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Surname		Other names	
Pearson Edexcel	Centre Number	Ca	andidate Number
<b>CORE IVIATI</b> Advanced Subsidia	iema <sup>y</sup>		L12
<b>Core Ivlatr</b> Advanced Subsidiar Wednesday 24 May 2017 – <b>Time: 2 hours 30 minutes</b>	nema ry Morning	CICS ( Par W	Der Reference

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

# Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets – use this as a guide as to how much time to spend on each question.

# Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over 🕨



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Summer Past Paper	2017 www.mystudybro.com This resource was created and owned by Pearson Edexcel	Mathematic	<b>s C12</b> WMA01
<b>1.</b> <i>A</i>	An arithmetic sequence has first term 6 and common difference 10		Leave blank
(	a) the 15th term of the sequence,	(2)	
(	b) the sum of the first 20 terms of the sequence.	(2)	

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P 5 1 4 0 2 A 0 2 5 6

WMA01
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Question Number	Scheme	Marks
1 (a)	$a + 14d = 6 + 14 \times 10 = 146$	M1 A1
(b)	$\frac{20}{2}(2a+19d) = 10(12+190) = 2020$	(2) M1 A1 (2) (4 marks)

(a)

M1	For attempting $a + 14d$ with $a = 6$ and $d = 10$ . Alternatively lists 6, 16, 26, 36, with 15 terms and picks out the 15th term
A1	146
(b)	
M1	For attempting $\frac{n}{2}(2a+(n-1)d)$ with $n = 20$ , $a = 6$ and $d = 10$
	For attempting $\frac{n}{2}(a+l)$ with $n = 20$ , $a = 6$ and $l = a + 19d$

Alternatively lists 6+ 16+ 26+ 36+... (with or without the +signs) with 20 terms and adds A1 2020

Do not allow misreads in either case. For example, finding the 20<sup>th</sup> term in part (a) or the sum to 15 terms in part (b) is M0

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<b>2.</b> Simplify the for	llowing expressions fully.		Leave blank
(a) $\left(\frac{1}{9}x^4\right)^{0.5}$		(1)	
(b) $\left(\frac{x}{\sqrt{2}}\right)^{-2}$		(1)	
(c) $x\sqrt{3} \div \sqrt{\frac{43}{x^2}}$	8/4	(2)	

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Question Number	Scheme	Marks
2 (a)	$\frac{1}{3}x^2$	B1
	$(x)^{-2}$ 2	(1)
( <b>b</b> )	$\left(\frac{x}{\sqrt{2}}\right) = \frac{2}{x^2}$	B1
		(1)
( <b>c</b> )	$\sqrt{3}(x) \div \sqrt{\frac{48}{x^4}} = \frac{\sqrt{3}}{\sqrt{48}} \times x\sqrt{x^4} = \frac{1}{4}x^3$	M1A1
		(2) (4 marks)

(a)

B1 
$$\frac{1}{3}x^2$$
 Accept exact alternatives like  $\frac{x^2}{3}$  and  $0.3x^2$  but not expressions such as  $0.33x^2$  (b)

B1 
$$\frac{2}{x^2}$$
 Accept exact alternatives such as  $2 \times x^{-2}$  or  $2 \times \frac{1}{x^2}$  (All forms must have a '2')

M1 Either the correct coefficient (accept  $\frac{1}{4}$  or 0.25) or the correct power of x (accept  $x^3$  or  $\frac{1}{x^{-3}}$ ) A1 Only accept  $\frac{1}{4}x^3$  or simplified equivalents such as  $0.25 \times x^3$  Do NOT accept  $\frac{1}{4x^{-3}}$  for this mark.

Summer 2017 Past Paper	www.mystudybro.com         Ma           This resource was created and owned by Pearson Edexcel         Ma	athematics C1
		Leave
3. The line	$l_1$ has equation $2x + 3y = 6$	blank
The line	e $l_2$ is parallel to the line $l_1$ and passes through the point $(3, -5)$ .	
Find the	equation for the line l in the form $y = mr + c$ , where m and c are constant	te
Find the	e equation for the line $l_2$ in the form $y - mx + c$ , where <i>m</i> and <i>c</i> are constant	(4)
6		
U		

#### **Summer 2017**

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**Mathematics C12** 

Past Paper (Mark S	Scheme) This resource was created and owned by Pearson Edexcel	WMA01
Question Number	Scheme	Marks
3	$2x + 3y = 6 \Longrightarrow y = -\frac{2}{3}x + \dots$	B1
	Equation of $l_2$ is $y = -\frac{2}{3}x + c$	M1
	Substitutes 3,-5 into $y = -\frac{2}{3}x + c \Rightarrow -5 = -\frac{2}{3} \times 3 + c$	M1
	$y = -\frac{2}{3}x - 3$	A1
		(4 marks)
Alt	Equation of $l_2$ is $2x + 3y = c$	B1 M1
	Substitutes 3,-5 into $2x+3y=c \Rightarrow 6-15=c$	M1
	2x + 3y = -9	
	$y = -\frac{2}{3}x - 3$	A1
		(4 marks)
	1	1

States or implies the gradient of  $l_1$  is  $-\frac{2}{3}$  Alternatively accept  $l_1$  written in the form  $y = -\frac{2}{3}x + ...$ **B**1 States or implies the gradient of  $l_2$  is the same as  $l_1$  Eg.  $y = -\frac{2}{3}x + c$ . **M**1

If the gradient of  $l_2$  is incorrect then you must see

- Evidence that the gradient used for  $l_2$  has been linked with the gradient of  $l_1$ For example 2x+3y=6 Gradient of  $l_1$  is 2 so equation of  $l_2$  is y=2x+c
- Or a statement that the gradients are the same. 2x+3y=6 The gradient of  $l_1$  is 6 so • gradient of  $l_2$  is 6.

You must see some evidence of the candidate using equal gradients. They cannot just write down a gradient for this mark. So for example, given 2x+3y=6 gradient of  $l_2$  is 2 or equation of  $l_2$  is y = 2x + c scores M0, as there is insufficient evidence of the candidate using equal gradients. In the alternative scheme the first two marks can be implied by stating that the new equation is of the form 2x + 3y = c

M1 Substitutes 3,-5 into their 
$$y = -\frac{2}{3}x + c \Rightarrow c = \dots$$
 Also score for  $-\frac{2}{3} = \frac{y - 5}{x - 3}$  or

It is for knowing how to find an equation of a line knowing the gradient with the point 3, -5Hence follow through on an incorrect gradient, even a perpendicular one.

A1 
$$y = -\frac{2}{3}x - 3$$
 Accept forms like this  $y = \left(-\frac{2}{3}\right)x + \left(-3\right)$ 

 $y = -\frac{2}{3}x + ... \Rightarrow y = \frac{3}{2}x + c \Rightarrow -5 = \frac{3}{2} \times 3 + c \Rightarrow c = ..$ 

# Mathematics C12

WMA01 Leave

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- 4. The curve C has equation  $y = 4x\sqrt{x} + \frac{48}{\sqrt{x}} \sqrt{8}, x > 0$ 
  - (a) Find, simplifying each term,

(i) 
$$\frac{dy}{dx}$$
  
(ii)  $\frac{d^2y}{dx^2}$ 

(b) Use part (a) to find the exact coordinates of the stationary point of C.

