MyStudyBro - Revision Exercise Tool

This Revision Handout includes the Questions and Answers of a total of 5 exercises!

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Circular Measurements - C12 (Pearson Edexcel)

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(WMA01) 2017 Autumn - Answer

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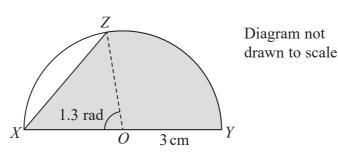


Figure 1

Figure 1 shows a semicircle with centre O and radius 3cm. XY is the diameter of this semicircle. The point Z is on the circumference such that angle XOZ = 1.3 radians. The shaded region enclosed by the chord XZ, the arc ZY and the diameter XY is a template for a badge.

Find, giving each answer to 3 significant figures,

(a) the length of the chord XZ,

(2)

(b) the perimeter of the template XZYX,

(4)

(c) the area of the template.

(4)

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Mathematics C12

Question Number	Scheme	Marks
10. (a)	$XZ^2 = 3^2 + 3^2 - 2 \times 3 \times 3\cos 1.3$, or $\sin 0.65 = \frac{x}{3}$ so $XZ = 2 \times x$	M1
	XZ = 3.63	A1 [2]
(b)	Arc length $ZY = 3 \times \theta$,= 3 × (π – 1.3) (= 5.52 / 5.53)	M1, A1
	Perimeter = $3 + 3 + \operatorname{arc} ZY + \operatorname{chord} XZ = 15.2 \text{ (cm)}$	dM1 A1 [4]
(c)	Area of triangle $OXZ = \frac{1}{2} \times 3 \times 3 \times \sin 1.3$ (=4.34)	M1
	Area of sector is $\frac{1}{2}r^2\theta = \frac{1}{2} \times 3^2 \times (\pi - 1.3)$ (= 8.28 / 8.29)	M1
	Total area is $\frac{1}{2} \times 3^2 \times (\pi - 1.3) + \frac{1}{2} \times 3 \times 3 \times \sin 1.3$	
		dM1
	$= 12.6 \text{ (cm}^2)$	A1
		[4]
		10 marks
	Notes	

(a)

M1: Uses cosine rule – must be correct. Allow $XZ^2 = 3^2 + 3^2 - 2 \times 3 \times 3 \cos 1.3$, for the M1 Or splits into right angled triangles correctly, uses sin 0.65 and then doubles the result

Uses angles in a triangle rule with the sine rule to find the required side. Eg $\frac{x}{\sin 1.3} = \frac{3}{\sin 0.92}$

awrt 3.63 A1:

(b)

M1: Arc length formula $r \theta$ with r = 3 and $\theta = 1.3$, $(\pi - 1.3)$ or $(2\pi - 1.3)$ If decimals are seen accept 1.8 or 5.0 If the degree formula is being used look for $\frac{\theta}{360} \times 2\pi r$ with $\theta = 74^{\circ} - 75^{\circ}$ or $\theta = 105^{\circ} - 106^{\circ}$

A1: Uses arc length formula with a correct angle. It does not need to be processed

Allow $3(\pi-1.3)$, 3×1.84 , awrt 5.52/5.53 In degrees look for the minimum accuracy of $\frac{105.5}{360}\times2\pi\times3$

dM1: Complete method for perimeter. It is dependent upon the previous M. Look for 6+(a)+ arc length

A1: awrt15.2 (cm) – you do not need to see units

(c)

M1: Uses area formula for triangle correctly. If $\frac{1}{2}bh$ is used it must be the correct combinations found using a correct method.

M1: Uses the formula $\frac{1}{2}r^2\theta$ to find the area of the correct sector. There must be some valid attempt to use the correct angle. Allow as a minimum awrt 1.8 radians (3.1-1.3)

dM1: Adds two correct area formulae together. Both M's must have been awarded

A1: Accept awrt 12.6 (do not need units)

Alt (c)

M1: Attempts to find the area of the segment $\frac{1}{2} \times 3^2 (1.3 - \sin 1.3)$

M1: Attempts area of semi circle along with the area of segment

dM1: Finds area of the semi circle - segment $\frac{\pi \times 3^2}{2} - \frac{1}{2} \times 3^2 (1.3 - \sin 1.3)$

A1: awrt 12.6

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15.

0.8 radians

Figure 2

Figure 2 shows a plan for a garden.

The garden consists of two identical rectangles of width y m and length x m, joined to a sector of a circle with radius x m and angle 0.8 radians, as shown in Figure 2.

The area of the garden is 60 m².

