MyStudyBro - Revision Exercise Tool

This Revision Handout includes the Questions and Answers of a total of 5 exercises!

Chapters:

Circular Measurements - C12 (Pearson Edexcel)

Page 1	(WMA01) 2018 Summer
Page 2	(WMA01) 2018 Summer - Answer
Page 3	(WMA01) 2018 Autumn Differentiation
Page 4	(WMA01) 2018 Autumn - Answer Also Includes: Differentiation
Page 6	(WMA01) 2017 Winter
Page 7	(WMA01) 2017 Winter - Answer
Page 8	(WMA01) 2017 Summer Trigonometry
Page 9	(WMA01) 2017 Summer - Answer Also Includes: Trigonometry
Page 10	(WMA01) 2017 Autumn
Page 11	(WMA01) 2017 Autumn - Answer



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Question	Scheme	Marks	
Number	222		
10. (a)	$XZ^{2} = 3^{2} + 3^{2} - 2 \times 3 \times 3\cos 1.3$, or $\sin 0.65 = \frac{1}{3}$ so $XZ = 2 \times x$	M1	
	XZ = 3.63	A1 [2]	
(b)	Arc length $ZY = 3 \times \theta$, = 3 × (π – 1.3) (= 5.52 / 5.53)	M1, A1	
	Perimeter = $3 + 3 + \operatorname{arc} ZY + \operatorname{chord} XZ = 15.2 \text{ (cm)}$	dM1 A1 [4]	
(c)	Area of triangle $OXZ = \frac{1}{2} \times 3 \times 3 \times \sin 1.3$ (=4.34)	M1	
	Area of sector is $\frac{1}{2}r^2\theta = \frac{1}{2} \times 3^2 \times (\pi - 1.3)$ (= 8.28 / 8.29)	M1	
	Total area is $\frac{1}{2} \times 3^2 \times (\pi - 1.3) + \frac{1}{2} \times 3 \times 3 \times \sin 1.3$	dM1	
	$= 12.6 \text{ (cm}^2)$	A1	
		[4]	
	Notes	10 11111 KS	
M1: Uses Or sj	cosine rule – must be correct. Allow $XZ^2 = 3^2 + 3^2 - 2 \times 3 \times 3\cos 1.3$, for the M1 plits into right angled triangles correctly, uses sin 0.65 and then doubles the result		
A1: awrt (b)	3.63		
M1: Arc le	ength formula $r \theta$ with $r = 3$ and $\theta = 1.3, (\pi - 1.3)$ or $(2\pi - 1.3)$ If decimals are seen accept 1.8 or	5.0	
If the	degree formula is being used look for $\frac{\theta}{360} \times 2\pi r$ with $\theta = 74^{\circ} - 75^{\circ}$ or $\theta = 105^{\circ} - 106^{\circ}$		
A1: Uses a	rc length formula with a correct angle. It does not need to be processed		
Allow	$3(\pi - 1.3), 3 \times 1.84$, awrt 5.52/5.53 In degrees look for the minimum accuracy of $\frac{105.5}{360} \times 2\pi \times 10^{-10}$	3	
dM1: Com	plete method for perimeter. It is dependent upon the previous M. Look for $6+(a)+ \text{arc length}$		
AI: awrt1: (c)	5.2 (cm) - you do not need to see units		
M1: Uses	area formula for triangle correctly. If $\frac{1}{2}bh$ is used it must be the correct combinations found using	a correct	
method	1. 1		
M1: Uses	the formula $\frac{1}{2}r^2\theta$ to find the area of the correct sector. There must be some valid attempt to use the	e correct	
an, dM1: Add A1: Accep Alt (c)	gle. Allow as a minimum awrt 1.8 radians $(3.1-1.3)$ Is two correct area formulae together. Both M's must have been awarded of awrt 12.6 (do not need units)		
M1: Atten	npts to find the area of the segment $\frac{1}{2} \times 3^2 (1.3 - \sin 1.3)$		
M1: Atten	npts area of semi circle along with the area of segment		
dM1: Fin	dM1: Finds area of the semi circle - segment $\frac{\pi \times 3^2}{2} - \frac{1}{2} \times 3^2 (1.3 - \sin 1.3)$		
A1: awrt 1	2.6		