(5)

(c) Determine whether the stationary point of C is a maximum or minimum, giving a reason for your answer.

(2)



#### Summer 2017 Past Paper (Mark Sc

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Mathematics C12

t <mark>Paper (Mark S</mark>	cheme) This resource was created and owned by Pearson Edexcel	WMA01
Question Number	Scheme	Marks
4(a)(i)	$\frac{dy}{dx} = 6x^{0.5} - 24x^{-1.5}$	M1A1A1
(ii)	$\frac{d^2 y}{dx^2} = 3x^{-0.5} + 36x^{-2.5}$	M1A1
		(5)
<b>(b</b> )	$\frac{\mathrm{d}y}{\mathrm{d}x} = 0 \Longrightarrow 6x^{0.5} - 24x^{-1.5} = 0$	M1
	$x^2 = 4 \Longrightarrow x = 2$	dM1, A1
	Substitutes their $x = 2$ into $y = 4x\sqrt{x} + \frac{48}{\sqrt{x}} - \sqrt{8} \Rightarrow y = 30\sqrt{2}$	M1,A1
		(5)
(c)	Substitutes their $x = 2$ into their $\frac{d^2 y}{dx^2} = 3x^{-0.5} + 36x^{-2.5}$	M1
	Statement +reason. ie $\frac{d^2 y}{dr^2} > 0 \Rightarrow$ minimum	A1 cso
		(2)
		(12 marks)

M1 For a correct power on any of the 'three' terms including the  $\sqrt{8} \rightarrow 0$ .

A1 Two of the three terms correctly differentiated (can be unsimplified) Volume accort  $6x^{0.5}$  as  $4x^{1.5}x^{1.5-1}$  and  $24x^{-1.5}$  as  $148x^{-1}x^{-0.5}$ .

You may accept  $6x^{0.5}$  as  $4 \times 1.5x^{1.5-1}$  and  $-24x^{-1.5}$  as  $+48 \times -\frac{1}{2}x^{-0.5-1}$ 

A1 Cao but remember to isw. Accept alternatives for the terms in x such as  $x^{0.5} = \sqrt{x} = x^{\frac{1}{2}}$ Allow expressions given in the form of the question  $\left(\frac{dy}{dx}\right) = 6\sqrt{x} - \frac{24}{x\sqrt{x}}$ 

(a)(ii)

M1 Differentiating again. Scored for reducing any **fractional** power by one (seen once allowing follow through)

A1 Cao. See part (i) notes for acceptable alternatives. Eg accept  $\left(\frac{d^2 y}{dx^2}\right) = \frac{3}{\sqrt{x}} - \frac{36}{x^2\sqrt{x}}$ 

M1 Sets (or implies that) their  $\frac{dy}{dx} = 0$ 

- dM1 Dependent upon the previous M. For forming an equation of the type  $x^n = A$ , following correct index work.
- A1 x = 2 (Ignore any reference to x = -2). Part (a) must be correct and both M's must have been scored.

# M1 For substituting their solution (of $\frac{dy}{dx} = 0$ ) into $y = 4x\sqrt{x} + \frac{48}{\sqrt{x}} - \sqrt{8} \Rightarrow y = ....$

- A1  $(y) = 30\sqrt{2}$  Part (a) must be correct and all three M's must have been scored.
- (c)

M1 For substituting their x = 2 into their  $\left(\frac{d^2y}{dx^2}\right) = 3x^{-0.5} + 36x^{-2.5}$  and finding (or implying to find)

a numerical result. Alternatively, for substituting their x = 2 into their  $\left(\frac{d^2y}{dx^2}\right) = 3x^{-0.5} + 36x^{-2.5}$ 

and considering the sign. Eg When  $x = 2 \Rightarrow 3 \times 2^{-0.5} + 36 \times 2^{-2.5} > 0$ 

A1 CSO Requires a correct x = 2 and a correct  $\left(\frac{d^2 y}{dx^2}\right) = 3x^{-0.5} + 36x^{-2.5}$ 

A statement and a conclusion is required to score this mark. Allow the candidate to state that when x = 2  $\frac{d^2 y}{dx^2} = 3 \times 2^{-0.5} + 36 \times 2^{-2.5} > 0 \Rightarrow$  minimum If the candidate gives the numerical value to  $\frac{d^2 y}{dx^2}$ , it must be correct. Accept  $6\sqrt{2}$  oe or awrt 8.5

Alternatives in part (c)

- M1 Finding the value of 'y' at x = 2, left of 2 and right of 2. Alternatively finding the  $\frac{dy}{dx}$  at x = 2, left of 2 and right of 2
- A1 A statement and a conclusion is required to score this mark. A sketch graph can be used instead of a statement. Numerical values must be correct.



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Question Number	Scheme	Marks	
<b>5</b> (a)	Attempts f (±1)	M1	
	Remainder =2	A1	
			(2)
<b>(b</b> )	Attempts $f(\pm 3) = -4 \times (\pm 3)^3 + 16 \times (\pm 3)^2 - 13 \times (\pm 3) + 3$	M1	
	Remainder = $0 \Rightarrow (x-3)$ is a factor	A1*	
			(2)
(c)	Divides their $f(x)$ by $(x-3)$ to get the quadratic factor	M1	
	$(-4x^2+4x-1)$	A1	
	$f(x) = (x-3) \times -(2x-1)(2x-1) = (3-x)(2x-1)^2$	dM1A1	
			(4)
( <b>d</b> )	$f(x) \leqslant 0 \Longrightarrow (3-x)(2x-1)^2 \leqslant 0$		
	$x = \frac{1}{2}, x \ge 3$	B1,B1	
		(10 mark	(2) s)

- (a)
- M1 Attempts to calculate  $f(\pm 1)$  condoning slips. Algebraic division does not score this mark.
- A1 (Remainder is) 2 Accept sight of f(1) = 2 for both marks
- (b)
- M1 Attempts to find f (±3) condoning slips. We must see some substitution or calculation  $-4 \times (\pm 3)^3 + 16 \times (\pm 3)^2 - 13 \times (\pm 3) + 3$  or -108 + 144 - 39 + 3 is OK. We cannot accept just sight of 'f(3) =0' Algebraic division does not score this mark.

A1\* It is a "show that" so requires both a statement and a conclusion. For example  $f(3) = -4 \times (3)^3 + 16 \times (3)^2 - 13 \times (3) + 3 = 0 \Rightarrow (x - 3)$  is a factor. The conclusion could be QED or a tick following the working to f(3) = 0It could also as a preamble before the working.

