\right)$	A1 (4)
	Notes	1
8 (a)	First M1 for resolving perp to plane, with usual criteria	
	First A1 for a correct equation	
	Second M1 for resolving vertically, with usual criteria	
	Second A1 for a correct equation, in terms of a and T	
	Third M1 for resolving parallel to the slope, with usual criteria.	
	Third A1 for a correct equation , in terms of a , F and T	
	₽ <i>2</i>	
	<u>N.B. Their <i>a</i> could be UP the slope in which case all 4 marks for the 2</u>	
	equations are available with – <i>a</i> replacing <i>a</i> , provided they are	
	consistent. If they are inconsistent, then assume the vertical resolution	
	is the correct one and mark accordingly.	
	Either of the above two equations can be replaced by the 'whole	
	system' equation	
	N.B. If they use $a = 0$, in any of the above 3 equations, and they	
	use the equation to find T, they lose both marks for that equation,	
	and they lose the two M marks for eliminating and solving.	
	First B1 for $F = \frac{1}{2}R$ seen or implied;	
	Second B1 for $\sin \alpha = 0.8$ or $\cos \alpha = 0.6$ seen or implied. Allow close approximations if $\alpha = 53.1^{\circ}$ used.	
	Fourth M1 independent for eliminating <i>a</i> or finding <i>a</i> .	
	Fifth M1 for solving for <i>T</i> but must have had an <i>a</i> .	
	Fourth A1 for $2g/3$, 6.5 or 6.53.	
	1 ourum 111 101 26/5, 0.5 01 0.55.	