MSB - Page 3



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Question Number	Scheme	Notes	Marks	
15(a)	(Arc length=)0.8x Correct expression			
	P = 2x + 4y + 0.8x	$P = \alpha x + \beta y + "0.8x", \alpha, \beta \neq 0$	M1	
	This may be implied by e.g. P	P = 2x + 4 (their y) + 0.8x		
	$2xy + \frac{1}{2}(0.8)x^2 = 60$ Correct equation for the area			
	$y = \frac{60 - 0.4x^2}{2x} \Rightarrow P = 4\left(\frac{60 - 0.4x^2}{2x}\right) + 2.8x$	Makes <i>y</i> the subject and substitutes	M1	
	$P = \frac{120}{x} + 2x^*$	Obtains printed answer with no errors with $P = \dots$ or Perimeter = \dots appearing at some point.	A1*	
	Note that it is sufficient to go from $P = 4$	$\left(\frac{60-0.4x^2}{2x}\right) + 2.8x \text{ to } P = \frac{120}{x} + 2x^*$		
			(5)	

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15(b)	Mark (b) and (c) together		
	Allow e.g. $\frac{dy}{dx}$ for $\frac{dP}{dx}$ and/or $\frac{d^2y}{dx^2}$ for $\frac{d^2P}{dx^2}$		
	$\frac{\mathrm{d}P}{\mathrm{d}x} = 2 - \frac{120}{x^2}$	Correct derivative	B1
	$2 - \frac{120}{x^2} = 0 \Longrightarrow x = \sqrt{60}$	$\frac{dP}{dx} = 0 \text{ and solves for } x. \text{ Must be fully}$ correct algebra for their $\frac{dP}{dx} = 0$ which is solvable.	M1
	$P = \frac{120}{\sqrt{60}} + 2\sqrt{60}$	Substitutes into <i>P</i> , a positive <i>x</i> which has come from an attempt to solve their $\frac{dP}{dx} = 0$	M1
	$P = 4\sqrt{60}$ or $8\sqrt{15}$ or $\sqrt{960}$	Correct exact answer. Cso.	A1
	Note that if $\frac{dP}{dx} = 2 + \frac{120}{x^2}$ is obtained, this co	ould score a maximum of B0M0M1A0	
	if a positive value of x is	substituted into <i>P</i> .	
(c)			(4)
	$\left(\frac{d^2 P}{dx^2}\right) = \frac{240}{x^3} = \frac{240}{\left(\sqrt{60}\right)^3}$	Attempts the second derivative $x^n \rightarrow x^{n-1}$ seen at least once (allow $k \rightarrow 0$ as evidence) and then substitutes at least one positive value of x from their $\frac{dP}{dx} = 0$ or makes reference to the sign of the second derivative provided they have a positive x.	M1
	$\left(\frac{d^2 P}{dx^2} = \right) \frac{240}{\left(\sqrt{60}\right)^3} \Rightarrow \frac{d^2 P}{dx^2} > 0 \therefore \text{ minimum}$ Requires a correct second derivative and the correct value of <i>x</i> . There must be a reference to the sign of the second derivative. If <i>x</i> is substituted and then $\frac{d^2 P}{dx^2}$ is evaluated incorrectly allow this mark if the other conditions are met. If <i>x</i> is not substituted then the reference to $\frac{d^2 P}{dx^2}$ being positive must also include a reference to the fact that <i>x</i> is positive. Allow alternatives e.g. considers values of <i>P</i> either side of $\sqrt{60}$ or values of $\frac{dP}{t}$ either side of $\sqrt{60}$ can score M1		
	and then A1 if a full reason a	nd conclusion is given.	
			(2) Total 11

15.

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Mathematics C12

WMA01



Figure 5

Figure 5 shows the design for a logo.

The logo is in the shape of an equilateral triangle ABC of side length 2r cm, where r is a constant.

The points L, M and N are the midpoints of sides AC, AB and BC respectively.

The shaded section R, of the logo, is bounded by three curves MN, NL and LM.

The curve MN is the arc of a circle centre L, radius r cm.

The curve NL is the arc of a circle centre M, radius r cm.

The curve LM is the arc of a circle centre N, radius r cm.