- (c)
- M1 Divides f(x) by (x-3) to get a quadratic. If part (b) is done by division it can be awarded in (c) from work in (b). If inspection is used look for first and last terms. Eg  $f(x) = (x-3)(\pm 4x^2 + ...x \pm 1)$

If division is used look for first two terms x-3

$$-3) \frac{\pm 4x^2 \pm 4x...}{-4x^3 + 16x^2 - 13x + 3}$$
$$\frac{-4x^2 + 12x^2}{4x^2}$$

- A1  $(-4x^2+4x-1)$
- dM1 Dependent upon the previous M. For further factorisation of their  $(-4x^2+4x-1)$ Method and accuracy marks may be awarded if seen in part (d)

A1 
$$f(x) = (3-x)(2x-1)^2$$
,  $f(x) = -(x-3)(2x-1)^2 f(x) = (x-3)(2x-1)(-2x+1)$   
 $f(x) = 4(3-x)\left(x-\frac{1}{2}\right)\left(x-\frac{1}{2}\right)$  oe You do not need to see the  $f(x)$   
If there is little or no working in (c) with no quadratic factor seen then

If there is little or no working in (c) with no quadratic factor seen then..... award all marks if the answer is correct (See above for possible options) award M1 A0 M1 A0 by implication for  $(x-3)(2x-1)^2$  or equivalent

award no marks for answers such as  $(x-3)(x-\frac{1}{2})^2$ 

- (d) It is quite difficult to ascertain whether candidates are finding roots or solving the question so mark as follows
- B1 Sight of either  $\frac{1}{2}$  and/or 3 seen in part (d).
- B1 Both of  $x = \frac{1}{2}$ ,  $x \ge 3$  Do not accept this if candidates write down roots first and just  $x \ge 3$  later Accept set language Eg  $\left\{ x : x = \frac{1}{2} \cup x \ge 3 \right\}$



#### Summer 2017 Past Paper (Mark Scheme)

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Scheme	Marks
$\cos \angle BAC = \frac{12^2 + 10^2 - 6^2}{2 \times 12 \times 10} \Rightarrow \angle BAC = 0.5223$	M1A1
Arc $BD = r\theta = 10 \times 0.5223$ Perimeter = 6+2+ 10×0.5223=13.22 (m)	(2) M1 dM1,A1 (3)
Area of sector $BAD = \frac{1}{2}r^2\theta = \frac{1}{2} \times 10^2 \times 0.5223$ (= 26.116)	M1
Area of triangle $ABC \frac{1}{2}ab\sin C = \frac{1}{2} \times 12 \times 10 \times \sin 0.5223$ (= 29.932) Area of flowerbed $BCD = \frac{1}{2} \times 12 \times 10 \times \sin 0.5223 = \frac{1}{2} \times 10^2 \times 0.5223$	M1 dM1
$= 3.81 / 3.82 \text{ (m}^2)$	A1 (4) (9 marks)
	Scheme $\cos \angle BAC = \frac{12^2 + 10^2 - 6^2}{2 \times 12 \times 10} \Rightarrow \angle BAC = 0.5223$ Arc $BD = r\theta = 10 \times 0.5223$ Perimeter = 6+2+ 10×0.5223=13.22 (m) Area of sector $BAD = \frac{1}{2}r^2\theta = \frac{1}{2} \times 10^2 \times 0.5223$ (= 26.116) Area of triangle $ABC \frac{1}{2}ab \sin C = \frac{1}{2} \times 12 \times 10 \times \sin 0.5223$ (= 29.932) Area of flowerbed $BCD = \frac{1}{2} \times 12 \times 10 \times \sin 0.5223 - \frac{1}{2} \times 10^2 \times 0.5223$ $= 3.81 / 3.82 \text{ (m}^2)$

(a)

M1 Attempts use of the formula  $6^2 = 10^2 + 12^2 - 2 \times 10 \times 12 \cos A$  or  $\cos \angle BAC = \frac{12^2 + 10^2 - 6^2}{2 \times 12 \times 10}$ The sides must be in the correct "position" within the formula. Condone different notation Eg.  $\theta$ 

A1  $\angle BAC = awrt \ 0.5223$  The angle in degrees (awrt 29.9°) is A0

(b)

- M1 Attempts arc formula: In radians uses Arc  $BD = r\theta = 10 \times "0.5223"$ In degrees uses Arc  $BD = \frac{\theta}{360} \times 2\pi r = \frac{"29.9"}{360} \times 2\pi \times 10$
- dM1 Dependent upon the arc formula having been used. It is for calculating the perimeter as 8 + arc length.
  A1 Derimeter awart 12 22 (m)
- A1 Perimeter = awrt 13.22(m)
- (c)
- M1 Attempts area of sector formula: Area of sector  $BAD = \frac{1}{2}r^2\theta = \frac{1}{2} \times 10^2 \times "0.5223"$ In degrees uses Area of sector  $BAD = \frac{\theta}{360} \times \pi r^2 = \frac{"29.9"}{360} \times \pi \times 10^2$

M1 Attempts area of triangle formula: Area of triangle  $ABC = \frac{1}{2}ab\sin C = \frac{1}{2}\times12\times10\times\sin^{\circ}0.5223^{\circ}$ You may see Herons formula used with  $S = \frac{10+6+12}{2} = (14)$  and  $A = \sqrt{S(S-10)(S-6)(S-12)}$ Watch for other methods including the calculation of a perpendicular.

dM1 Dependent upon both correct formulae. It is scored for finding area of triangle - area of sector A1 Allow awrt 3.81 or 3.82 (m<sup>2</sup>)

# Mathematics C12

**WMA01** 

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Figure 3 shows a sketch of part of the curve with equation y = f(x).

The curve crosses the *y*-axis at the point (0, 8).

The line with equation y = 10 is the only asymptote to the curve.

The curve has a single turning point, a minimum point at (2, 5), as shown in Figure 3.

- (a) State the coordinates of the minimum point of the curve with equation  $y = f\left(\frac{1}{4}x\right)$ (1)
- (b) State the equation of the asymptote to the curve with equation y = f(x) 3

The curve with equation y = f(x) meets the line with equation y = k, where k is a constant, at two distinct points.

- (c) State the set of possible values for *k*.
- (d) Sketch the curve with equation y = -f(x). On your sketch, show clearly the coordinates of the turning point, the coordinates of the intersection with the y-axis and the equation of the asymptote.

(3)

(2)

(1)

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(a)
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B1 Accept (8, 5) or x = 8, y = 5 or a sketch of  $y = f\left(\frac{1}{4}x\right)$  with a minimum point marked at (8, 5)

(b)

B1 y = 7. It must be an equation and not just '7'

- (c)
- M1 Accept one "side" of the inequality condoning a misunderstanding of whether the boundary is included or not. Allow for k > 5,  $k \ge 5$ , k < 10,  $k \le 10$  Condone a different variable for the M1
- A1 cao 5 < k < 10. Allow k > 5 and k < 10 k > 5, k < 10 (5,10)  $\{k \in \mathbb{R} : 5 < k < 10\}$ Do not allow k > 5 or k < 10
- (d)

B1 For a reflection of the original curve in the x – axis. Look for the shape shown in the scheme but be tolerant of slips at either end.
B1 For the graph to have an intercept of (0,-8) and a (single) maximum point of (2,-5) Accept -8 being marked on the y- axis and the graph passing through this.