(a) Show that the perimeter, P m, of the garden is given by

$$P = 2x + \frac{120}{x}$$
 (5)

(b) Use calculus to find the exact minimum value for P, giving your answer in the form $a\sqrt{b}$, where a and b are integers.

(4)

(c) Justify that the value of *P* found in part (b) is the minimum.

(2)

Autumn 2018

Mathematics C12

Past Paper (Mark Scheme)

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WMA01

Question Number	Scheme	Notes	Marks
15(a)	(Arc length =) 0.8x	Correct expression	B1
	P = 2x + 4y + 0.8x	$P = \alpha x + \beta y + "0.8x", \alpha, \beta \neq 0$	M1
	This may be implied by e.g. P	y = 2x + 4 (their y) + 0.8x	
	$2xy + \frac{1}{2}(0.8)x^2 = 60$	Correct equation for the area	B1
	$y = \frac{60 - 0.4x^2}{2x} \Rightarrow P = 4\left(\frac{60 - 0.4x^2}{2x}\right) + 2.8x$	Makes <i>y</i> the subject and substitutes	M1
	$P = \frac{120}{x} + 2x^*$	Obtains printed answer with no errors with $P =$ or Perimeter = appearing at some point.	A1*
	Note that it is sufficient to go from $P = 4$	$\left(\frac{60-0.4x^2}{2x}\right) + 2.8x \text{ to } P = \frac{120}{x} + 2x^*$	
			(5)

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WMA01

15(b)	Mark (b) and (c) t		
	Allow e.g. $\frac{dy}{dx}$ for $\frac{dP}{dx}$ and/o	For $\frac{d^2y}{dx^2}$ for $\frac{d^2P}{dx^2}$	
	$\frac{\mathrm{d}P}{\mathrm{d}x} = 2 - \frac{120}{x^2}$	Correct derivative	B1
	$2 - \frac{120}{x^2} = 0 \Rightarrow x = \sqrt{60}$	$\frac{dP}{dx} = 0$ and solves for x. Must be fully correct algebra for their $\frac{dP}{dx} = 0$ which is solvable.	M1
	$P = \frac{120}{\sqrt{60}} + 2\sqrt{60}$ h	Substitutes into P , a positive x which has come from an attempt to solve heir $\frac{dP}{dx} = 0$	M1
	, , , , , , , , , , , , , , , , , , ,	Correct exact answer. Cso.	A1
	Note that if $\frac{dP}{dx} = 2 + \frac{120}{x^2}$ is obtained, this could	d score a maximum of B0M0M1A0	
	if a positive value of x is su		(1)
(c)			(4)
	$\left(\frac{d^{2}P}{dx^{2}}\right) = \frac{240}{x^{3}} = \frac{240}{\left(\sqrt{60}\right)^{3}}$	Attempts the second derivative $x^n \to x^{n-1}$ seen at least once allow $k \to 0$ as evidence) and then ubstitutes at least one positive value of x from their $\frac{dP}{dx} = 0$ or makes eference to the sign of the second derivative provided they have a positive x .	M1
	$\left(\frac{d^2P}{dx^2}\right) = \frac{240}{\left(\sqrt{60}\right)^3} \Rightarrow \frac{d^2P}{dx^2} > $	and the correct value of x . In of the second derivative. Correctly allow this mark if the other met. $\frac{P}{2}$ being positive must also include a tax is positive.	A1
	Allow alternation e.g. considers values of P either dP	ther side of $\sqrt{60}$ or	
	values of $\frac{dP}{dx}$ either side of $\frac{dP}{dx}$		
	and then A1 if a full reason and	i conclusion is given.	(2)
			Total 11

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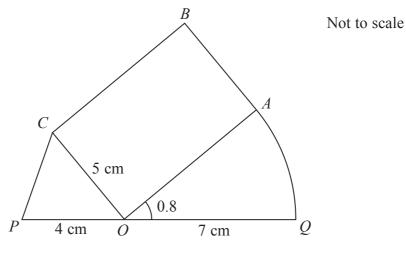


Figure 1

The shape *POQABCP*, as shown in Figure 1, consists of a triangle *POC*, a sector *OQA* of a circle with radius 7 cm and centre O, joined to a rectangle OABC.

The points P, O and Q lie on a straight line.

PO = 4 cm, CO = 5 cm and angle AOQ = 0.8 radians.

(a) Find the length of arc AQ.

(2)

(b) Find the size of angle *POC* in radians, giving your answer to 3 decimal places.