Find, in cm², the area of R. Give your answer in the form kr^2 , where k is an exact constant to be determined.

(5)

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Winter 2017	www.mystudybro.com Mathe	ematics C12		
Question Number	Scheme	Marks		
15	Area of triangle = $\frac{1}{2} \times (2r)^2 \sin\left(\frac{\pi}{3} \text{ or } 60\right)$ or $\frac{1}{2} \times (r)^2 \sin\left(\frac{\pi}{3} \text{ or } 60\right)$ Correct method for the area of either triangle. Ignore any reference to which triangle they are finding the area of			
	Area of sector = $\frac{1}{2} \times r^2 \times \frac{\pi}{3}$ Use of the sector formula $\frac{1}{2}r^2\theta$ with $\theta = \frac{\pi}{3}$ which may be embedded within a segment			
	Area R = Sector + 2 Segments = $\frac{1}{2}r^2 \times \frac{\pi}{3} + 2 \times \left(\frac{1}{2}r^2 \times \frac{\pi}{3} - \frac{1}{2}r^2 \times \frac{\sqrt{3}}{2}\right)$ Area R = Triangle + 3 Segments = $\frac{1}{2}r^2 \times \frac{\sqrt{3}}{2} + 3 \times \left(\frac{1}{2}r^2 \times \frac{\pi}{3} - \frac{1}{2}r^2 \times \frac{\sqrt{3}}{2}\right)$ Area R = 3 Sectors - 2 Triangles = $3 \times \frac{1}{2}r^2 \times \frac{\pi}{3} - 2 \times \left(\frac{1}{2}r^2 \times \frac{\sqrt{3}}{2}\right)$ Area R = Big triangle - 3 White bits = $\frac{1}{2} \times (2r)^2 \frac{\sqrt{3}}{2} - 3 \times \left(\frac{1}{2}r^2 \times \frac{\sqrt{3}}{2} - \left(\frac{1}{2}r^2 \times \frac{\pi}{3} - \frac{1}{2}r^2 \times \frac{\sqrt{3}}{2}\right)\right)$ M1: A fully correct method (may be implied by a final answer of awrt 0.705r^2) A1: Correct exact expression - for this to be scored $\sin \frac{\pi}{2} = \frac{\sqrt{3}}{2}$ must be seen			
	$=\frac{1}{2}\pi r^2 - \frac{\sqrt{3}}{2}r^2 = r^2 \left(\frac{1}{2}\pi - \frac{\sqrt{3}}{2}\right)$ Cso (Allow $\frac{r^2}{2}(\pi - \sqrt{3})$ or any exact equivalent with r^2 taken out as a common factor)	A1		
		(5 marks)		



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Question Number	Scheme	Marks
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6(a)	$\cos \angle BAC = \frac{12^2 + 10^2 - 6^2}{2 \times 12 \times 10} \Longrightarrow \angle BAC = 0.5223$	M1A1
		(2)
(b)	Arc $BD = r\theta = 10 \times 0.5223$	M1
	Perimeter = $6+2+10 \times 0.5223=13.22$ (m)	dM1.A1
		(3)
(c)	Area of sector $BAD = \frac{1}{2}r^2\theta = \frac{1}{2} \times 10^2 \times 0.5223 (= 26.116)$	M1
	Area of triangle $ABC \frac{1}{2} ab \sin C = \frac{1}{2} \times 12 \times 10 \times \sin 0.5223 (= 29.932)$	M1
	Area of flowerbed $BCD = \frac{1}{2} \times 12 \times 10 \times \sin 0.5223 - \frac{1}{2} \times 10^2 \times 0.5223$	dM1
	=3.81/3.82 (m ²)	A1
		(4)
		(9 marks)

(a)

M1 Attempts use of the formula $6^2 = 10^2 + 12^2 - 2 \times 10 \times 12 \cos A$ or $\cos \angle BAC = \frac{12^2 + 10^2 - 6^2}{2 \times 12 \times 10}$ The sides must be in the correct "position" within the formula. Condone different notation Eg. θ

A1 $\angle BAC = awrt \ 0.5223$ The angle in degrees (awrt 29.9°) is A0

(b)