Condone (-8,0) as long as it is marked on the correct axis

B1 For giving the equation of the asymptote as y = -10The graph must clearly be asymptotic but be tolerant of slips. See practice items for clarification.

<b>umme</b> st Paper	r 2017 www.mystudybro This resource was created and owne	b.com Mathematic d by Pearson Edexcel	SC1
8.	(a) Find $\int (3x^2 + 4x - 15) dx$ , simplifying each term	ı. (3)	Leav blanl
	Given that <i>b</i> is a constant and		
	$\int_{b}^{4} (3x^2 + 4x - 15)  \mathrm{d}x = 1$	36	
	(b) show that $b^3 + 2b^2 - 15b = 0$	(2)	
	(c) Hence find the possible values of <i>b</i> .	(3)	
24			

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#### Summer 2017 Past Paper (Mark Sch

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**Mathematics C12** 

t Paper (Mark S	cheme) I his resource was created and owned by Pearson Edexcei	VVIVIA	401
Question Number	Scheme	Marks	
8 (a)	$\int (3x^2 + 4x - 15) dx = x^3 + 2x^2 - 15x + c$	M1A1A1	
(b)	$\int_{b}^{4} (3x^{2} + 4x - 15) dx = \left[ x^{3} + 2x^{2} - 15x + (c) \right]_{b}^{4} = 36$		(3)
	$(64+32-60) - (b^3+2b^2-15b) = 36$	M1	
	$b^3 + 2b^2 - 15b = 0$	A1*	(2)
(c)	b = 0	B1	
	$b^2 + 2b - 15 = 0 \Longrightarrow (b+5)(b-3) = 0$	M1	
	<i>b</i> = -5, 3	A1	
			(3)
		(8 marks)	

(a)

- M1 Raises the index of any term in *x* by one
- A1 Two of the three algebraic terms correct (unsimplified). For example accept  $2x^2 = \frac{4}{2}x^{1+1}$
- A1 cao including the +c
- (b)
- M1 Substitutes 4 and *b* into their integrated expression, subtracts either way around and sets equal to 36
- A1\* Simplifies to the given solution. This is a given answer and therefore the intermediate line(s) must be correct. Minimum expectation for an intermediate line is  $36-(b^3+2b^2-15b)=36$  or equivalent with the bracket removed.
- (c)
- B1 b=0
- M1 Factorises/ attempts to solve the quadratic
- A1 b = -5, 3

<b>C12</b> /MA01
Leave

<b>Summer 2017</b> Past Paper (Mark S	cheme) This resource was created and owned by Pearson Edexcel	Mathematics C12 WMA01
Question Number	Scheme	Marks
9(i)	$2\log_{10}(x-2) - \log_{10}(x+5) = 0 \Longrightarrow \log_{10}(x-2)^2 = \log_{10}(x+5)$	M1
	$\Rightarrow (x-2)^2 = (x+5)$	M1
	$\Rightarrow x^2 - 5x - 1 = 0$	A1
	$x = \frac{5 \pm \sqrt{29}}{2} \Longrightarrow x = \frac{5 \pm \sqrt{29}}{2}$ only	M1,A1
		(5)
(ii)	$\log_p(4y+1) - \log_p(2y-2) = 1 \Longrightarrow \log_p\left(\frac{4y+1}{2y-2}\right) = \log_p p$	M1, M1
	$\Rightarrow \left(\frac{4y+1}{2y-2}\right) = p$	A1
	$\Rightarrow 4y + 1 = 2py - 2p \Rightarrow y = \frac{1 + 2p}{2p - 4}$	M1A1

(i)

- M1 Use of the power law of logs
- For 'undoing' the logs by either setting  $\log_{10} \dots = \log_{10} \dots$  or using the subtraction law and  $0 = \log_{10} 1$ M1

(5)

(10 marks)

A1 A correct simplified quadratic 
$$x^2 - 5x - 1 = 0$$

M1 A correct attempt to find a solution to a 3TQ of equivalent difficulty (ie no factors). Allow formula, completing the square and use of a calculator giving exact or decimal answers

A1 cso 
$$\frac{5+\sqrt{29}}{2}$$
 or exact simplified equivalent without extra answers.

- (ii)
- Use of subtraction (or addition) law of logs M1
- For using  $1 = \log_{p} p$  or equivalent in an attempt to get an equation not involving logs. **M**1

$$\log_p(4y+1) - \log_p(2y-2) = 1 \Rightarrow (4y+1) - (2y-2) = p \text{ implies this and scores M0 M1.}$$

- A correct equation in p and y not involving logs. Accept  $\left(\frac{4y+1}{2y-2}\right) = p^1$ A1
- Score for an attempt to change the subject. This must include cross multiplication, collection of M1 terms in y, followed by factorisation of the y term.

A1 cso 
$$y = \frac{1+2p}{2p-4}$$
 or equivalent such as  $y = \frac{-1-2p}{4-2p}$ 

Special cases in (i): Case 1 Allow the subtraction law either way around as the rhs of the equation will be 1

Case 2 
$$\log_{10} \frac{(x-2)^2}{(x+5)} = 0 \Rightarrow \frac{(x-2)^2}{(x+5)} = 0 \Rightarrow (x-2)^2 = (x+5) \Rightarrow x^2 - 5x - 1 = 0$$
  
$$\Rightarrow x = \frac{5 + \sqrt{29}}{2} \text{ only will be awarded M1 M0 A1 M1 A0}$$

Special cases in (ii):  $\log_p(4y+1) - \log_p(2y-2) = 1 \Rightarrow \frac{\log_p(4y+1)}{\log_p(2y-2)} = \log_p p \Rightarrow \left(\frac{4y+1}{2y-2}\right) = p^1$  $\Rightarrow 4y + 1 = 2py - 2p \Rightarrow y = \frac{1 + 2p}{2p - 4}$  will be awarded M0 M1A1 M1 A0|

(4)

WMA01 Leave

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10. (a) Find the first 3 terms, in ascending powers of x, of the binomial expansion of

$$\left(2-\frac{x}{8}\right)^{10}$$

giving each term in its simplest form.

$$f(x) = \left(2 - \frac{x}{8}\right)^{10} (a + bx)$$
, where a and b are constants

Given that the first two terms, in ascending powers of x in the series expansion of f(x), are 256 and 352x,

- (b) find the value of *a*,
- (c) find the value of b.