(2)

(c) Find the perimeter of the shape *POOABCP*, in cm, giving your answer to 2 decimal places.

(4)



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Paper (Mark 3	Triis resource was created at	na emied sy'r eareen Edexee.	VVIVIAUT
Question Number	Sch	eme	Marks
3(a)	$S = r\theta = 7 \times 0.8 = 5.6$ (cm)	M1: Uses $S = r\theta$ A1: 5.6 oe e.g. 28/5	M1A1
	Note that if the 0.8 is converted to	degrees e.g. $0.8 \times \frac{180}{\pi} = 45.8366$,	
		or truncated when attempting	
	$\frac{45.8366}{360} \times 2 \times \pi \times 7 \text{ for the}$	M1 so allow A1 for awrt 5.6	
			(2)
(b)		M1: Attempts to find $\frac{\pi}{2}$ – 0.8 or	
	$\angle POC = \frac{\pi}{2} - 0.8 = \text{awrt } 0.771$	$\pi - \frac{\pi}{2} - 0.8$. Allow an attempt to	M1A1
	2 0.0 - awit 0.771	find θ from $\theta + \frac{\pi}{2} + 0.8 = \pi$.	1411711
		Accept as evidence awrt 0.77	
		A1: awrt 0.771	
		only can score M1A0	
	e.g. 180-90-0.8	$\times \frac{160}{\pi} (= 44.163)$	
			(2)
(c)	$4^{2} + 5^{2} - 2 \times 4 \times 5 \cos'(0.771')$ or $\sqrt{4^{2} + 5^{2} - 2 \times 4 \times 5 \cos'(0.771')}$	Correct use of the cosine rule to find CP or CP^2 . NB 0.771 radians is awrt 44 degrees. Ignore lhs for this mark and look for e.g. $4^2 + 5^2 - 2 \times 4 \times 5 \cos' 0.771$ or 44'	M1
	$CP^{2} = 4^{2} + 5^{2} - 2 \times 4 \times 5 \cos 0.771$ or $CP = \sqrt{4^{2} + 5^{2} - 2 \times 4 \times 5 \cos 0.771}$	A correct expression for <i>CP</i> or <i>CP</i> ² with lhs consistent with rhs. Allow awrt 0.77 radians or awrt 44 degrees. (May be implied if a correct numerical value is used in	A1
	Perimeter = $4+5+2\times7+'5.6'+'3.5'$	subsequent work) $4+5+2\times7+$ their $AQ+$ their CP . Need to see all 6 lengths but may be implied by e.g. $23+'5.6'+'3.5'$	M1
	= 32.11 (cm)	Awrt 32.11 (ignore units)	A1
		(-0	(4)
			(8 marks)

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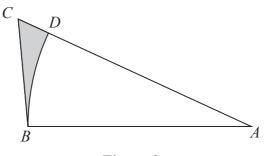


Figure 2

Figure 2 shows a sketch of a design for a triangular garden ABC.

The garden has sides BA with length 10 m, BC with length 6 m and CA with length 12 m.

The point D lies on AC such that BD is an arc of the circle centre A, radius 10 m.

A flowerbed *BCD* is shown shaded in Figure 2.

(a) Find the size of angle BAC, in radians, to 4 decimal places.

(2)

(b) Find the perimeter of the flowerbed *BCD*, in m, to 2 decimal places.

(3)

(c) Find the area of the flowerbed BCD, in m^2 , to 2 decimal places.

(4)



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Mathematics C12

Past Paper (Mark Scheme)

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٧v	/M	ΑC)1

Question Number	Scheme	Marks
6(a)	$\cos \angle BAC = \frac{12^2 + 10^2 - 6^2}{2 \times 12 \times 10} \Rightarrow \angle BAC = 0.5223$	M1A1
(b)	Arc $BD = r\theta = 10 \times 0.5223$ Perimeter = 6+2+ 10×0.5223=13.22 (m)	(2) M1 dM1,A1 (3)
(c)	Area of sector $BAD = \frac{1}{2}r^2\theta = \frac{1}{2} \times 10^2 \times 0.5223$ (= 26.116)	M1
	Area of triangle $ABC \frac{1}{2} ab \sin C = \frac{1}{2} \times 12 \times 10 \times \sin 0.5223$ (= 29.932) Area of flowerbed $BCD = \frac{1}{2} \times 12 \times 10 \times \sin 0.5223 - \frac{1}{2} \times 10^2 \times 0.5223$	M1 dM1
	$= 3.81 / 3.82 \text{ (m}^2\text{)}$	A1 (4) (9 marks)

(a)