- M1 Attempts arc formula: In radians uses Arc $BD = r\theta = 10 \times "0.5223"$ In degrees uses Arc $BD = \frac{\theta}{360} \times 2\pi r = \frac{"29.9"}{360} \times 2\pi \times 10$
- dM1 Dependent upon the arc formula having been used. It is for calculating the perimeter as 8 + arc length.
 A1 Designator awart 12.22 (m)
- A1 Perimeter = awrt 13.22(m)
- (c)
- M1 Attempts area of sector formula: Area of sector $BAD = \frac{1}{2}r^2\theta = \frac{1}{2} \times 10^2 \times "0.5223"$ In degrees uses Area of sector $BAD = \frac{\theta}{360} \times \pi r^2 = \frac{"29.9"}{360} \times \pi \times 10^2$

M1 Attempts area of triangle formula: Area of triangle $ABC = \frac{1}{2}ab\sin C = \frac{1}{2}\times12\times10\times\sin^{\circ}0.5223^{\circ}$ You may see Herons formula used with $S = \frac{10+6+12}{2} = (14)$ and $A = \sqrt{S(S-10)(S-6)(S-12)}$ Watch for other methods including the calculation of a perpendicular.

dM1 Dependent upon both correct formulae. It is scored for finding area of triangle - area of sector A1 Allow awrt 3.81 or 3.82 (m²)

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8.	$ \begin{array}{c} B\\ \theta\\ 0 \\ r \end{array} $	Lb
	Figure 3	
Figure 3 shows	s a circle with centre O and radius r cm.	
The points A and	nd <i>B</i> lie on the circumference of this circle.	
The minor arc	AB subtends an angle θ radians at O, as shown in Figure 3.	
Given the leng	th of minor arc AB is 6 cm and the area of minor sector OAB	r is 20 cm ² ,
(a) write down	n two different equations in r and θ .	(2)
(b) Hence find	d the value of r and the value of θ .	(4)
18 MSB - Page 10		

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Mathematics C12

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Question Number	Scheme	Marks
8. (a)	$r\theta = 6$ and $\frac{1}{2}r^2\theta = 20$	B1 B1
		[2]
(b)	Substitute $r\theta = 6$ into $\frac{1}{2}r^2\theta = 20 \Rightarrow \frac{1}{2} \times 6r = 20$	M1
	$\Rightarrow r = \frac{20}{3}$	A1
	Substitutes $r = \frac{20}{3}$ in $r\theta = 6 \implies \theta = \frac{9}{10}$	dM1A1
		[4]
		(6 marks)

This may be marked as one complete question. Eg they may just give the equations $s = r\theta$ and $A = \frac{1}{2}r^2\theta$ in (a) Don't penalise this sort of error.

(a)

B1 Either
$$r\theta = 6$$
 or $\frac{1}{2}r^2\theta = 20$ (or exact equivalents)
Allow $\frac{\theta}{2\pi} \times 2\pi r = 6$ or $\frac{\theta}{2\pi} \times \pi r^2 = 20$ but not $\frac{\theta}{360} \times 2\pi r = 6$ or $\frac{\theta}{360} \times \pi r^2 = 20$
B1 Both $r\theta = 6$ and $\frac{1}{2}r^2\theta = 20$ (or exact equivalents)
Allow $\frac{\theta}{2\pi} \times 2\pi r = 6$ and $\frac{\theta}{2\pi} \times \pi r^2 = 20$ but not $\frac{\theta}{360} \times 2\pi r = 6$ and $\frac{\theta}{360} \times \pi r^2 = 20$
(b)

Combines two equations in r and θ producing an equation in one unknown. **M**1

 $r = \frac{20}{3}$ or $\theta = \frac{9}{10}$ or exact equivalents. A1

You may just see answers following correct equations. This is fine for all the marks This is dependent upon having started with two equations with correct expressions in r and θ dM1 Look for $..r\theta = ...$ and $..r^2\theta = ...$.

It is awarded for correctly substituting their value of r or θ into one of the equations to find the second unknown.

A1
$$r = \frac{20}{3}$$
 and $\theta = \frac{9}{10}$ or exact equivalents. Condone 6.6 for $\frac{20}{3}$ Do not allow 6.67