(2)

(2)

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#### Summer 2017 Past Paper (Mark Sc

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Mathematics C12

st	Paper (Mark S	Scheme) This resource was created and owned by Pearson Edexcel	WM	IA01
	Question Number	Scheme	Marks	
	10 (a)	$2^{10}$ OR 1024 seen as the constant term	B1	
		$\left(2 - \frac{x}{8}\right)^{10} = 2^{10} + {}^{10}C_1 2^9 \left(-\frac{x}{8}\right)^1 + {}^{10}C_2 2^8 \left(-\frac{x}{8}\right)^2 + \frac{x}{8}$	M1A1	
		$=1024 - 640x + 180x^2$	A1	(4)
		$\left(2 - \frac{x}{8}\right)^{10} \left(a + bx\right) = \left(1024 - 640x + 180x^2\right) \left(a + bx\right)$		(-)
	(b)	$1024a = 256 \Longrightarrow a = \frac{1}{4}$ oe	M1A1	(2)
	(c)	$1024b - 640a = 352 \Longrightarrow b = \frac{1}{2}$	M1A1	(2)
			(8 marks)	)

(a)

B1  $2^{10}$  OR 1024 seen as the constant term

M1 For a correct attempt at the binomial expansion for  $(a+b)^n$  with a=2,  $b=\pm\frac{x}{8}$  and n=10Condone missing brackets. Accept any unsimplified term in x as evidence Accept a power series expansion on  $(1\pm kx)^{10} = 1+10(\pm kx) + \frac{10\times 9}{2}(\pm kx)^2$  condoning missing brackets. Again accept any unsimplified term in x as evidence

A1 A completely correct unsimplified solution.

Accept = 
$$2^{10} + {}^{10}C_1 2^9 \left(-\frac{x}{8}\right)^1 + {}^{10}C_2 2^8 \left(-\frac{x}{8}\right)^2 +$$
  
Accept =  $2^{10} \left(1 + 10 \times \left(-\frac{x}{16}\right) + \frac{10 \times 9 \times \left(-\frac{x}{16}\right)^2}{2!} + ...\right)$ 

A1  $1024-640x+180x^2$  Accept  $1024+-640x+180x^2$ Can be listed with commas or appear on separate lines. Accept in reverse order.

(b) M1

Sets their '1024'  $\times a = 256$ 

A1  $a = \frac{1}{4}$ . Accept equivalents such as 0.25.

Accept this for both marks (it can be done by substituting x = 0 into both sides of the expression) as long as it is not found from an incorrect method

- (c)
- M1 Sets their '1024'  $\times b \pm$  their '640' a = 352

A1 
$$b = \frac{1}{2}$$
 or 0.5

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This resource was created and owned by Pearson Edexcel Leave blank 11. Wheat is to be grown on a farm. A model predicts that the mass of wheat harvested on the farm will increase by 1.5% per year, so that the mass of wheat harvested each year forms a geometric sequence. Given that the mass of wheat harvested during year one is 6000 tonnes, (a) show that, according to the model, the mass of wheat harvested on the farm during year 4 will be approximately 6274 tonnes. (2) During year N, according to the model, there is predicted to be more than 8000 tonnes of wheat harvested on the farm. (b) Find the smallest possible value of N. (5) It costs £5 per tonne to harvest the wheat. (c) Assuming the model, find the total amount that it would cost to harvest the wheat from year one to year 10 inclusive. Give your answer to the nearest £1000. (3) 36 P 5 1 4 0 2 A 0 3 6 5 6

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Past Paper (	Mark	Sch

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t <u>Paper (Mark S</u>	cheme) This resource was created and owned by Pearson Edexcel	WMA01
Question Number	Scheme	Marks
11 (a)	Attempts $U_4 = 6000 \times (1.015)^3 = 6274$ (tonnes)	M1A1*
(b)	Attempts $U_{N} = 6000 \times 1.015^{N-1} > 8000$	M1
	$1.015^{N-1} > \frac{8000}{6000}$ oe	A1
	$\log(1.015^{N-1}) > \log\left(\frac{4}{3}\right) \Rightarrow N > \frac{\log\left(\frac{4}{3}\right)}{\log(1.015)} + 1 = (20.3)$	M1A1
	(N) = 21	A1
(c)	Attempts $S_n = \frac{a(1-r^n)}{(1-r)}$ with $n = 10$ $a = 6000/30000$ and $r = 1.015$	(5) M1
	$S = 5 \times \frac{6000(1.015^{10} - 1)}{(1.015 - 1)} \text{ OR } S = \frac{30000(1.015^{10} - 1)}{(1.015 - 1)}$	A1
	Awrt £321 000	A1
		(3) (10 marks)

(a)

M1 Attempts to use  $ar^3$  with a = 6000, r = 1.015. Accept r = 1+1.5%Condone for this mark r = 1.15 or 1.0015 Accept a list of 4 terms with the same conditions A1\* cso  $6000 \times (1.015)^3 = 6274$  (tonnes).

If candidate states  $U_4 = 6000 \times (1.015)^3 = 6274.07$  (tonnes) or 6274.0 (or anything that rounds to 6274) they don't need to round to the given answer.

- (b)
- M1 Attempts to use  $ar^{n-1}$ ...8000 or  $ar^n$ ...8000 with a = 6000, r = 1.015 or 1+1.5% condoning values of *r* being 1.15 or 1.0015
- A1 For reaching the intermediate result  $1.015^{n-1}...\frac{4}{3}$  or  $1.015^n...\frac{4}{3}$ .

Allow  $\frac{4}{3}$  to be rounded or truncated to 1.33 (to 2dp or better)

- M1 Uses logs correctly to get *n* or *n*-1 This mark may be awarded from a sum formula
- A1 This is scored for a 'correct' (unrounded) answer. It may be left in log form. If the candidate has used n instead of n-1, they will not score this unless they subsequently reach a final answer of 21. Allow for N or n.

Accept versions of 
$$n \dots \frac{\log\left(\frac{4}{3}\right)}{\log(1.015)} + 1 = (20.3)$$
 or  $n \dots \log_{1.015}\left(\frac{4}{3}\right) + 1 = (20.3)$  or  
 $n \dots \frac{\log(1.33)}{\log(1.015)} + 1 = (20.15)$   
A1  $(N) = 21$  Do not accept  $N > 21$  etc  
The two final A marks may be implied by finding 'n' and adding 1 to reach 21

#### Summer 2017

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Past Paper (Mark Scheme) This resource was created and owned by Pearson Edexcel So trial and improvement above and below

M1 Attempts 
$$(U_{20}) = 6000 \times (1.015)^{19}$$
 or  $(U_{21}) = 6000 \times (1.015)^{20}$ 

A1 Achieves either 
$$(U_{20}) = \text{awrt } 7960 \text{ or } (U_{21}) = \text{awrt } 8080$$

M1 Attempts 
$$(U_{20}) = 6000 \times (1.015)^{19}$$
 and  $(U_{21}) = 6000 \times (1.015)^{20}$ 

- A1 Achieves both  $(U_{20}) = awrt 7960 and (U_{21}) = awrt 8080$
- A1 States (N) = 21