- M1 Attempts use of the formula $6^2 = 10^2 + 12^2 2 \times 10 \times 12 \cos A$ or $\cos \angle BAC = \frac{12^2 + 10^2 6^2}{2 \times 12 \times 10}$ The sides must be in the correct "position" within the formula. Condone different notation Eg. θ
- A1 $\angle BAC = \text{awrt } 0.5223$

The angle in degrees (awrt 29.9°) is A0

(b)

- M1 Attempts arc formula: In radians uses Arc $BD = r\theta = 10 \times "0.5223"$ In degrees uses Arc $BD = \frac{\theta}{360} \times 2\pi r = \frac{"29.9"}{360} \times 2\pi \times 10$
- dM1 Dependent upon the arc formula having been used. It is for calculating the perimeter as 8 + arc length.
- A1 Perimeter = awrt 13.22(m)

(c)

- M1 Attempts area of sector formula: Area of sector $BAD = \frac{1}{2}r^2\theta = \frac{1}{2}\times10^2\times"0.5223"$ In degrees uses Area of sector $BAD = \frac{\theta}{360}\times\pi r^2 = \frac{"29.9"}{360}\times\pi\times10^2$
- Attempts area of triangle formula: Area of triangle $ABC = \frac{1}{2}ab\sin C = \frac{1}{2} \times 12 \times 10 \times \sin^{\circ} 0.5223^{\circ}$ You may see Herons formula used with $S = \frac{10+6+12}{2} = (14)$ and $A = \sqrt{S(S-10)(S-6)(S-12)}$ Watch for other methods including the calculation of a perpendicular.
- dM1 Dependent upon both correct formulae. It is scored for finding area of triangle area of sector A1 Allow awrt 3.81 or 3.82 (m²)

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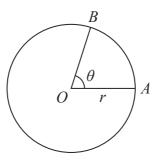


Figure 3

Figure 3 shows a circle with centre O and radius r cm.

The points A and B lie on the circumference of this circle.

The minor arc AB subtends an angle θ radians at O, as shown in Figure 3.

Given the length of minor arc AB is 6 cm and the area of minor sector OAB is $20 \, \text{cm}^2$,

(a) write down two different equations in r and θ .

(2)

(b) Hence find the value of r and the value of θ .

(4)



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Mathematics C1

WMA01

Question Number	Scheme	Marks
8.(a)	$r\theta = 6$ and $\frac{1}{2}r^2\theta = 20$	B1 B1
		[2]
(b)	Substitute $r\theta = 6$ into $\frac{1}{2}r^2\theta = 20 \Rightarrow \frac{1}{2} \times 6r = 20$	M1
	$\Rightarrow r = \frac{20}{3}$	A1
	Substitutes $r = \frac{20}{3}$ in $r\theta = 6 \Rightarrow \theta = \frac{9}{10}$	dM1A1
		[4]
		(6 marks)

This may be marked as one complete question. Eg they may just give the equations $s = r\theta$ and $A = \frac{1}{2}r^2\theta$ in (a) Don't penalise this sort of error.

(a)

B1 Either
$$r\theta = 6$$
 or $\frac{1}{2}r^2\theta = 20$ (or exact equivalents)
Allow $\frac{\theta}{2\pi} \times 2\pi r = 6$ or $\frac{\theta}{2\pi} \times \pi r^2 = 20$ but not $\frac{\theta}{360} \times 2\pi r = 6$ or $\frac{\theta}{360} \times \pi r^2 = 20$

Both $r\theta = 6$ and $\frac{1}{2}r^2\theta = 20$ (or exact equivalents) **B**1 Allow $\frac{\theta}{2\pi} \times 2\pi r = 6$ and $\frac{\theta}{2\pi} \times \pi r^2 = 20$ but not $\frac{\theta}{360} \times 2\pi r = 6$ and $\frac{\theta}{360} \times \pi r^2 = 20$

(b)

M1Combines two equations in r and θ producing an equation in one unknown.

 $r = \frac{20}{3}$ or $\theta = \frac{9}{10}$ or exact equivalents. A₁

You may just see answers following correct equations. This is fine for all the marks

This is dependent upon having started with two equations with correct expressions in r and θ dM1 Look for $..r\theta = ...$ and $..r^2\theta = ...$.

It is awarded for correctly substituting their value of r or θ into one of the equations to find the second unknown.

 $r = \frac{20}{3}$ and $\theta = \frac{9}{10}$ or exact equivalents. Condone 6.6 for $\frac{20}{3}$ Do not allow 6.67 **A**1