Candidate uses a "solve" option on a calculator. M1  $6000 \times 1.015^{N-1} = 8000$  M1 A1 A1 (N) = 20.3 (to 1 dp at least) A1 states 21

Candidates can attempt to write down 20 terms which would follow the same scheme as trial and improvement

(c)

- M1 Attempts  $S_n = \frac{a(1-r^n)}{(1-r)}$  with n = 10 a = 6000/30000 and r = 1.015/1+1.5%/1.15/1.0015Alternatively accept a list of ten terms starting with £30 000, £30450, £30906.75, ... added Or £6000, £6090, £6181.35,....added
- A1 A correct unsimplified answer to the **cost** for 10 years Accept either  $S = 5 \times \frac{6000(1.015^{10} - 1)}{(1.015 - 1)}$  OR  $S = \frac{30000(1.015^{10} - 1)}{(1.015 - 1)}$
- A1 cso awrt (£) 321 000

# Mathematics C12

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Past Paper



Figure 4 shows a sketch of part of the curve C with equation

$$y = x^3 - 9x^2 + 26x - 18$$

The point P(4, 6) lies on C.

(a) Use calculus to show that the normal to C at the point P has equation

$$2y + x = 16$$

The region R, shown shaded in Figure 4, is bounded by the curve C, the x-axis and the normal to C at P.

(b) Show that C cuts the x-axis at (1, 0)

(c) Showing all your working, use calculus to find the exact area of R.

(Solutions based entirely on graphical or numerical methods are not acceptable.)



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(5)

(1)

(6)

Sun Past I	<b>hmer 2017</b> Paper (Mark S	www.mystudybro.comMathScheme)This resource was created and owned by Pearson Edexcel	ematics C	<b>C12</b> IA01
	Question Number	Scheme	Marks	
	12(a)	$y = x^{3} - 9x^{2} + 26x - 18 \Longrightarrow \frac{dy}{dx} = 3x^{2} - 18x + 26$	M1A1	
		At $x = 4 \implies \frac{dy}{dx} = 3 \times 4^2 - 18 \times 4 + 26 (= 2)$	M1	
		Equation of normal is $y-6 = -\frac{1}{2}(x-4) \Longrightarrow 2y + x = 16$	dM1A1*	
			D1*	(5)
	(b)	Sub $x = 1$ in $(y) = 1 - 9 + 26 - 18 = 0$	DI	(1)
	(c)	$\int x^{3} - 9x^{2} + 26x - 18dx = \left[\frac{1}{4}x^{4} - 3x^{3} + 13x^{2} - 18x\right]$	M1A1	
		Normal meets x axis at $x = 16$	B1	
		Area of triangle = $\frac{1}{2} \times (16 - 4) \times 6 = (36)$	M1	
		Correct method for area = $\left[\frac{1}{4}x^4 - 3x^3 + 13x^2 - 18x\right]_1^4 + \frac{1}{2} \times (16 - 4) \times 6$	dM1	
		= 51.75	A1	
			(12 ma)	(6) rks)

(a)

M1 Two of the three terms correct (may be unsimplified).

A1 
$$\left(\frac{dy}{dx}\right) = 3x^2 - 18x + 26$$
, need not be simplified. You may not see the  $\frac{dy}{dx}$ 

M1 Substitutes x = 4 into their  $\frac{dy}{dx}$ 

dM1 The candidate must have scored both M's. It is for the correct method of finding the equation of a normal. Look for  $y-6 = -\frac{dx}{dy}\Big|_{x=4} \times (x-4)$ 

If the form y = mx + c is used it is for proceeding as far as c = ...

A1\* cso 2y + x = 16 Note that this is a given answer. x + 2y = 16 is ok

(b)  
B1\* Either substitute 
$$x = 1$$
 in  $(y) = 1^3 - 9 \times 1^2 + 26 \times 1 - 18 = 0$  or  $(y) = 1 - 9 + 26 - 18 = 0$ 

Or substitute y = 0 reach  $(x-1)(x^2-8x+18)$  by inspection or division and state x = 1

#### Summer 2017

A1

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Past Paper (Mark Scheme) This resource was created and owned by Pearson Edexcel To mark consistently decide on the method first

## (c) Way One: Finding area under curve C

- M1 Integrates  $x^3 9x^2 + 26x 18$  with at least two terms correct (unsimplified)
- A1  $\int x^3 9x^2 + 26x 18dx = \left[\frac{1}{4}x^4 3x^3 + 13x^2 18x\right]$  or equivalent. May be unsimplified
- B1 For sight of the normal meeting the *x* axis at 16. May be embedded within a formula or on the diagram

M1 For correct method for the area of the triangle. Either  $\frac{1}{2} \times ('16'-4) \times 6$  or correct integration with

limits of 4 to their 16  $\left[8x - \frac{1}{4}x^2\right]_{x=4}^{x=16^{\circ}}$ 

dM1 Dependent upon the candidate having scored both M's. It is a fully correct method of finding the area of R. The limits of the integral(s) must be correct

Correct method for area = 
$$\left[ \left[ \frac{1}{4} x^4 - 3x^3 + 13x^2 - 18x' \right]_1^4 + \frac{1}{2} \times (16' - 4) \times 6 \right]$$
  
cso 51.75 oe such as  $\frac{207}{4}$ 

.....

Alternatives in part (c). In some cases candidates may try to find the area between the line and the curve. If you see an attempt where this occurs score as follows.

#### Way Two: Finding area between line and curve

- M1 Integrates their  $\left(8 \frac{1}{2}x\right) \left(x^3 9x^2 + 26x 18\right)$  either way around with at least two terms correct (unsimplified). Condone slips on the straight line (eg 8 x, 16 x or on the subtraction)
- A1 Completely correct integration of their expression either way around  $\pm \left\{ \left( 8x \frac{1}{4}x^2 \right) \left( \frac{1}{4}x^4 3x^3 + 13x^2 18x \right) \right\}$

You may follow through on their equation of the line or on their combined expression of line and curve. This A1 is for correct integration following the award of the M mark.

- B1 For sight of the normal meeting the *x* axis at 16. May be implied within a triangle formula of from the diagram
- M1 For correct method for the area of the large triangle. The base length of the triangle is (their 16 -1). The height of the triangle must be an attempt to find the *y* value on the normal at x=1

Either by 
$$\frac{1}{2} \times ('16'-1) \times y_{_{NORM at x=1}} = \left(\frac{1}{2} \times ('16'-1) \times '7.5' = (56.25)\right)$$
 or by correct integration with limits of 1 to their 16  $\left[8x - \frac{1}{4}x^2\right]_{x=1}^{x='16'}$ 

dM1 Dependent upon the candidate having scored both M's. It is a fully correct method of finding the area of R. The limits of the integral(s) must be correct

Correct method for area = 
$$\frac{1}{2} \times ('16'-1) \times '7.5' - \left[ \left[ \left( 8x - \frac{1}{4}x^2 \right) - \left( \frac{1}{4}x^4 - 3x^3 + 13x^2 - 18x \right) \right]_1^4 \right]_1^4$$

A1 cso 51.75

mmer 20	17 www.mystudybro.com This resource was created and owned by Pearson Edexcel	
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<b>13.</b> (a)	Show that the equation	blan
	$5\cos x + 1 = \sin x \tan x$	
	can be written in the form	
	$6\cos^2 x + \cos x - 1 = 0$	(4)
(b)	Hence solve, for $0 \le \theta < 180^{\circ}$	
	$5\cos 2\theta + 1 = \sin 2\theta \tan 2\theta$	
	giving your answers, where appropriate, to one decimal place.	
(Sol	lutions based entirely on graphical or numerical methods are not acceptable	le.) (6)

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Summer 2017	www.mystudybro.com	Math
Past Paper (Mark Scheme)	This resource was created and owned by Pearson Edexcel	

Mathemat	ics	C12
	W	MA01

Question	Scheme	Marks
Number		
13(a)	$5\cos x + 1 = \sin x \tan x \Rightarrow 5\cos x + 1 = \sin x \times \frac{\sin x}{\cos x}$	M1
	$5\cos^2 x + \cos x = \sin^2 x$	A1
	$5\cos^2 x + \cos x = 1 - \cos^2 x$	M1
	$6\cos^2 x + \cos x - 1 = 0$	A1*
		(4)
<b>(b)</b>	$6\cos^2 k + \cos k - 1 = 0 \Longrightarrow (3\cos k - 1)(2\cos k + 1) = 0$	M1
	$\Rightarrow \cos k = \frac{1}{3}, -\frac{1}{2}$	A1
	Either $\cos 2\theta = \frac{1}{3} \Rightarrow 2\theta = 70.53, 289.47$ Or $\cos 2\theta = -\frac{1}{2} \Rightarrow 2\theta = 120, 240$	
	$\Rightarrow \theta = 35.3^{\circ}, 144.7^{\circ}, 60^{\circ}, 120^{\circ}$	M1A1M1A1
		(6)
		(10 marks)

(a)

M1 Uses  $\tan x = \frac{\sin x}{\cos x}$  in the given equation. You may see it used in the form  $\tan x \cos x = \sin x$ 

- A1 A correct equation (not involving fractions) in both sin and cos. Eg  $5\cos^2 x + \cos x = \sin^2 x$  oe
- M1 Replaces  $\sin^2 x$  by  $1 \cos^2 x$  to produce a quadratic equation/expression in just  $\cos x$

A1\* Proceeds correctly to the given answer  $6\cos^2 x + \cos x - 1 = 0$ All notation should be consistent and correct including  $\cos x$  instead of  $\cos x$  and  $\sin^2 x$  instead of  $\sin x^2$ 

#### Summer 2017

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Past Paper (Mark Scheme) (b)

> M1 Attempts to factorise and solve expression of the form  $6\cos^2 k + \cos k - 1 = 0$ Accept use of formula or GC They may solve  $6y^2 + y - 1 = 0$  which is fine

A1 Correct answers for quadratic Accept  $\cos k = \frac{1}{3}, -\frac{1}{2}$  with  $k = \theta$  or  $2\theta$  or x or even  $y = \frac{1}{3}, -\frac{1}{2}$ 

M1 Correct order of operations to produce at least one value for  $\theta$  in the range  $0 \rightarrow 360^{\circ}$ 

Look for 
$$\cos 2\theta = \frac{1}{3} \Rightarrow \theta = \frac{\arccos\left(\frac{1}{3}\right)}{2}$$
 or  $\cos 2\theta = \frac{1}{2} \Rightarrow \theta = \frac{180 - \arccos\left(\frac{1}{2}\right)}{2}$ 

- A1 Two of  $\theta$  = awrt 35.3°, 144.7°, 60°, 120° Any of these values would imply M1
- M1 Correct order of operations to produce at least one other value for  $\theta$  in the range  $0 \rightarrow 180^{\circ}$  from their principal value

Look for 
$$\cos 2\theta = \frac{1}{3} \Rightarrow \theta = \frac{360 - \arccos\left(\frac{1}{3}\right)}{2}$$
 or  $\cos 2\theta = \frac{1}{2} \Rightarrow \theta = \frac{180 + \arccos\left(\frac{1}{2}\right)}{2}$ 

A1 All four of  $\theta = \text{awrt } 35.3^\circ, 144.7^\circ, 60^\circ, 120^\circ \text{ with no additional solutions in the range.}$ If the answers are given in radians 0.615, 2.526,  $\frac{\pi}{3}(1.047), \frac{2\pi}{3}(2.094)$  just withhold the final A1

Special Case 1: If candidates solve part (b) giving values for  $2\theta$  (perhaps mistakenly thinking that the question was  $6\cos^2\theta + \cos\theta - 1 = 0$ ) then you may award special case 1 1 1 0 0 0 for sight of both solutions ( $\theta$ ) = awrt 70.5°, 120° in the range  $0 \rightarrow 180^\circ$ 





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<b>mmer</b> t Paper (	2017 (Mark S	www.mystudybro.com         Ma           Scheme)         This resource was created and owned by Pearson Edexcel	thematics C12 WMA01
Que Nur	stion nber	Scheme	Marks
14	(a)	$\left(\frac{1+7}{2},\frac{4+8}{2}\right) = (4,6)$	M1A1
			(2)
	( <b>b</b> )	$\frac{\sqrt{(7-1)^2 + (8-4)^2}}{2} \text{ Or } \sqrt{(4'-1)^2 + (6'-4)^2} \text{ Or } \sqrt{(7-4')^2 + (8-6')^2}$	M1
		(Radius of circle) = $\sqrt{13}$	A1
(	c)	Equation of C <sub>2</sub> is $x^2 + y^2 = r^2$	(2) M1
		Attempts either value of r as $(\sqrt{4'^2 + 6'^2} \pm \text{their } r)$	M1
		When $r = \sqrt{52} - \sqrt{13} = \sqrt{13} \implies x^2 + y^2 = 13$	A1
		When $r = \sqrt{52} + \sqrt{13} = 3\sqrt{13} \implies x^2 + y^2 = 117$	A1
			(4) (8marks)
A1 (b) M1	(4, 6) Scor an at	i). No working is required, Correct answer scores both marks. Condone lack ed for using Pythagoras' theorem to find the distance between their centre and tempt at $\sqrt{('4'-1)^2 + ('6'-4)^2}$ or similar. If the original coordinates are used	of brackets d a point. Look fo l then there must
A1	be so $=\sqrt{1}$	Correct answer scores both marks	
(c)	<b>D</b>	$f(x) = \frac{1}{2} \int \frac{1}{2} 1$	1
IVI I	alget	braic 'r' Accept $x^2 + y^2 = k$ If a value of k is given then k must be positive	
M1	Atte	mpts either value of r Look for $\left(\sqrt{4'^2+6'^2} \pm \text{their } r\right)$ Accept $r = \frac{\sqrt{4^2+6^2}}{2}$	_
A1	Eithe	er of $x^2 + y^2 = 13$ or $x^2 + y^2 = 117$	
	Allo	w for this mark variations like $(x-0)^2 + (y-0)^2 = \sqrt{13}^2$	
A1	Both Any	of $x^2 + y^2 = 13$ and $x^2 + y^2 = 117$ . Equations must be simplified as seen he one correct equation will imply the first two M's.	re
Alt me	ethod 1	to find equations using the intersections:	

- M1: As above
- Solves 'their'  $y = \left|\frac{3}{2}\right| x$  with their  $(x 4')^2 + (y 6')^2 = 13' \Rightarrow$  Intersections (2,3) and (6,9) So this time the method is scored for either  $\sqrt{2'^2 + 3'^2}$  or  $\sqrt{6'^2 + 9'^2}$ M1:

A1 A1 as before

**Mathematics C12** www.mystudybro.com WMA01 This resource was created and owned by Pearson Edexcel Leave blank 15. The height of water, H metres, in a harbour on a particular day is given by the equation  $H = 4 + 1.5\sin\left(\frac{\pi t}{6}\right),$  $0 \leqslant t < 24$ where t is the number of hours after midnight, and  $\frac{\pi t}{6}$  is measured in radians. (a) Show that the height of the water at 1 a.m. is 4.75 metres. (1) (b) Find the height of the water at 2 p.m. (2) (c) Find, to the nearest minute, the first two times when the height of the water is 3 metres. (Solutions based entirely on graphical or numerical methods are not acceptable.) (6)

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#### Summer 2017 Past Paper (Mark Scheme)

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WMA01

Question Number	Scheme	Marks
15 (a)	$t = 1 \Longrightarrow H = 4 + 1.5 \sin\left(\frac{\pi}{6}\right) = 4.75(m)$	B1*
(b)	$t = 14 \Rightarrow H = 4 + 1.5 \sin\left(\frac{14\pi}{6}\right) = \text{awrt } 5.3(\text{m})$	(1) M1A1 (2)
( <b>c</b> )	$H = 3 \Longrightarrow 3 = 4 + 1.5 \sin\left(\frac{\pi t}{6}\right)$	
	$\Rightarrow \sin\left(\frac{\pi t}{6}\right) = -\frac{2}{3}$	M1 A1
	$\Rightarrow \sin\left(\frac{\pi t}{6}\right) = -\frac{2}{3} \Rightarrow t = \frac{6 \times \left(\pi + \arcsin\left(\frac{2}{3}\right)\right)}{\pi} = \text{awrt } 7.4$	M1A1
	And $\Rightarrow t = \frac{6 \times \left(2\pi - \arcsin\left(\frac{2}{3}\right)\right)}{\pi} = \text{awrt } 10.6$	M1
	Times are /:23//:24 am and 10:36/10:37 am	(6) (9 marks)

(a)

B1\* This is a given answer. Score for sight of  $(H =) 4 + 1.5 \sin\left(\frac{\pi}{6}\right) = 4.75(m)$ Alternatively they can work backwards with  $H = 4.75 \Rightarrow \frac{\pi t}{6} = \frac{\pi}{6} \Rightarrow t = 1 \Rightarrow$  Hence (time) = 1a.m

(b)

M1 For substituting t = 14 into H and an attempt to calculate. Score for  $4+1.5\sin\left(\frac{14\pi}{6}\right) = ..$ 

A1 awrt 5.3 (m) or  $\frac{16+3\sqrt{3}}{4}$  m following correct work.

 $4+1.5\sin\left(\frac{2\pi}{6}\right) = 5.30 \,(\text{m}) \text{ is M0A0 unless there is an explanation that states that the period is 12 hours so}$  $4+1.5\sin\left(\frac{2\pi}{6}\right) = 4+1.5\sin\left(\frac{14\pi}{6}\right)$ 

(c)

M1 For substituting 
$$H = 3$$
 into  $H = 4 + 1.5 \sin\left(\frac{\pi t}{6}\right)$  WITH some attempt to make  $\sin\left(\frac{\pi t}{6}\right)$  the subject

You may see the  $\left(\frac{\pi t}{6}\right)$  being replaced by another variable which is fine for the first two marks

A1 
$$\sin\left(\frac{\pi t}{6}\right) = -\frac{2}{3}$$
 oe Condone awrt  $\sin\left(\frac{\pi t}{6}\right) = -0.67$ 

M1 For a correct attempt to find **one of the first two positive** values of *t* using **their** '-0.67'.

So for 
$$\sin\left(\frac{\pi t}{6}\right) = -\frac{2}{3}$$
 score for either  $t = \frac{6 \times \left(2\pi - \arcsin\left(\frac{2}{3}\right)\right)}{\pi}$  or  $\frac{6 \times \left(\pi + \arcsin\left(\frac{2}{3}\right)\right)}{\pi}$ 

For 
$$\sin\left(\frac{\pi t}{6}\right) = \frac{2}{3}$$
 score for either  $t = \frac{6 \times \arcsin\left(\frac{\pi}{3}\right)}{\pi} = \operatorname{awrt} 1.4$  or  $\frac{6 \times \left(\pi - \arcsin\left(\frac{2}{3}\right)\right)}{\pi} = \operatorname{awrt} 4.6$ 

A relatively common answer following  $\sin\left(\frac{\pi t}{6}\right) = -\frac{2}{3}$  is t = -1.39. This scores M0 as it not one of the first two positive values for a rbs of  $\frac{2}{3}$ 

the first two positive values for a rhs of  $-\frac{2}{3}$ .

- A1 One of *t* awrt 7.4 or awrt 10.6 One of these values would probably imply the previous M mark Can be implied one correct time 7:23/7:24 am (0724) or 10:36/10:37 am (1036). Can be implied by one correct number of minutes 443/444 minutes and 636/637 minutes
- M1 For a (correct) attempt to find both of the first two positive values of *t* using their -0.67.
  A1 Times are required for this mark only Accept both 7:23/7:24 am and 10:36/10:37 am in 12 hour times Allow 0723/ 0724 and 1036/1037 in 24 hour times.
  Allow 07:23/ 07:24 and 10:36/1037 in 24 hour times 07.23/ 07.24 and 10.36/10.37 in 24 hour times. (The 0 must be present in 07.23/ 07.24 )

Some candidates may choose to do part (c) using degrees. This is fine and the scheme can be applied as long as  $\pi = 180^{\circ}$  and the candidates are consistently using degrees

M1 A1 sin(30t) = 
$$-\frac{2}{3}$$

M1 Attempts to find one value of t (but the units must be consistent)

$$\sin(30t) = -\frac{2}{3} \Longrightarrow 30t = 221.81 \text{ or } 318.19 \Longrightarrow t =$$